Transparent Semiconductor-Superconductor Interface and Induced Gap in an Epitaxial Heterostructure Josephson Junction

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Measurement of multiple Andreev Reflection (MAR) in a Josephson junction made from an InAs quantum well heterostructure with epitaxial aluminum is used to quantify a highly transparent effective semiconductor-superconductor interface with near-unity transmission. The observed temperature dependence of MAR does not follow a conventional BCS form but instead agrees with a model in which the density of states in the quantum well acquires an effective induced gap, in our case, 180 μeV, close to that of the epitaxial superconductor, indicating an intimate contact between Al and the InAs heterostructure. The carrier density dependence of MAR is investigated using a depletion gate revealing the subband structure of the semiconductor quantum well, consistent with magnetotransport experiments of the bare InAs performed on the same wafer.

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I. INTRODUCTION

The coupling of a semiconducting material with a superconductor allows for the realization of a hybrid system where certain properties of the superconductor can be harnessed in conjunction with the tunability afforded by semiconducting materials. A dramatically increased interest in such hybrid materials stems from the recent proposals to realize hybrid topological materials for quantum-information processing [1–3], as well as the successful demonstration of similar hybrid materials deployed in the setting of superconducting qubits [4,5].

From another perspective, many ballistic and mesoscopic transport effects are expected in semiconductor-superconductor hybrids [6,7] but have not been investigated due to lack of an appropriate material system. In particular, hybrid systems consisting of a superconducting metal in contact with a two-dimensional electron gas (2DEG) were widely explored in previous decades [8–11], but material difficulties hampered progress [11–14].

For all these applications, the quality of the superconductor-semiconductor interface, which controls how superconducting properties are imparted on the semiconductor, is of critical importance [15–17]. In semiconductor nanowires, the difficulty of creating strong uniform coupling to a superconductor was recently resolved by growing the superconductor material in situ by molecular beam epitaxy [18]. A hard superconducting gap measured by tunneling into the wire end indicated an intimate coupling between materials [19].

For the purposes of moving to larger integrated devices using hybrid materials for topological (or superconducting) quantum-information processing, a two-dimensional platform, which is amenable to top-down fabrication, provides an alternative and scalable path forward. In particular, state-of-the-art proposals for topological quantum-information processors require (for a single primitive) on the order of approximately six coupled topological regions aligned to quantum dots in a finely tuned manner [20]. Such a device will be dramatically simpler to construct starting from a 2D platform, as opposed to alignment of individual nanowires. Similarly, for superconducting qubits, where scalability is one of the main research directions of the field [21], the hybrid nanowire-based approach will benefit from circumventing the need for precise placement of individual nanowires by instead using Josephson junctions embedded in a 2D geometry as the nonlinear element.

A first step towards such 2DEG-based hybrid materials was recently reported, where in situ growth of Al was applied to InAs 2DEGs [22]. This system also exhibits a hard superconducting gap in tunnel spectroscopy [23], similar to the result for nanowires. Here we expand in detail...
the results on 2DEG-based hybrid materials by studying the properties of a planar Josephson junction amenable to both the pursuit of topological materials [24,25] and gateable superconducting qubits formed using top-down processing of InAs 2DEG with in situ Al grown.

II. THE JOSEPHSON JUNCTION IN A QUANTUM-WELL HETEROSTRUCTURE

We report multiple Andreev reflections (MARs) in a gateable Josephson junction formed from an InAs 2DEG epitaxial Al heterostructure. We observe a temperature dependence of the MAR peak positions that differs from expectations for a conventional BCS-like gap, but it is consistent with an induced gap in the InAs under the Al [16,17,26,27]. The appearance of an induced gap $\Delta'$ in the local density of states of the semiconductor reflects the finite time a state from the quantum well spends in the superconductor [28]. Comparing MAR data to a quantitative model (described below), we infer an induced gap $\Delta' = 180 \mu eV$ in the InAs region covered by Al and a transmission through the effective interface formed at the boundary between the covered and uncovered InAs in excess of 97%. These results are consistent with tunnel spectroscopy measurements on the same wafer [23].

The high transparency of our junction is further confirmed by the shape of the MAR features, where we observe dips in conductance when the applied voltage is a fraction of the gap, $V = 2\Delta'/eN$. This dip-to-peak transition in conductance is a longstanding prediction for highly transparent superconducting qubits formed using top-down processing and lock-in techniques, with current excitation in the range $2.5 \text{ to } 5 \text{ nA}$. As demonstrated below, at $V_g = 0$ the quantum well has two subbands (see, also, Appendix A).

The wafer is patterned into mesa structures using a standard III-V wet etch. The Al is then patterned using a selective Al etch (Transene D). Next, an unpatterned 40-nm aluminum oxide layer is deposited using atomic layer deposition. Finally, a Ti/Au gate is deposited, patterned to cover the exposed 2DEG. Figure 1(a) shows a false-color micrograph of the final device, and Fig. 1(c) shows a schematic cross section through the junction. The exposed 2DEG region has a length $L = 250 \text{ nm}$ and a width $W = 3 \mu \text{m}$. The superconducting gap of the 10-nm-thick Al layer is inferred from the critical temperature ($T_c = 1.56 \text{ K}$, independently measured in four-terminal measurement) via $\Delta_{Al} = 1.76k_BT_c = 237 \mu eV$. We note that the gap of the Al layer is larger than bulk Al [33], with $T_c$ consistent with previously reported values [34,35].

All measurements are performed in a dilution refrigerator with base temperature $T \sim 30 \text{ mK}$ using standard dc and lock-in techniques, with current excitation in the range 2.5 to 5 nA.

III. DEVICE CHARACTERIZATION

The hybrid heterostructure used in this study is grown by molecular beam epitaxy and consists (from top to bottom) of 10-nm Al, 10-nm In$_{0.8}$Ga$_{0.2}$As, 7-nm InAs (quantum well), 4-nm In$_{0.8}$Ga$_{0.2}$As, and an In$_{0.8}$Al$_{0.2}$As buffer on an InP wafer. We emphasize that the Al layer is grown in situ as part of the heterostructure [22]. Density $n = 1.26 \times 10^{12} \text{ cm}^{-2}$ and mobility $\mu = 15,600 \text{ cm}^2/\text{Vs}$ measured in a top-gated Hall bar geometry with the Al removed yield a mean free path $l_c \sim 290 \text{ nm}$ at top-gate voltage $V_g = -2.5 \text{ V}$. As demonstrated below, at $V_g = 0$ the quantum well has two subbands (see, also, Appendix A).

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All measurements are performed in a dilution refrigerator with base temperature $T \sim 30 \text{ mK}$ using standard dc and lock-in techniques, with current excitation in the range 2.5 to 5 nA.

IV. MULTIPLE ANDREEV REFLECTIONS IN QUANTUM-WELL JOSEPHSON JUNCTIONS

The theoretical approach to this system begins with the Octavio-Blonder-Tinkham-Klapwijk (OBTK) model for...
multiple Andreev reflections [36]. As originally formulated, this model assumes a well-defined voltage is dropped across the normal region (green rectangle in Fig. 1(a)), leading to the MAR process sketched in Fig. 1(b). For a planar junction where the 2DEG extends under the Al [Fig. 1(c)], the voltage can also drop along the horizontal Al 2DEG interface. In the case of imperfect Al 2DEG transparency, this voltage drop leads to smearing of the resonances arising from MAR [37,38]. The OBTK model was later extended to account for the planar geometry [26] denoted $S$-$N$-c-$N$-$S$, where $c$ is the semiconducting region in which the superconducting top layer is removed. The $S$-$N$ electrodes consisting of 2DEG with Al on top are assumed to be disordered and in equilibrium, while the exposed 2DEG region of length $L$ is assumed ballistic. The model yields a renormalized density of states in the 2DEG, with an induced gap $\Delta^* < \Delta_0$ determined by the quality of the interface between the quantum well and the Al [26].

Figure 2 shows differential conductance (left) and dc voltage (right) as a function of applied dc current for two gate voltages. The inset in Fig. 2(a) shows an enlargement indicating the excess current and critical current for $V_g = 0$ V. The critical current is $I_c = 1.77 \mu A$ yielding an $I_c R_n$ product of 165 $\mu$eV, about 70% of the gap of the Al film, and a critical current density $J_c = I_c/W = 0.59 \mu A/\mu m$. The excess current reflecting enhanced current through the junction due to Andreev reflection is defined as the $V = 0$ intercept of a linear fit to $V(I)$ taken at $V \gg \Delta_0/e$ [green dashed line in Fig. 2(a)]. The measured excess current $I_{exc} = 1.44 \mu A$ corresponds to $I_{exc} R_n = 140$ $\mu$eV [the excess current can be related to the gap via $I_{exc} = \alpha \Delta / e R_n$, where $\alpha = 8/3$ in the ballistic, fully transparent case [15], and $\alpha = (\pi^2/4-1)$ in the fully diffusive case [39]]. The differential conductance [red curve in Fig. 2(a)] shows a series of peaks and dips as the current is increased. The peak and dip structure is a manifestation of the MAR processes and is expected to follow the series $eV = 2\Delta/n$, with $n = 1, 2, 3, \ldots$ corresponding to the number of Andreev reflections.

However, a broad dip in conductance highlighted with black horizontal bar in Fig. 2(a) occurs at energies larger than $2\Delta$ but follows the temperature dependence of $I_c$ and disappears at $T_c$ (cf. Fig. 7 in Appendix B) indicating that the feature has a superconductive origin. Such anomalous resistance features are believed to be associated with the planar Josephson-junction geometry [40,41], where quasi-particles in the 2DEG can undergo several scattering events at the Al interface before ultimately undergoing Andreev reflection and traversing the same path back. On a length scale smaller than the normal-state coherence length $\xi_N = \hbar v_F / k_B T$, this process appears as an Andreev reflection from an effective boundary indicated by the gray vertical dashed line in Fig. 1(c). The finite-bias properties of such systems cannot be adequately described by either the $S$-$N$-c-$N$-$S$ or OBTK models, and the simple picture in Fig. 1(b) breaks down. With the contacts out of equilibrium, the position of the peaks in Fig. 2(a) cannot be directly related to the superconducting gap. However, by increasing the resistance in the exposed region relative to the horizontal interface, the peaks at finite bias follow a regular series and can be used to extract a value for the induced gap.

In Fig. 2(b), the gate covering the exposed 2DEG region is energized to $V_g = -2.2$ V, substantially depleting the junction, leading to a normal-state resistance $R_n = 740 \Omega$. At this gate voltage, the broad conductance dip at energies $eV > 2\Delta_0$ is absent, and the dc voltages of the first three peaks (indicated with vertical black arrows) are positioned proportional to $1/n$, that the voltage drop now occurs predominantly in the 2DEG region not covered by Al. At this gate voltage, $I_c R_n$ is reduced from the $V_g = 0$ value (full $I_c R_n$ versus $V_g$ is shown in Fig. 8 of Appendix C). As we show below, the $I$-$V$ curves in Fig. 2 are consistent with near-unity transmission through a $S$-$N$-c-$N$-$S$ junction.

In highly transparent junctions, the resonances due to MAR appear as dips in the differential conductance, as opposed to the often-used peaks. This subtle point can be appreciated by considering the nature of the current in a Josephson junction at finite voltages. In general, the current is a combination of the number of Andreev reflections $n$ and the transmission $\tau$ of the junction. For the $n$th-order Andreev reflection, the particle traverses the normal region $n + 1$ times, and neglecting the energy dependence of Andreev reflection probability, the current depends on transmission as

$$I(V) \sim (n + 1)\tau^{n+1} V. \quad (1)$$

For low $\tau$, the current, thus, decreases rapidly for higher-order Andreev reflection processes (i.e., increasing $n$). In
contrast, for very transparent interfaces, higher-order Andreev reflections will still yield an appreciable contribution to the current. This situation is demonstrated in Fig. 3(a), where we show the current in a S-N-S device calculated according to Eq. (1). For low transparencies, the slope of the $I$ versus $V$ curves increases as $n$ decreases, and the current increases at the transition from $n$ to $n-1$ Andreev reflections. As a result, the conductance of opaque junctions forms a staircase pattern that increases in voltage with peaks at the subgap features [cf. the conductance depicted with the orange and green curves in Fig. 3(b) calculated using the model of Ref. [29]]. In contrast, in the transmissive junctions, the current curve exhibits an opposite pattern, which results in a declining staircase pattern in the conductance with the peaks replaced by dips [see the purple curve in Fig. 3(b)]. This effect leads to an overall increase in the conductance between values of the voltage corresponding to integer multiples of the gap (i.e., at $V = 2\Delta/e$). Therefore, the vertical arrows in Fig. 2(b) point to local minima, not maxima, in conductance to indicate multiples of the gap arising from the relation $V = 2\Delta/e$.

V. ELECTROSTATIC GATE DEPENDENCE

To extract the value of $\Delta^*$, we plot the conductance from Fig. 2 against the dc voltage drop, as shown in Fig. 4(a). The theoretical MAR resonances in Fig. 4(a) are simulated using a generalized scattering matrix approach developed for S-N-S junctions [29,42]. Within the model of an induced gap [26], the S-N-c-N-S system is interpreted as an effective $S'$-N-$S'$ junction, where $S'$ is the superconducting quantum well covered by Al with a gap $\Delta^*$ and a critical temperature identical to that of the parent superconductor. Simulations are performed by calculating the conductance $G^{(i)}(V)$ of a single mode with transmission $\tau$ from the dc component of the current $I^{(i)}(V,t) = \sum_k I_k^{(i)} \exp(2i k e V t / \hbar)$. The time-independent Fourier component of $I_k^{(i)}$ is calculated from the functions of the quasiparticles accelerated by the voltage $V$ across the junction. In the case of a ballistic junction ($L < l_c$), the backscattering effectively occurs only at the boundary between $S'$ and $N$ [vertical gray dashed line in Fig. 1(c)]. The total current through the junction is the sum of currents carried by $N$ modes in $M$ subbands. The resulting conductance through the multimode junction is given by $G(V) = \sum_i^M N_i G^{(i)}(V)$ where $N_i$ is the number of modes in the $i$th subband, and $\tau_i$ is the transmission of the modes in the $i$th subband.

A nonlinear least-squares procedure is used to fit simulated $G(V)$ curves to the data in Fig. 4(a), where $\tau_i$, $\Delta^*$, and $N$ are fitting parameters, and $M$ is predefined (see, also, Ref. [43]). The minimal number of subbands needed to capture the essential features of the data is found to be $M = 2$. For $M > 2$, the optimal fit does not populate the $i > 2$ subbands (i.e., $N_i \sim 0$ for $i > 2$), indicating that the data are well described by two subbands (in Fig. 9 of Appendix D, we show simulations using $M = 1$ and $M = 3$). The result of fitting to the MAR features at two $V_g$ values are shown as dashed curves in Fig. 4(a). At $V_g = 0$, the induced gap is $\Delta^* = 182$ $\mu$eV with $N_1 = 199$, $N_2 = 109$, $\tau_1 = 0.98$, and $\tau_2 = 0.8$. When the gate is energized to $V_g = -2.2$ $V$, the fitting values are $\Delta^* = 180$ $\mu$eV, with $N_1 = 100$, $N_2 = 29$, $\tau_1 = 0.97$, and $\tau_2 = 0.65$. The gate-voltage dependence of the fitting parameters $\tau_i$ and $N_i$ are shown in Figs. 4(c) and 4(d).
The gap $\Delta^*$ extracted from the fitting routine is identical to the one measured in a tunneling experiment on the same wafer [23].

The presence of two transmission species in the optimal fit is attributed to the 2DEG having two occupied subbands. The carrier density in the 2DEG denoted $n_{\text{Hall}}$ is measured in a Hall bar geometry via the Hall slope [shown in Fig. 4(b)]. The density from the Hall slope is compared to the density extracted from the periodicity of the Shubnikov–de Haas (SdH) oscillations in an out-of-plane magnetic field. The data in Fig. 4(b) show the density change in the 2DEG as the top gate is energized. The power spectrum of $\rho_{xx}(1/B)$ exhibits a two-peak structure indicating two subbands with different densities in the quantum well at $V_g = 0\, \text{V}$ [44]. The density corresponding to the major peak is denoted $n_1$, and the difference $n_{\text{Hall}} - n_1$ is denoted $n_2$. The density in the two subbands changes as the top gate is energized, as shown in Fig. 4(b), similar to $N_1$ and $N_2$ extracted from fitting to the MAR features. In particular, the $N_2$ species becomes depopulated at a gate voltage similar to the depletion of the second subband in the Hall bar [Fig. 4(b)]. The decrease of transmission of the $i = 2$ species in Fig. 4(c) could be due to a breakdown of the ballistic assumption as the second subband is depleted.

Within the 1D Blonder-Tinkham-Klapwijk formalism for a $S$-$N$ interface, the transparency is often parameterized using the dimensionless quantity $Z$ related to the transmission via $\tau = (1 + Z^2)^{-1/2}$ [15]. For the first subband, we extract an average transmission $\tau_1 \approx 0.97$ corresponding to a $Z$ parameter of $Z_1 \approx 0.18$. This low $Z$ parameter indicates that the effective interface between the uncovered quantum well and the region covered by Al is pristine.

### VI. ELUCIDATING THE INDUCED GAP

The distinction between a BCS-like gap $\Delta_{Al}$ and an induced gap $\Delta^*$ is revealed through the temperature dependence of the superconducting properties. In the case where the effective thickness of the quantum well is much less than the normal-state coherence length $d_N \ll \xi_N$, any position dependence of the gap magnitude in the growth direction in the 2DEG can be neglected, and the temperature dependence of the induced gap depends on $\Delta_{Al}$ according to [10,26,45]

$$
\Delta^*(T) = \frac{\Delta_{Al}(T)}{1 + \gamma_B \sqrt{\Delta_{Al}^2(T) - \Delta^2(T)} / \pi k_B T_c},
$$

where $\Delta_{Al}(T)$ is determined self-consistently from BCS theory. The dimensionless parameter $\gamma_B$ is a measure of the horizontal $S$-$N$ interface transparency [black horizontal dashed line in Fig. 1(c)], where $\gamma_B = 0$ corresponds to a perfectly transparent interface [46]. The parameter $\gamma_B$ represents the discontinuity in the superconducting pair potential and gives rise to the difference between the gap in aluminum $\Delta_{Al}$ and the induced gap $\Delta^*$ in the 2DEG denoted $\delta$ in Fig. 1(c). For the present case, we find $\gamma_B = 0.87$ using $\Delta^* = 180\, \mu\text{eV}$ and $\Delta_{Al} = 237\, \mu\text{eV}$ consistent with a high-quality interface between the quantum well covered by Al and the Al itself.

To elucidate the nature of the induced superconducting gap, we study the temperature dependence of the differential conductance at $V_g = -2.2\, \text{V}$ shown in Fig. 5(a). The position of the second MAR-related dip (denoted $p_2$) is tracked in Fig. 5(b) as the temperature is increased. The curves in Fig. 5(b) show the solution of Eq. (2) (purple), temperature dependence of a BCS gap $\Delta_{Al}(T)$ (teal), and a BCS-like gap $\Delta'_c(T)$ (teal, dashed), where the gap value is rescaled to coincide with the data at $T = 30\, \mu\text{K}$. The inadequacy of the temperature dependence of a BCS-like gap (both unscaled and rescaled) to account for the temperature dependence of the peaks is contrasted by the good correspondence between Eq. (2) and our data. The temperature dependence of the first and third dip positions $p_1$ and $p_3$ are shown in Fig. 5(c). The curves identified with $p_1$ and $p_3$ are found by multiplying $\Delta^*(T)$ by a factor of 2 and 2/3, respectively, corresponding to $n = 1$ and $n = 3$ in the $2/n$ MAR series.

The small deviation between $V(p_2) \approx 0.21\, \text{meV}$, which one might expect is located at $V = 2\Delta^*/(2e) = \Delta^*/e$, and the gap extracted from the fitting in Sec. V ($\Delta^* \sim 0.18\, \text{meV}$) can be understood by again appealing to the simulation in Fig. 3(b). There, the black vertical arrow shows the minimal conductance close to the $n = 2$ MAR resonance, which does not coincide exactly with

![FIG. 5.](image-url)
Δ/e. From the simulation, we see that the voltage difference from the resistance maxima at the vertical arrow and the gap is approximately 10%, in good agreement with \( V(p_2) \) and \( \Delta \) which differ by approximately 14%. Regardless, the correspondence between the temperature dependence of the MAR features and temperature dependence of the gap is unchanged by this effect, and the excellent agreement also with \( n = 1 \) and \( n = 3 \) resonances indicates that the superconducting properties of the junction are well described within the induced gap model.

VII. CONCLUSION AND OUTLOOK

In conclusion, we measure MAR resonances in a Josephson junction in an InAs 2DEG heterostructure, where aluminum is epitaxially matched to the 2DEG. By fitting the conductance of the MAR features, we extract a transmission close to unity through an effective S’-N-S’ junction, where S’ represents the InAs quantum well covered by the Al. The temperature dependence of the MAR resonances is well described by the theory of an effective induced gap, and we find \( \Delta' = 180 \mu eV \) in the 2DEG region covered by Al, close to the gap of the Al itself, indicating a transparent interface between the two.

The intrinsic flexibility offered by the hybrid system presented here, combined with the quality of the coupling between semi- and superconductor, makes this material a promising candidate for exploring scalable topological and superconducting quantum-information systems. As an example of this platform, we mention that the quality of the 2DEG allows a monotonic suppression of \( I_c \) as the top gate is used to deplete (shown in Fig. 8). Such a property is highly desirable within the gateon superconducting-qubit architecture, where the qubit frequency is determined in part by the value of \( I_c \) and is the key control parameter [47]. Finally, we mention that several recent proposals [24,25] show that planar Josephson junctions, as the type that we demonstrate here, can be tuned into a topological regime with minor adjustments to the device geometry.

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M. K. and H. J. S. contributed equally to this work.

APPENDIX A: MOBILITY PEAK AND SUBNIKOV–DE HAAS OSCILLATIONS

In Fig. 6(a), the gate dependence of the 2DEG mobility is shown, measured in the same Hall bar as the data in Fig. 4(b) of the main text. The mobility peak is at \( V_g = -2.75 \) V, the same gate-voltage value at which \( n = 0 \) [see Fig. 4(b)], consistent with the interpretation of a mobility-limiting second subband being depleted. Two examples of Shubnikov–de Haas oscillations of \( \rho_{xx} \) are shown in Fig. 6(b) at \( V_g = 0 \) V (the two-subband regime) and \( V_g = -2.5 \) V (the one-subband regime).

APPENDIX B: TEMPERATURE DEPENDENCE OF THE ANOMALOUS RESISTANCE PEAK

Figure 7 shows the evolution of the differential resistance as the temperature is increased at \( V_g = 0 \) V. The anomalous resistance peak discussed in Fig. 2(a) of the main text (highlighted with horizontal black bar) has identical temperature dependence to other superconducting features of the device. The complementary data at \( V_g = -2.2 \) V are shown in Fig. 5 and are used for extracting the temperature dependence of the gap.

FIG. 6. (a) Mobility of the 2DEG as a function of top-gate voltage measured in a Hall bar. (b) Shubnikov–de Haas oscillations at two values of top-gate voltage in a Hall bar.

FIG. 7. Temperature dependence of differential resistance at \( V_g = 0 \) V. Curves successively offset by 25 \( \Omega \) except for \( T = 0.05 \) K. Horizontal bars indicate positions of the anomalous resistance peak.
APPENDIX C: GATE DEPENDENCE OF THE SUPERCONDUCTING PROPERTIES OF THE 2DEG

The gate-voltage dependence of the differential resistance of the S-2DEG-S junction is shown in Fig. 8. At $V_g = -2.5 \, \text{V}$, the junction is no longer able to sustain a supercurrent, and the normal-state resistance is $R_n = 1.7 \, \text{k} \Omega$. The $I_cR_n$ product has only a weak dependence on gate voltage [Fig. 8(b)], with a maximum $I_cR_n \approx 250 \, \mu \text{eV}$ at $V_g = -1.95 \, \text{V}$.

APPENDIX D: SUBBANDS IN THE SIMULATIONS

In the main text, we introduce the simulations used to fit the MAR features in Fig. 4(a). The fit procedure takes as input a fixed number of subbands denoted $M$, which can have a different number of modes $N$ and transmission $\tau$. At $V_g = 0 \, \text{V}$, we find the optimal subband number is $M = 2$. As shown in Fig. 9, at $M = 1$ the fit is visibly worse, while for $M = 3$ the optimal least-squares fit to the experimental data does not involve any modes in the third subband, i.e., $N_3 = 0$. We note that for $M = 3$ and a specific choice of the initial guess of the parameters, the fitting procedure can distribute modes among all three subbands, creating two subbands that are almost degenerate in transmission probability. When this happens, the fitting errors of $N_i$ and $\tau_i$ are larger than the fitted values by several orders of magnitude, and, hence, we disregard such solutions. In Table I, we list the number of modes in the optimal least-squares fit for $M = 1, 2, 3$.

<table>
<thead>
<tr>
<th>$M$</th>
<th>$N_1$</th>
<th>$N_2$</th>
<th>$N_3$</th>
<th>$\tau_1$</th>
<th>$\tau_2$</th>
<th>$\tau_3$</th>
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<td></td>
<td>0</td>
<td>0.98</td>
<td></td>
<td></td>
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<td>0.98</td>
<td>0.8</td>
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<td>123</td>
<td>0</td>
<td>0.98</td>
<td>0.82</td>
<td>n.a.</td>
</tr>
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</table>

Based on these results, we choose $M = 2$ for the remaining simulations.


