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Uncertainty in geocenter estimates in the context of ITRF2014

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Abstract Uncertainty in the geocenter position and its subsequent motion affects positioning estimates on the surface of the Earth and downstream products such as site velocities, particularly the vertical component. The current version of the International Terrestrial Reference Frame, ITRF2014, derives its origin as the long-term averaged center of mass as sensed by satellite laser ranging (SLR), and by definition, it adopts only linear motion of the origin with uncertainty determined using a white noise process. We compare weekly SLR translations relative to the ITRF2014 origin, with network translations estimated from station displacements from surface mass transport models. We find that the proportion of variance explained in SLR translations by the model-derived translations is on average less than 10%. Time-correlated noise and nonlinear rates, particularly evident in the Y and Z components of the SLR translations with respect to the ITRF2014 origin, are not fully replicated by the model-derived translations. This suggests that translation-related uncertainties are underestimated when a white noise model is adopted and that substantial systematic errors remain in the data defining the ITRF origin. When using a white noise model, we find uncertainties in the rate of SLR X, Y, and Z translations of ±0.03, ±0.03, and ±0.06, respectively, increasing to ±0.13, ±0.17, and ±0.33 (mm/yr, 1 sigma) when a power law and white noise model is adopted.

1. Introduction

The need to monitor global change processes, such as sea level change and postglacial rebound, at a level below 1 mm/yr, illustrates the requirement for an accurate and precise global geodetic reference frame. The International Terrestrial Reference Frame (ITRF) [Altamimi et al., 2007, 2011, 2016] attempts to meet accuracy and stability goals of 1 mm and 0.1 mm/yr, respectively [Gross et al., 2009]. As each iteration of the ITRF provides improvements in the precision and accuracy of the global reference frame, challenges remain to meet the accuracy and stability goals. Particularly challenging is the realization of the origin (defined as the long-term averaged center of mass (CM) of the Earth) and its evolution in time [Dong et al., 2014]. Presently, this realization is limited given that it is determined using measurements from a single measurement technique (satellite laser ranging (SLR)) [Altamimi et al., 2016; Wu et al., 2011] that is known to be affected by systematic biases and network asymmetry [Appleby et al., 2016]. The ITRF2014 (and each predecessor) is a linear frame by definition, and consequently, the long-term motion of its origin is described by a linear trend. Limitations arise given that when specifying the ITRF origin to coincide with the long-term origin of the SLR frame, only time-constant annual and semiannual terms are included with a white noise model [Altamimi et al., 2007, 2011, 2016; Argus, 2012], neglecting any other nonlinear motions as part of the functional or stochastic model.

Relative motion between the center of mass of the total Earth system (CM) and the center of surface figure (CF) of the solid Earth can be observed using space geodetic observations that tie Earth-fixed permanent geodetic sites and space-based satellite platforms. Both secular and seasonal geocenter motion occur as a result of past and present mass redistribution, where geocenter motion is the difference between CM and CF (the difference between geophysically determined origins). Past mass redistribution on the surface or interior such as glacial isostatic adjustment (GIA) induces secular geocenter motion, while intra-annual, seasonal, and interannual signals relate to present-day distributions, such as exchanges within and between the ocean, atmosphere, continents, and cryosphere [Argus, 2012; Dong et al., 1997; Wu et al., 2012]. SLR translations with respect to the ITRF2014 origin therefore consist of both measurement error and a component of real geocenter motion affected by the nonhomogenous network distribution of SLR tracking stations. This leads to a
sampling bias known as the “network effect,” and should ideally reflect the offset between the network origin (CN) and the CM rather than the geocenter motion.

An alternative approach to studying geocenter motion uses observations and numerical models of surface mass transport to derive deformation of the solid Earth at the locations of the SLR stations (that change over time), from which network translations may be estimated. The mass transport models provide bounds on the network translations which are to be expected from known surface loading processes. Any inconsistency between observed SLR translations and those derived from a surface loading model will hint at problems in either the SLR methods (observations or processing) or problems within the surface loading model. In this paper, SLR translations and output from two surface loading models are used to assess the uncertainty in the SLR translations with respect to the ITRF2014 long-term origin.

2. Data

The origin of ITRF2014 is defined such that there are zero translation parameters and rates at epoch 2010.0 between the International Laser Ranging Service (ILRS) long-term mean origin from SLR and ITRF2014 [Altamimi et al., 2016]. The SLR temporal translation components used here have been derived with respect to the ITRF2014 origin that has been defined using the internal constraint method described in Altamimi et al. [2007] and Altamimi et al. [2016]. The translations were estimated using a seven-parameter similarity transformation between each week and a SLR ITRF2014 network of 21 core stations. The time series of the seven parameters were adjusted globally, in one run using the CATREF software (Combination and Analysis of Terrestrial Reference Frames) [e.g., Altamimi et al., 2016], with the full variance-covariance information of the total SLR SINEX time series. We analyze the translations from weekly combined SLR solutions relative to the ITRF2014 (linear) origin over the time span 1993.0 to 2015.0 in the temporal and spectral domains. The complete ILRS SLR reference frame solutions in SINEX format submitted for the realization of ITRF2014 covers the time span 1983.0 to 2015.0. Only the data from 1993.0 onward are used here due to noisy data in the early section of the time series, producing large formal uncertainties in the SLR translation series before the LAGEOS-2 satellite was launched in 1992 [Dong et al., 2014]. We compare the SLR translation time series with respect to the ITRF2014 long-term origin with two different estimates of network translations that are derived from independent surface mass transport models.

The ITRF2014 origin is considered theoretically representative of the long-term CM, where geocenter motion is defined as motion of the CM with respect to the CF [Altamimi et al., 2016]. Linear motions for ground stations are assumed, with some discontinuities and postseismic deformations enforced for sites affected by major earthquakes or equipment changes. The ITRF origin reflects CM on secular timescales due to it coinciding with the long-term average CM as observed by SLR, but on shorter (including seasonal) timescales, the ITRF origin reflects CF [Blewitt, 2003; Collilieux et al., 2009; Dong et al., 2003]. We note that some of the literature considers the opposite convention, that is, displacement of CF with respect to CM [e.g., M"{e}tivier et al., 2010; Dong et al., 2014].

Our first comparative geophysical model is from Rietbroek et al. [2015], who calculated surface mass transport loading based on a combination of Gravity Recovery and Climate Experiment (GRACE) and radar altimetry data using an inversion approach that applied conservation of mass to solve the sea level equation [Rietbroek et al., 2016]. Surface displacement components are provided for the time span 2002.3 to 2014.5 with monthly sampling, hereon referred to as R15. R15 considers mass redistribution from the Antarctic and Greenland ice sheets, land glaciers, GIA, continental water storage, and contributions from the oceans and atmosphere. Although GRACE alone is not capable of observing degree-1 mass redistribution, combination with additional data sets and use of an inversion methodology enables derivation of surface mass transport values. The short data span is limiting given that it covers only half of the SLR series but remains useful given the independent GRACE-based approach.

Our second data set was estimated from numerical surface mass transport models and solves the sea level equation to conserve mass for the global system after taking into account self-atraction and loading effects [Gordeev et al., 1977; Frederikse et al., 2016; Tamisiea et al., 2010] using fingerprints [Mitrovica et al., 2001] to represent the nonuniform redistribution of water. Hereon, this modeled surface mass product is referred to as MSM. MSM yields values over the time span 1993.0 to 2015.0 with monthly sampling. This data set includes modeled ocean and atmosphere mass redistribution (defined using the
two models. Our use of two geophysical models aims to re
contribute to each model. Further information on the model uncertainties can be found in the associated
data sets in the temporal domain sampled at monthly epochs for clarity. The surface deformation values at
removed from the SLR translation components as these are signals of interest. Figures 1a
weekly solutions over the time span 1993.0 to 2015.0. Annual and semiannual periodic signals were not
By construction, there are zero translation rates (trends) between ITRF2014 and the SLR stacked frame of
other terrestrial water storage from the Noah Global Land Data Assimilation System (GLDAS) product
Both the land glacier and dam retention components are sampled annually and have
been linearly interpolated to monthly intervals for consistency with the other data sets, constraining the
temporal resolution. It would be expected for these components to contain annual signals due to the
seasonal nature of hydrologic mass exchange, and we return to this in section 4. A groundwater com-
ponent is available using data from Wada et al. [2010]. The contribution from groundwater to the overall
signal is primarily linear with very small annual amplitude for the available period. Further data descrip-
tion for MSM is available in the supporting information (Text S1) and Frederikse et al. [2016], including
uncertainties for the component contributions.

Surface displacements from each geophysical model were derived by redistributing loaded masses within a
thin shell on the Earth’s surface. They are spherically symmetric, stratified, and nonrotating Earth responses
elastically redistributed over subsecular (subdaily to decadal) timescales. The displacements are proportional
to the incremental load potential according to the load Love number theory [Farrell, 1972] and are derived
from the preliminary reference Earth model elastic Earth model (PREM) [Dziewonski and Anderson, 1981].

Following the methodology of Collilieux et al. [2009], network translations have been derived from station dis-
placements due to loading effects from two distinct surface mass transport models and compared with SLR
translations with respect to the ITRF2014 long-term origin to account for the network effect of the SLR
station geometry.

From each of the geophysical models, network translations are computed following the methodology of
Collilieux et al. [2009], using the ITRF2014 station positions and velocities plus the modeled surface mass load-
ing deformation at each epoch of the respective data set. At each epoch, we used only those SLR sites that
were active. The monthly surface deformation values are interpolated from monthly to weekly values using
a cubic spline. The two synthetic time series are then used to estimate transformation parameters, using
Globk [Herring et al., 2015], with respect to ITRF2014 using the full covariance matrix of the ILRS combined
solution submitted for ITRF2014 analysis. Following Collilieux et al. [2012], only three rotations and three
translations were estimated (that is, scale was not estimated). Repeating the analysis with the scale parameter
included produced only negligible changes to the estimated transformation parameters. Covariance informa-
tion was used as given; an occasional site was automatically removed for a given week due to the estimated
station adjustments being larger than 10 sigma. Given that the ILRS combined solution was generated using
a loose constraint approach, correlations exist between the Helmert parameters where some of the station
placements may leak into the rotation parameters [Collilieux et al., 2009]. Here the rotations have a mean
and standard deviation of 0.00±0.02 milliseconds of arc for all components from both models (1 sigma),
which induces station displacements below 1 mm.

The two network translation models, R15 and MSM, are compared with the SLR translation components
with respect to the ITRF2014 origin to assess the sensitivity of the SLR observed origin against geophysically
modeled geocenter motion taking into account the network effect of the SLR observing network.

3. Comparison of SLR and Modeled Network Translations

By construction, there are zero translation rates (trends) between ITRF2014 and the SLR stacked frame of
weekly solutions over the time span 1993.0 to 2015.0. Annual and semiannual periodic signals were not
removed from the SLR translation components as these are signals of interest. Figures 1a–1c show the three
data sets in the temporal domain sampled at monthly epochs for clarity. The surface deformation values at
each site were detrended before transformation [Collilieux et al., 2009]. Formal errors are not available for
either of the surface mass transport models, but uncertainties are available for the constituent data sets that
contribute to each model. Further information on the model uncertainties can be found in the associated
references. Our use of two geophysical models aims to reflect, at least partly, the uncertainty in the
two models.
Figures 1d–1f show the SLR translations alongside the differences of R15 and MSM with SLR, where the qualitative agreement of the curves reveals that the differences are heavily influenced by signal not in R15 and MSM. Considering the residual series, the percentage of SLR variance explained by R15 is 12.5%, 1.3%, and 2.1% for the X, Y, and Z components, respectively, with MSM explaining 8.1%, 4.0%, and 2.0%, respectively. The small proportion of variance explained by the surface mass transport models indicates that either the geophysical models are not able to capture the surface mass transport variability or systematic errors from the SLR technique are substantial. The visual agreement between R15 and MSM is noteworthy given the dissimilarity in the data used to construct the series. Surface thermoelastic effects, with annual amplitudes...
### Table 1. Noise Parameters From HECTOR of the Full SLR Data Set and MSM Network Translation Model [1993.0 2015.0]a

<table>
<thead>
<tr>
<th>Model</th>
<th>SLR</th>
<th>MSM</th>
<th>SLR-MSM</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>White-Only</td>
<td>PLW</td>
<td>GGM</td>
</tr>
<tr>
<td><strong>AIC</strong></td>
<td>1323.350</td>
<td>1282.103</td>
<td>1256.500</td>
</tr>
<tr>
<td><strong>BIC</strong></td>
<td>1323.350</td>
<td>1289.263</td>
<td>1263.659</td>
</tr>
<tr>
<td><strong>k</strong></td>
<td>0</td>
<td>-0.80</td>
<td>0.98 ± 0.30</td>
</tr>
<tr>
<td><strong>1 phi</strong></td>
<td></td>
<td></td>
<td>0.51 ± 0.14</td>
</tr>
<tr>
<td><strong>STD</strong></td>
<td>2.939</td>
<td>2.689</td>
<td>2.570</td>
</tr>
<tr>
<td><strong>Bias (mm)</strong></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td><strong>Trend (mm yr</strong>⁻¹**)**</td>
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<tr>
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<td></td>
<td>White-Only</td>
<td>PLW</td>
<td>GGM</td>
</tr>
<tr>
<td><strong>AIC</strong></td>
<td>1371.096</td>
<td>1222.215</td>
<td>1192.371</td>
</tr>
<tr>
<td><strong>BIC</strong></td>
<td>1371.096</td>
<td>1229.374</td>
<td>1199.531</td>
</tr>
<tr>
<td><strong>k</strong></td>
<td>0</td>
<td>-0.98</td>
<td>0.98 ± 0.13</td>
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<tr>
<td><strong>1 phi</strong></td>
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<td>0.29 ± 0.08</td>
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<tr>
<td><strong>STD</strong></td>
<td>3.216</td>
<td>2.391</td>
<td>2.275</td>
</tr>
<tr>
<td><strong>Bias (mm)</strong></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td><strong>Trend (mm yr</strong>⁻¹**)**</td>
<td></td>
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</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>White-Only</td>
<td>PLW</td>
<td>GGM</td>
</tr>
<tr>
<td><strong>AIC</strong></td>
<td>1761.462</td>
<td>1638.007</td>
<td>1585.610</td>
</tr>
<tr>
<td><strong>BIC</strong></td>
<td>1761.462</td>
<td>1645.166</td>
<td>1592.769</td>
</tr>
<tr>
<td><strong>k</strong></td>
<td>0</td>
<td>-0.93</td>
<td>1.48 ± 0.32</td>
</tr>
<tr>
<td><strong>1 phi</strong></td>
<td></td>
<td></td>
<td>0.48 ± 0.10</td>
</tr>
<tr>
<td><strong>STD</strong></td>
<td>6.717</td>
<td>5.252</td>
<td>4.777</td>
</tr>
<tr>
<td><strong>Bias (mm)</strong></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td><strong>Trend (mm yr</strong>⁻¹**)**</td>
<td></td>
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</tr>
</tbody>
</table>

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*aAIC is a measure of the relative quality of statistical models for a given set of data; BIC is a criterion for model selection among a finite set of models; the model with the lowest AIC/BIC value is preferred; k is the spectral index; 1 phi is a GGM parameter; STD is the standard deviation (units mm).*
approaching 3 mm for radial displacements and 1.5 mm for transverse displacements [Xu et al., 2017], could explain some of the difference between the SLR translations and the respective network translations.

3.1. Seasonal Variation
The dominant signal throughout the SLR translation series has an annual period with apparent variable amplitude. Over the full time series, the SLR translation annual signal in the Z component is approximately twice that of the SLR translation X and Y components (see Table 1). The greatest agreement in overall amplitude and its temporal variation between SLR, R15, and MSM is found in the X component, which is predominantly ocean driven due to the limited land area along the X axis (X is in the direction of 0°N 0°E, Y of 0°N, and Z of 90°N).

The annual signal expressed in the residuals for each coordinate component (Figures 1d–1f, SLR minus model) computed between the SLR origin and model-based network translation estimates demonstrates reasonable qualitative agreement in phase and amplitude, again demonstrating that both the R15 and MSM models significantly underestimate the amplitude of the annual signal within the SLR translations. To explore the strength of the annual signals more closely, we computed the power spectral density (PSD) using the Lomb-Scargle approach described by Press et al. [1992]. Figure 2 shows the PSD for each data set across each coordinate component. Lower frequency trends are less well resolved by R15 due to the restricted temporal span, and care should be taken not to overinterpret differences at these frequencies.

The annual signal expressed in MSM significantly underestimates the observed SLR amplitude in all components, particularly during the latter part of the Y component time series (Figure 1b) and remains visible as a peak in the residual PSD (Figure 2e). The shorter duration R15 model also underestimates the magnitude of the annual signal, where the most notable differences for both R15 and MSM are with respect to the Z component (Figure 1c). This is confirmed by the presence of a residual peak at the 1 c/yr frequency in Figures 2d–2f.
The SLR series was compared with the MSM translations over the same time span as R15 (results not plotted here). In this analysis, the annual signal amplitude and phase of MSM were not statistically different from R15 in comparison to SLR over the shortened time span. The MSM data set, over the R15 time span, is very similar to the SLR Y component but has reduced agreement with the SLR X and Z components, particularly in the latter part (2002 onward) of the time series (similarly as for R15) where the signal deviates (Figure 1). That the surface mass transport models are indistinguishable from each other in the later part of the time series provides confidence in their construction, noting again the dissimilarities in their constituent data series.

The magnitude-squared coherence of the SLR time series with each of the models in Figure 3 provides further evidence that an annual signal is clearly present in both the observations from SLR and the network translation estimates from geophysical models. A strong peak in each component is centered about 1 c/yr, with an average magnitude-squared coherence of 0.9 across the X, Y, and Z components. Figure 3a shows that agreement in the X component is poor for signals other than annual, particularly between SLR and R15. Better agreement at other frequencies is evident in the Y and Z components between SLR and the network translation models. Other less significant peaks are observed at subannual periods, but they are not considered further here.

To assess the time variability of the time series, we follow a similar method to Argus [2012], whereby each time series is divided into 4 year segments, each overlapping by 1 year, producing seven segments in our analysis. A linear plus seasonal model was fitted to each segment, with the amplitude for each origin component shown in Figures 4a–4c, each centered on the midpoint of the segment. Four years is sufficient to reliably estimate the linear plus annual and semiannual terms [Blewitt and Lavallée, 2002]. For the SLR data, a number of annual amplitudes computed from segmented data are significantly different to those computed over the full series in the Y and Z components. While natural variation in these terms is expected, some of the behavior appears systematic and specific to SLR. For example, the Y component shows a marked reduction in amplitude following the segment centered on 2003.5 (Figure 4b), which is not reflected in the R15 data, and only marginally reflected in the MSM data. The largest variability in SLR annual amplitude is found in the Z component (Figure 4c), with the large deviation in the segment centered on 1997.5 not reproduced by either R15 or MSM.

We also note a decrease in the uncertainty of the annual amplitude across the SLR data segments, most noticeably in the X and Z components. This perhaps reflects refinements in the SLR observing networks' geometry and operation capacity over time [Varghese, 2013].

3.2. Noise Characteristics

Examination of Figure 2 shows clear features other than the dominant annual signals. The noise floor of the SLR data set is substantially higher than that of both the network translation models, presumably associated the effect of measurement error. The SLR X component (Figure 2a) shows a flatter (whiter) spectrum than in Y and Z indicating increased time-correlated noise in the latter components. The spectra of SLR-R15 and SLR-MSM (Figures 2d–2f) also suggest time-correlated noise across each component.
Figure 4. (a–c) Annual amplitude and uncertainty of each network translation component where each data set has been segmented into 4 year segments with 1 year overlap for SLR, R15, and MSM with a PLW noise model. Uncertainties are one sigma. (d–f) Linear rates and uncertainty with a PLW noise model of the time series (Figures 1d–1f). The shaded area is the respective amplitude and linear rate values for the full SLR time series with 1 sigma uncertainty [1993.0–2015.0]. R15 and MSM have been offset in time for clarity. Four year segments are as follows: 1993.0–1997.0, 1996.0–2000.0, 1999.0–2003.0, 2002.0–2006.0, 2005.0–2009.0, 2008.0–2012.0, and 2011.0–2015.0.
<table>
<thead>
<tr>
<th>Model</th>
<th>AIC</th>
<th>BIC</th>
<th>k</th>
<th>STD</th>
<th>Bias (mm)</th>
<th>Trend (mm yr⁻¹)</th>
</tr>
</thead>
<tbody>
<tr>
<td>X</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>SLR</td>
<td>717.384</td>
<td>688.717</td>
<td>668.043</td>
<td>205.392</td>
<td>0.000 ± 0.229</td>
<td>0.000 ± 0.065</td>
</tr>
<tr>
<td>R15</td>
<td>694.698</td>
<td>674.024</td>
<td>1.13 ± 0.39</td>
<td>0.90</td>
<td>−0.008 ± 3.682</td>
<td>−0.014 ± 0.270</td>
</tr>
<tr>
<td>SLR-R15</td>
<td>203.392</td>
<td>188.084</td>
<td>0.67</td>
<td>2.464</td>
<td>0.026 ± 0.040</td>
<td>0.009 ± 0.012</td>
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<tr>
<td>White-Only</td>
<td>171.120</td>
<td>177.087</td>
<td>0.47</td>
<td>2.313</td>
<td>−0.022 ± 0.413</td>
<td>0.012 ± 0.032</td>
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<td>PLW</td>
<td>628.424</td>
<td>624.247</td>
<td>0.44 ± 0.23</td>
<td>0.47</td>
<td>0.004 ± 0.115</td>
<td>0.009 ± 0.017</td>
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<tr>
<td>GGM</td>
<td>623.919</td>
<td>629.886</td>
<td>0.29 ± 0.07</td>
<td>0.489</td>
<td>−0.104 ± 0.075</td>
<td>−0.010 ± 0.065</td>
</tr>
<tr>
<td>1 phi</td>
<td>0.50 ± 0.16</td>
<td>0.043 ± 0.040</td>
<td>0.31 ± 0.11</td>
<td>0.225</td>
<td>0.003 ± 0.038</td>
<td>0.004 ± 0.014</td>
</tr>
<tr>
<td>Y</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>SLR</td>
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<td>646.078</td>
<td>628.424</td>
<td>−20.596</td>
<td>0.000 ± 0.220</td>
<td>0.000 ± 0.062</td>
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<tr>
<td>R15</td>
<td>652.059</td>
<td>634.405</td>
<td>0.92 ± 0.19</td>
<td>0.93</td>
<td>0.204 ± 3.932</td>
<td>0.079 ± 0.245</td>
</tr>
<tr>
<td>SLR-R15</td>
<td>−37.551</td>
<td>−40.178</td>
<td>−0.63</td>
<td>2.020</td>
<td>−0.001 ± 0.091</td>
<td>−0.006 ± 0.005</td>
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<td>White-Only</td>
<td>−46.146</td>
<td>−50.747</td>
<td>0.39 ± 0.11</td>
<td>0.225</td>
<td>0.003 ± 0.038</td>
<td>−0.001 ± 0.014</td>
</tr>
<tr>
<td>PLW</td>
<td>572.596</td>
<td>557.252</td>
<td>0.12 ± 0.12</td>
<td>0.205</td>
<td>0.325 ± 0.142</td>
<td>−0.004 ± 0.010</td>
</tr>
<tr>
<td>GGM</td>
<td>550.747</td>
<td>556.514</td>
<td>0.06 ± 0.06</td>
<td>0.204</td>
<td>0.357 ± 0.962</td>
<td>−0.387 ± 0.041</td>
</tr>
<tr>
<td>1 phi</td>
<td>0.63</td>
<td>0.39 ± 0.11</td>
<td>0.000 ± 0.123</td>
<td>0.394</td>
<td>0.066 ± 0.005</td>
<td>−0.351 ± 0.019</td>
</tr>
<tr>
<td>Z</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>SLR</td>
<td>905.651</td>
<td>860.284</td>
<td>832.483</td>
<td>141.685</td>
<td>0.000 ± 0.434</td>
<td>0.000 ± 0.123</td>
</tr>
<tr>
<td>R15</td>
<td>866.265</td>
<td>838.464</td>
<td>1.33 ± 0.37</td>
<td>−0.95</td>
<td>−0.023 ± 10.493</td>
<td>−0.66 ± 0.529</td>
</tr>
<tr>
<td>SLR-R15</td>
<td>121.640</td>
<td>112.263</td>
<td>0.49 ± 0.13</td>
<td>0.49</td>
<td>0.006 ± 0.060</td>
<td>0.032 ± 0.239</td>
</tr>
<tr>
<td>White-Only</td>
<td>118.230</td>
<td>77.2536</td>
<td>0.99 ± 0.00</td>
<td>0.404</td>
<td>0.002 ± 0.033</td>
<td>0.006 ± 0.009</td>
</tr>
<tr>
<td>PLW</td>
<td>787.566</td>
<td>766.569</td>
<td>0.36 ± 0.10</td>
<td>4.044</td>
<td>−0.017 ± 0.157</td>
<td>−0.002 ± 0.024</td>
</tr>
<tr>
<td>GGM</td>
<td>764.327</td>
<td>770.294</td>
<td>0.10 ± 0.11</td>
<td>0.393</td>
<td>0.003 ± 0.048</td>
<td>0.006 ± 0.014</td>
</tr>
<tr>
<td>1 phi</td>
<td>5.267</td>
<td>3.590</td>
<td>0.361</td>
<td>0.361</td>
<td>0.100 ± 0.297</td>
<td>0.239 ± 0.085</td>
</tr>
<tr>
<td>STD</td>
<td>4.404</td>
<td>3.287</td>
<td>0.350</td>
<td>0.350</td>
<td>−0.019 ± 1.337</td>
<td>0.197 ± 0.214</td>
</tr>
<tr>
<td>Bias (mm)</td>
<td>4.044</td>
<td>3.268</td>
<td>0.350</td>
<td>0.350</td>
<td>0.052 ± 0.612</td>
<td>0.201 ± 0.167</td>
</tr>
</tbody>
</table>
To further examine the properties of the time-correlated noise, we tested various noise models for each data set using HECTOR software [Bos et al., 2013], examining white noise only, random walk, flicker, autoregressive moving average, autoregressive fractionally integrated moving average, generalized Gauss-Markov (GGM) or power law and white (PLW) models. Noise model parameters and summary statistics were estimated along with a linear rate and annual plus semiannual periodic terms. We used both the Akaike information criterion [Akaike, 1973] and Bayesian information criterion [Schwarz, 1978] to identify the preferred noise model for each time series. The characteristics of the SLR series are best fit by a GGM or PLW model, in strong preference to a white noise-only model (see Table 1). Where a white noise-only model was estimated in HECTOR, our values are consistent with the time-constant annual and semiannual terms of Altamimi et al. [2016].

The uncertainty in the rate of the SLR translations, estimated with a PLW noise model over the complete time span, is a factor of 5 larger in comparison to a white noise-only model (see Table 1). That is, white noise uncertainties for X, Y, and Z rates, respectively, of ±0.03, ±0.03, and ±0.06 increase to ±0.13, ±0.17, and ±0.33 (mm/yr) when a PLW noise model is adopted. A PLW noise model was chosen instead of GGM for the remaining analysis as a conservative estimate of rate uncertainty. We examined the apparent offset around 2010 in the SLR origin Y component (Figures 1b and 1e), as described by Altamimi et al. [2016], and found it to be statistically insignificant when estimated within the noise analysis. Neither of the geophysical models shows an offset at this time. Together, this suggests that the apparent discontinuity is simply characteristic of power law time-correlated noise with spectral indices close to −1 (flicker noise) [Williams, 2003]. No other offsets were estimated for the data sets.

Neither of the network translations from the geophysical models captures the long-period variability in the SLR series particularly well. The removal of the models from the SLR series results in generally no change to the spectral index for the PLW model in the X, Y, and Z components for both MSM and R15, (see Tables 1 and 2).

### 3.3. Time-Variable Trends

We next consider the multiyear trends in the SLR translation time series. By convention, the linear rate of each SLR origin translation component is not statistically different from zero [Altamimi et al., 2016] over the full time series. However, low-frequency variability is evident in the SLR time series, particularly in the Y and Z components (Figures 1b and 1c). This signal is not present in either of the mass transport models (Figure 1, noting that the same scale is used in the left and right panels). The nonlinear signature observed in the temporal domain of the SLR Y component in Figure 1b is similarly reflected in Figure 2b where the Y component of the SLR origin series shows high power at low frequencies.

The time-variable rate within each data series is shown in Figures 4d–4f, for each of the 4 year segments discussed previously. Similarly to the annual amplitude, the largest temporal variability in the short-term rate is found in the SLR Y and Z components (Figures 4e and 4f), with a number of short-term rates significantly different to the rate determined over the full record (grey line, Figures 4d–4f). The section of the SLR X and Z components before 1997.0 are distinctly different from the long-term average, with the Z component almost a factor of 3 larger than the long-term mean in this period. Segments in the Y component have differences from the mean ranging from +0.8 mm/yr to −0.9 mm/yr, and the two segments covering 2005.0–2012.0 are statistically significant from the long-term average. R15 contains contributions from ocean mass and ice sheets mass that are indirectly affected by the GIA model used, which are not included in MSM and could explain some of the offset between the rates derived from the two models.

### 4. Discussion

Our comparison of the SLR translations with respect to the ITRF2014 origin with network translations derived from equivalently sampled geophysical models shows that it is likely that signals of nongeophysical origin, with a range of frequencies (monthly to interannual), are insufficiently accounted for in the stochastic model of the ITRF2014 origin. Altamimi et al. [2016] suggested to add annual corrections to the station positions (equations (2) and (3) in their paper) in order to bring the network origin closer to the instantaneous CM, as sensed by SLR. However, if the annual estimates are partly affected by systematic errors in SLR, it remains unclear how these errors will propagate into station positions (and satellite orbits) if the published annual and semiannual geocenter terms derived from SLR are applied.
Several studies have examined potential systematic error in SLR, in particular, the influence of the time-variable ground network distribution [Collilieux et al., 2009; Collilieux and Wöppelmann, 2011], and satellite observation geometry [Spatar et al., 2015] in order to assess uncertainty. Collilieux et al. [2009] found that the SLR network effect could affect the amplitude of the annual geocenter motion in the Z direction at approximately 1 mm, depending on the simulated observing network geometry. We found that the network effect was dominated by the geophysical models' annual signal, rather than the network geometry and account for the SLR network effect by deriving network translations from geophysical models, using only the surface deformation at those active SLR stations for each epoch.

Previous studies have explored uncertainty in the data series submitted to the previous ITRF, ITRF2008 [Altamimi et al., 2011], and found substantial nonlinear variation around the origin [Méttivier et al., 2010; Argus, 2012]. Dong et al. [2014] note an acceleration in the Z geocenter component of the ITRF2008 origin after 1998 and attribute this to terrestrial water mass redistribution, including mass loss from continental ice sheets and glaciers. We note the same feature in our analysis with a clear change in the short-term rate of the SLR Z component (Figure 4f), but note that this is not replicated by MSM, even though MSM and Dong et al. [2014] both use the GLDAS terrestrial water storage model. We note that there are differences in the glacier and ice sheet mass terms which could explain why the deviation is not present in MSM; the reason for this discrepancy requires further consideration.

The future improvement of the precision and accuracy of the ITRF origin will depend on advances in analysis and in the SLR network effect by deriving network translations from geophysical models, using only the surface deformation at those active SLR stations for each epoch.

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5. Conclusions

We assess the temporal variability of the latest SLR translations with respect to the International Terrestrial Reference Frame (ITRF2014) origin and find significant differences when compared to modeled network translations from two independent surface mass transport models. The proportion of variance explained in the SLR origin time series by geophysical models is on average less than 10% in each component. Others have evaluated the stability of the ITRF2008 origin using statistical and spectral analysis [Collilieux and Altamimi, 2013; Argus, 2012]. These analyses show that a colored noise model is more appropriate than a white noise-only model; an outcome that we find remains robust for the ITRF2014 origin. Argus [2012] demonstrated time variability in both the annual amplitude and short-term rates of geocenter motion and that the linear CM velocity uncertainties are ±0.4 mm/yr for X and Y and ±0.9 mm/yr for the Z component (95% confidence limit). Our findings confirm that a simple linear regression using a white noise-only model will poorly reflect the true uncertainty of the estimated parameters, with the uncertainty for the linear rate typically a factor of 5 smaller than estimates using a PLW noise model (see Tables 1 and 2). Our analysis of the SLR translations relative to the ITRF2014 origin suggests improvement of the CM velocity compared with those from Argus [2012] for ITRF2008. Simply scaling our rate uncertainties to 2 sigma, the PLW noise model results in a 27% improvement of the SLR Z component, reducing from ±0.9 mm/yr (95% confidence limit) [Argus, 2012] to ±0.66 mm/yr (95% confidence limit).

The future improvement of the precision and accuracy of the ITRF origin will depend on advances in analysis and in the SLR network effect by deriving network translations from geophysical models, using only the surface deformation at those active SLR stations for each epoch.

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yields an upper bound fivefold increase in rate uncertainty, compared to the white noise-only case. When using a power law and white model, the uncertainty of the SLR Z component (0.33 mm/yr; 1 sigma) is twice as large as that of the X and Y components (0.13 and 0.17 mm/yr, respectively). This represents a 27% improvement for the Z component of the results in comparison to those from Argus [2012] for ITRF2008. Over shorter time periods, the temporal variability of linear rates computed over 4 years suggests that the SLR translations with respect to the long-term ITRF2014 origin cannot be rigorously represented by a simple linear model over longer periods. For the annual signal, model-based network translations, particularly in the Z component, do not represent the variability in the annual amplitude of the SLR translations with respect to the ITRF2014 origin. This indicates that a significant component of the signal is due to other processes, including likely large systematic error.

Positioning uncertainty for geophysical applications is likely to be impacted by nonlinear geophysical signals of the kind we identify in the SLR translation time series with respect to the ITRF2014 origin and may be further impacted when noneogeophysical signals exist. Space geodetic analyses that require an instantaneous CM frame (precise orbit determination, for example) will also likely be affected given that the annual geocenter motion model used is derived from the same SLR data that are used to define the long-term origin of ITRF2014. Further improvements in SLR data analysis and network geometry are likely required to address this issue. The demonstration of other geodetic techniques to contribute to the Earth’s center of mass determination would also be of great benefit.

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References


