A Co-contextual Type Checker for Featherweight Java

Kuci, Edlira; Erdweg, Sebastian; Bračevac, Oliver; Bejleri, Andi; Mezini, Mira

DOI
10.4230/LIPIcs.ECOOP.2017.18

Publication date
2017

Document Version
Final published version

Published in
31st European Conference on Object-Oriented Programming (ECOOP 2017)

Citation (APA)

Important note
To cite this publication, please use the final published version (if applicable). Please check the document version above.

Copyright
Other than for strictly personal use, it is not permitted to download, forward or distribute the text or part of it, without the consent of the author(s) and/or copyright holder(s), unless the work is under an open content license such as Creative Commons.

Takedown policy
Please contact us and provide details if you believe this document breaches copyrights. We will remove access to the work immediately and investigate your claim.
A Co-contextual Type Checker for Featherweight Java

Edlira Kuci¹, Sebastian Erdweg², Oliver Bračevac³, Andi Bejleri⁴, and Mira Mezini⁵

¹ Technische Universität Darmstadt, Germany
² TU Delft, The Netherlands
³ Technische Universität Darmstadt, Germany
⁴ Technische Universität Darmstadt, Germany
⁵ Technische Universität Darmstadt, Germany and Lancaster University, UK

Abstract

This paper addresses compositional and incremental type checking for object-oriented programming languages. Recent work achieved incremental type checking for structurally typed functional languages through co-contextual typing rules, a constraint-based formulation that removes any context dependency for expression typings. However, that work does not cover key features of object-oriented languages: Subtype polymorphism, nominal typing, and implementation inheritance. Type checkers encode these features in the form of class tables, an additional form of typing context inhibiting incrementalization.

In the present work, we demonstrate that an appropriate co-contextual notion to class tables exists, paving the way to efficient incremental type checkers for object-oriented languages. This yields a novel formulation of Igarashi et al.’s Featherweight Java (FJ) type system, where we replace class tables by the dual concept of class table requirements and class table operations by dual operations on class table requirements. We prove the equivalence of FJ’s type system and our co-contextual formulation. Based on our formulation, we implemented an incremental FJ type checker and compared its performance against javac on a number of realistic example programs.

1998 ACM Subject Classification D.3.3 Language Constructs and Features, F.3.1 Specifying and Verifying and Reasoning about Programs, F.3.2 Semantics of Programming Languages

Keywords and phrases type checking; co-contextual; constraints; class table; Featherweight Java

Digital Object Identifier 10.4230/LIPIcs.ECOOP.2017.18

1 Introduction

Previous work [6] presented a co-contextual formulation of the PCF type system with records, parametric polymorphism, and subtyping by duality of the traditional contextual formulation. The contextual formulation is based on a typing context and operations for looking up, splitting, and extending the context. The co-contextual formulation replaces the typing context and its operations with the dual concepts of context requirements and operations for generating, merging, and satisfying requirements. This enables bottom-up type checking that starts at the leaves of an expression tree. Whenever a traditional type checker would look up variable types in the typing context, the bottom-up co-contextual type checker generates fresh type variables and generates context requirements stating that these type variables need to be bound to actual types; it merges and satisfies these requirements as it visits the syntax.
A Co-contextual Type Checker for Featherweight Java

new List().add(1).size() + new LinkedList().add(2).size();

(R₁) List.init() (R₄) LinkedList.init()
(R₂) List.add : Int → U₁ (R₅) LinkedList.add : Int → U₂
(R₃) U₁.size : () → U₃ (R₆) U₂.size : () → U₄

Figure 1 Requirements generated from co-contextually type checking the + expression.

tree upwards to the root. The co-contextual type formulation of PCF enables incremental type checking giving rise to order-of-magnitude speedups [6].

These results motivated us to investigate co-contextual formulation of the type systems for statically typed object-oriented (OO) languages, the state-of-the-art programming technology for large-scale systems. We use Featherweight Java [8] (FJ) as a representative calculus for these languages. Specifically, we consider two research questions: (a) Can we formulate an equivalent co-contextual type system for FJ by duality to the traditional formulation, and (b) if yes, how to define an incremental type checker based on it with significant speedups? Addressing these questions is an important step towards a general theory of incremental type checkers for statically typed OO languages, such as Java, C♯, or Eiffel.

We observe that the general principle of replacing the typing context and its operations with co-contextual duals carries over to the class table. The latter is propagated top-down and completely specifies the available classes in the program, e.g., member signatures and super classes. Dually, a co-contextual type checker propagates class table requirements bottom-up. This data structure specifies requirements on classes and members and accompanying operations for generating, merging, and removing these requirements.

However, defining appropriate merge and remove operations on co-contextual class table requirements poses significant challenges, as they substantially differ from the equivalent operations on context requirements. Unlike the global namespace and structural typing of PCF, FJ features context dependent member signatures (subtype polymorphism), a declared type hierarchy (nominal typing), and inherited definitions (implementation inheritance).

For an intuition of class table requirements and the specific challenges concerning their operations, consider the example in Figure 1. Type checking the operands of + yields the class table requirements R₁ to R₆. Here and throughout the paper we use metavariable U to denote unification variables as placeholders for actual types. For example, the invocation of method add on new List() yields a class table requirement R₂. The goal of co-contextual type checking is to avoid using any context information, hence we cannot look up the signature of List.add in the class table. Instead, we use a placeholder U₁ until we discover the definition of List.add later on. As consequence, we lack knowledge about the receiver type of any subsequent method call, such as size in our example. This leads to requirement R₃, which states that (yet unknown) class U₁ should exist that has a method size with no arguments and (yet unknown) return type U₃. Assuming + operates on integers, type checking the + operator later unifies U₃ and U₁ with Int, thus refining the class table requirements.

To illustrate issues with merging requirements, consider the requirements R₃ and R₆ regarding size. Due to nominal typing, the signature of this method depends on U₁ and U₂, where it is yet unknown how these classes are related to each other. It might be that U₁ and U₂ refer to the same class, which implies that these two requirements overlap and the corresponding types of size in R₃ and R₆ are unified. Alternatively, it might be the case that U₁ and U₂ are distinct classes, individually declaring a method size. Unifying the types of size from R₃ and R₆ would be wrong. Therefore, it is locally indeterminate whether a merge should unify or keep the requirements separate.
To illustrate issues with removing class requirements, consider the requirement $R_5$. Suppose that we encounter a declaration of `add` in `LinkedList`. Just removing $R_5$ is not sufficient because we do not know whether `LinkedList` overrides `add` of a yet unknown superclass $U$, or not. Again, the situation is locally indeterminate. In case of overriding, FJ requires that the signatures of overriding and overridden methods be identical. Hence, it would necessary add constraints equating the two signatures. However, it is equally possible that `LinkedList.add` overrides nothing, so that no additional constraints are necessary. If, however, `LinkedList` inherits `add` from `List` without overriding it, we need to record the inheritance relation between these two classes, in order to be able to replace $U_2$ with the actual return type of `size`.

The example illustrates that a co-contextual formulation for nominal typing with subtype polymorphism and implementation inheritance poses new research questions that the work on co-contextual PCF did not address. A key contribution of the work presented in this paper is to answer these questions. The other key contribution is an incremental type checker for FJ based on the co-contextual FJ formulation. We evaluate the initial and incremental performance of the co-contextual FJ type checker on synthesized FJ programs and realistic Java programs by comparison to javac and a context-based implementation of FJ.

To summarize, the paper makes the following contributions:

- We present a co-contextual formulation of FJ’s type system by duality to the traditional type system formulation by Igarashi et al. [8]. Our formulation replaces the class table by its dual concept of class table requirements and it replaces field/method lookup, class table duplication, and class table extension by the dual operations of requirement generation, merging, and removing. In particular, defining the semantics of merging and removing class table requirements in the presence of nominal types, OO subtype polymorphism, and implementation inheritance constitute a key contribution of this work.

- We present a method to derive co-contextual typing rules for FJ from traditional ones and provide a proof of equivalence between contextual and co-contextual FJ.

- We provide a description of type checker optimizations for co-contextual FJ with incrementalization and a performance evaluation.

2 Background and Motivation

In this section, we present the FJ typing rules from [8] and give an example to illustrate how contextual and co-contextual FJ type checkers work.

2.1 Featherweight Java: Syntax and Typing Rules

Featherweight Java [8] is a minimal core language for modeling Java’s type system. Figure 2 shows the syntax of classes, constructors, methods, expressions, and typing contexts. Metavariables $C$, $D$, and $E$ denote class names and types; $f$ denotes fields; $m$ denotes method names; `this` denotes the reference to the current object. As is customary, an overline denotes a sequence in the metalanguage. $\Gamma$ is a set of bindings from variables and `this` to types.

The type system (Figure 3) ensures that variables, field access, method invocation, constructor calls, casting, and method and class declarations are well-typed. The typing judgment for expressions has the form $\Gamma; CT \vdash e : C$, where $\Gamma$ denotes the typing context, $CT$ the class table, $e$ the expression under analysis, and $C$ the type of $e$. The typing judgment for methods has the form $C; CT \vdash M \text{ OK}$ and for classes $CT \vdash L \text{ OK}$.

In contrast to the FJ paper [8], we added some cosmetic changes to the presentation. For example, the class table $CT$ is an implicit global definition in FJ. Our presentation explicitly
18:4  A Co-contextual Type Checker for Featherweight Java

\[
\begin{align*}
L & ::= \text{class } C \text{ extends } D \{ C \overline{f}; \ K \overline{M} \} & \text{class declaration} \\
K & ::= C(C \overline{f}); \text{ constructor} \\
M & ::= C m(C \overline{x}) \{ \text{ return } e; \} & \text{method declaration} \\
e & ::= x \mid \text{ this } \mid e.f \mid e.m(\overline{x}) \mid \text{ new } C(\overline{x}) \mid (C)e & \text{expression} \\
\Gamma & ::= \emptyset \mid \Gamma; x : C \mid \Gamma; \text{ this } : C & \text{typing contexts}
\end{align*}
\]

\textbf{Figure 2} Featherweight Java syntax and typing context.

propagates CT top-down along with the typing context. Another difference to Igarashi et al. is in the rule T-New: Looking up all fields of a class returns a constructor signature, i.e., fields\((C, CT) = C.\text{ init}(\overline{D})\) instead of returning a list of fields with their corresponding types. We made this subtle change because it clearer communicates the intention of checking the constructor arguments against the declared parameter types. Later on, these changes pay off, because they enable a systematic translation of typing rules to co-contextual FJ (Sections 3 and 4) and give a strong and rigorous equivalence result for the two type systems (Section 5).

Furthermore, we explicitly include a typing rule T-Program for programs, which is implicit in Igarashi et al.'s presentation. The typing judgment for programs has the form \(\Gamma \vdash OK\): A program is well-typed if all class declarations are well-typed. The auxiliary functions addExt, addCtor, addFs, and addMs extract the supertype, constructor, field and method declarations from a class declaration into entries for the class table. Initially, the class table is empty, then it is gradually extended with information from every class declaration by using the above-mentioned auxiliary functions. This is to emphasize that we view the class table as an additional form of typing context, having its own set of extension operations. We describe the class table extension operations and their co-contextual duals formally in Section 3.

\subsection{2.2 Contextual and Co-Contextual Featherweight Java by Example}

We revisit the example from the introduction to illustrate that, in absence of context information, maintaining requirements on class members is non-trivial:

\[
\text{new List().add(1).size()} + \text{new LinkedList().add(2).size()}
\]

Here we assume the class declarations on the right-hand side: List with methods \text{add()} and \text{size()} and LinkedList inheriting from List. As before, we assume there are typing rules for numeric Int literals and the + operator over Int values. We use LList instead of LinkedList in Figure 4 for space reasons.

Figure 4 (a) depicts standard type checking with typing contexts in FJ. The type checker in FJ visits the syntax tree “down-up”, starting at the root. Its inputs (propagated downwards) are the context \(\Gamma\), class table \(CT\), and the current subexpression \(e\). Its output (propagated upwards) is the type \(C\) of the current subexpression. The output is computed according to the currently applicable typing rule, which is determined by the shape of the current subexpression. The class table used by the standard type checker contains classes List and LinkedList shown above. The type checker retrieves the signatures for the method invocations of \text{add} and \text{size} from the class table \(CT\).

To recap, while type checking constructor calls, method invocations, and field accesses the context and the class table flow top-down; types of fields/methods are looked up in the class table.
\[
\begin{align*}
T-\text{VAR} & \quad \Gamma(x) = C \quad \Gamma; CT \vdash x : C \\
T-\text{FIELD} & \quad \Gamma; CT \vdash e : C_e \quad \text{field}(f_i, C_e, CT) = C_i \\
T-\text{INVK} & \quad \Gamma; CT \vdash e : C_e \quad \Gamma; CT \vdash \pi : C \quad \text{mtype}(m, C_e, CT) = \overline{D} \rightarrow C \quad \overline{C} \triangleleft \overline{D} \\
T-\text{NEW} & \quad \Gamma; CT \vdash \pi : \overline{C} \quad \text{fields}(C, CT) = C.\text{init}(\overline{D}) \quad \overline{C} \triangleleft \overline{D} \\
T-\text{UCAST} & \quad \Gamma; CT \vdash e : D \quad D <: C \quad \Gamma; CT \vdash (C)e : C \\
T-\text{DCAST} & \quad \Gamma; CT \vdash e : D \quad C <: D \quad C \neq D \\
T-\text{SCAST} & \quad \Gamma; CT \vdash e : D \quad C \neq D \quad D \neq C \\
T-\text{METHOD} & \quad \pi : \overline{C}; \textbf{this} : C \quad \Gamma; CT \vdash e : E_0 \quad \text{extends}(C, CT) = D \quad E_0 <: C_0 \\
& \quad \text{if} \quad \text{mtype}(m, D, CT) = \overline{D} \rightarrow D_0, \text{then} \quad \overline{C} = \overline{D}; \quad C_0 = D_0 \\
& \quad C; CT \vdash C m(\overline{C} \pi)\{\text{return} \ e\} \ OK \\
T-\text{CLASS} & \quad CT \vdash \textbf{class} \ C \ extends \ D \ \{\overline{C} \ \overline{f}; \ \text{super}(\overline{g})\}; \ \textbf{this} \ \overline{f} = \overline{f} \} \quad \text{fields}(D, CT) = D.\text{init}(\overline{D}) \\
& \quad C; CT \vdash M \ OK \\
T-\text{PROGRAM} & \quad CT = \bigcup_{L' \in \overline{L}}(\text{addExt}(L') \cup \text{addCtor}(L') \cup \text{addFs}(L') \cup \text{addMs}(L')) \\
& \quad (CT \vdash L' \ OK, L' \in \overline{L}) \\
& \quad \overline{L} \ OK
\end{align*}
\]

**Figure 3** Typing rules of Featherweight Java.

Figure 4 (b) depicts type checking of the same expression in co-contextual FJ. Here, the type checker starts at the leaves of the tree with no information about the context or the class table. The expression type \( T \), the context requirements \( R \), and class table requirements \( CR \) all are outputs and only the current expression \( e \) is input to the type checker, making the type checker context-independent. At the leaves, we do not know the signature of the constructors of List and LinkedList. Therefore, we generate requirements for the constructor calls List.\text{init}() and LinkedList.\text{init}() and propagate them as class table requirements. For each method invocation of add and size in the tree, we generate requirements on the receiver type and propagate them together with the requirements of the subexpressions.

In addition to generating requirements and propagating them upwards as shown in Figure 4 (b), a co-contextual type checker also merges requirements when they have compatible receiver types. In our example, we have two requirements for method add and two requirements for method size. The requirements for method add have incompatible ground receiver types and therefore cannot be merged. The requirements for method size both have placeholder receivers and therefore cannot be merged just yet. However, for the size requirements, we can already extract a conditional constraint that must hold if the requirements become mergeable, namely \( U_2 = U_4 \text{ if } U_1 = U_3 \). This constraint ensures the
18:6 A Co-contextual Type Checker for Featherweight Java

(a) Contextual type checking propagates contexts and class tables top-down.

(b) Co-contextual type checking propagates context and class table requirements bottom-up.

Figure 4 Contextual and co-contextual type checking.

signatures of both \texttt{size} invocations are equal in case their receiver types \(U_1\) and \(U_3\) are equal. This way, we enable early error detection and incremental solving of constraints. Constraints can be solved continuously as soon as they have been generated in order to not wait for the whole program to be type checked. We discuss incremental type checking in more detail in Section 6.

After type checking the + operator, the type checker encounters the class declarations of \texttt{List} and \texttt{LinkedList}. When type checking the class header \texttt{LinkedList extends List}, we have to record the inheritance relation between the two classes because methods can be invoked by \texttt{LinkedList}, but declared in \texttt{List}. For example, if \texttt{List} is not known to be a superclass of \texttt{LinkedList} and given the declaration \texttt{List.add}, then we cannot just yet satisfy the requirement \texttt{LinkedList.add : Num \rightarrow U_3}. Therefore, we duplicate the requirement regarding \texttt{add} having \texttt{as} receiver \texttt{List}, i.e., \texttt{List.add : Num \rightarrow U_3}. By doing so, we can deduce the actual type of \(U_3\) for the given declaration of \texttt{add} in \texttt{List}. Also, requirements regarding \texttt{size} are duplicated.

In the next step, the method declaration of \texttt{size} in \texttt{List} is type checked. Hence, we consider all requirements regarding \texttt{size}, i.e., \(U_1, \texttt{size : ()} \rightarrow U_2\) and \(U_3, \texttt{size : ()} \rightarrow U_4\). The receivers of \texttt{mashitsize} in both requirements are unknown. We cannot yet satisfy these requirements because we do not know whether \(U_1\) and \(U_3\) are equal to \texttt{List}, or not. To solve this, we introduce conditions as part of the requirements, to keep track of the relations between the unknown required classes and the declared ones. By doing so, we can deduce the actual types of \(U_2\) and \(U_4\), and satisfy the requirements later, when we have more information about \(U_1\) and \(U_3\).

Next, we encounter the method declaration \texttt{add} and satisfy the corresponding requirements. After satisfying the requirements regarding \texttt{add}, the type checker can infer the actual types of \(U_1\) and \(U_3\). Therefore, we can also satisfy the requirements regarding \texttt{size}.
To summarize, during the co-contextual type checking of constructor calls, method invocations, and field accesses, the requirements flow bottom-up. Instead of looking up types of fields/methods in the class table, we introduce new class table requirements. These requirements are satisfied when the actual types of fields/methods become available.

3 Co-Contextual Structures for Featherweight Java

In this section, we present the dual structures and operations for the co-contextual formulation of FJ’s type system. Specifically, we introduce bottom-up propagated context and class table requirements, replacing top-down propagated typing contexts and class tables.

3.1 Class Variables and Constraints

For co-contextual FJ, we reuse the syntax of FJ in Figure 2, but extend the type language to class types:

- \( U, V, \ldots \) Class Variable
- \( T ::= C \mid U \) Class Type

We use constraints for refining class types, i.e., co-contextual FJ is a constraint-based type system. That is, next to class names, the type system may assign class variables, designating unknowns in constraints. We further assume that there are countably many class variables, equality of class variables is decidable and that class variables and class names are disjoint.

During bottom-up checking, we propagate sets \( S \) of constraints:

- \( S ::= T = T \mid T \neq T \mid T \prec T \mid T \nsucceq T \mid T = T \text{ if } \text{cond} \) constraint
- \( S ::= \emptyset \mid S; s \) constraint set

A constraint \( s \) either states that two class types must be equal, non-equal, in a subtype relation, non-subtype, or equal if some condition holds, which we leave underspecified for the moment.

3.2 Context Requirements

A typing context is a set of bindings from variables to types, while a context requirement is a set of bindings from variables to class variables \( U \). Below we show the operations on typing contexts and their co-contextual correspondences, reproduced from [6]. Operations on typing context are lookup, extension, and duplication; their respective requirement context duals are: generating, removing, and merging. Co-contextual FJ adopts context requirements and operations for method parameters and \textbf{this} unchanged.

<table>
<thead>
<tr>
<th>Contextual</th>
<th>Co-contextual</th>
</tr>
</thead>
<tbody>
<tr>
<td>Context syntax ( \Gamma ::= \emptyset \mid \Gamma; x:T )</td>
<td>Requirements ( R \subset x \times T ) map variables to their types</td>
</tr>
<tr>
<td>Context lookup ( \Gamma(x) = T )</td>
<td>Requirement introduction ( R = {x:U} ) with fresh unification variable ( U )</td>
</tr>
<tr>
<td>Context extension ( \Gamma; x:T )</td>
<td>Requirement satisfaction ( R - x ) if ( R(x) = T ) holds</td>
</tr>
<tr>
<td>Context duplication ( \Gamma \rightarrow \Gamma, \Gamma )</td>
<td>Requirement merging ( \text{merge}_R(R_1, R_2) = R_1</td>
</tr>
<tr>
<td>Context is empty ( \Gamma = \emptyset )</td>
<td>No unsatisfied requirements ( R \equiv \emptyset )</td>
</tr>
</tbody>
</table>
3.3 Structure of Class Tables and Class Table Requirements

In the following, we describe the dual notion of a class table, called class table requirements and their operations. We first recapitulate the structure of FJ class tables [8], then stipulate the structure of class table requirements. Figure 5 shows the syntax of both. A class table is a collection of class definition clauses $CTcls$ defining the available classes. A clause is a class name $C$ followed by either the superclass, the signature of the constructor, a field type, or a method signature of $C$’s definition.

As Figure 5 suggests, class tables and definition clauses in FJ have a counterpart in co-contextual FJ. Class tables become class table requirements $CR$, which are collections of pairs $(CReq, cond)$, where $CReq$ is a class requirement and $cond$ is its condition. Each class definition clause has a corresponding class requirement $CReq$, which is one of the following:

- A **inheritance requirement** $T . extends: T'$, i.e., class type $T$ must inherit from $T'$.
- A **constructor requirement** $T . init(T')$, i.e., class type $T$’s constructor signature must match $T'$.
- A **field requirement** $T . f : T'$, i.e., class $T$ (or one of its supertypes) must declare field $f$ with class type $T'$.
- A **method requirement** $T . m : T' \rightarrow T''$, i.e., class $T$ (or one of its supertypes) must declare method $m$ matching signature $T' \rightarrow T''$.
- An **optional method requirement** $(T . m : T' \rightarrow T'')_{opt}$, i.e., if the class type $T$ declares the method $m$, then its signature must match $T' \rightarrow T''$. While type checking method declarations, this requirement is used to ensure that method overrides in subclasses are well-defined. An optional method requirement is used as a counterpart of the conditional method lookup in rule $T\text{-Method}$ of standard FJ, i.e., if $\text{mtype}(m, D, CT) = \overline{D} \rightarrow \overline{D}_0$, then $\overline{C} = \overline{D}$; $\overline{C}_0 = \overline{D}_0$, where $D$ is the superclass of the class $C$, in which the method declaration $m$ under scrutiny is type checked, and $\overline{C}$, $\overline{C}_0$ are the parameter and returned types of $m$ as part of $C$.

A condition $cond$ is a conjunction of equality and nonequality constraints on class types. Intuitively, $(CReq, cond)$ states that if the condition $cond$ is satisfied, then the requirement

\footnote{To make the correspondence to class table requirements more obvious, we show a decomposed form of class tables. The original FJ formulation [8] groups clauses by the containing class declaration.}
### Contextual Co-contextual Correspondence

<table>
<thead>
<tr>
<th>Contextual</th>
<th>Co-contextual</th>
</tr>
</thead>
<tbody>
<tr>
<td>Field name lookup $\text{field}(f, C, CT) = C_i$</td>
<td>Class requirement for field</td>
</tr>
<tr>
<td>Fields lookup $\text{fields}(C, CT) = C.\text{init}(\overline{C})$</td>
<td>Class requirement for constructor</td>
</tr>
<tr>
<td>Method lookup $\text{mtype}(m, C, CT) = \overline{C} \rightarrow C$</td>
<td>Class requirement for method</td>
</tr>
<tr>
<td>Conditional method override</td>
<td>Optional class requirement for method</td>
</tr>
<tr>
<td>Super class lookup $\text{extends}(C, CT) = D$</td>
<td>Class requirement for super class</td>
</tr>
<tr>
<td>Class table duplication $CT \rightarrow (CT, CT)$</td>
<td>Class requirement merging</td>
</tr>
</tbody>
</table>

- **Figure 6**: Operations on class table and their co-contextual correspondence.

$C\text{Req}$ must be satisfied, too. Otherwise, we have unsolvable constraints, indicating a typing error. With conditional requirements and constraints, we address the feature of nominal typing and inheritance for co-contextual FJ. In the following, we will describe their usage.

### 3.4 Operations on Class Tables and Requirements

In this section, we describe the co-contextual dual to FJ’s class table operations as outlined in Figure 6. We first consider FJ’s lookup operations on class tables, which appear in premises of typing rules shown in Figure 3 to look up (1) fields, (2) field lists, (3) methods and (4) superclass lookup. The dual operation is to introduce a corresponding class requirement for the field, list of fields, method, or superclass.

Let us consider closely field lookup, i.e., $\text{field}(f, C, CT) = C_i$, meaning that class $C$ in the class table $CT$ has as member a field $f_i$ of type $C_i$. We translate it to the dual operation of introducing a new class requirement $(C.f_i : U, \emptyset)$. Since we do not have any information about the type of the field, we choose a fresh class variable $U$ as type of field $f_i$. At the time of introducing a new requirement, its condition is empty.

Consider the next operation $\text{fields}(C, CT)$, which looks up all field members of a class. This lookup is used in the constructor call rule $T$-$\text{NEW}$; the intention is to retrieve the constructor signature in order to type check the subtyping relation between this signature and the types of expressions as parameters of the constructor call, i.e., $\overline{C} <: \overline{D}$ (rule $T$-$\text{NEW}$). As we can observe, the field names are not needed in this rule, only their types. Hence, in contrast to the original FJ rule [8], we deduce the constructor signature from fields lookup, rather than field names and their corresponding types, i.e., $\text{fields}(C, CT) = C.\text{init}(\overline{D})$. The dual operation on class requirements is to add a new class requirement for the constructor, i.e., $(C.\text{init}(\overline{U}), \emptyset)$. Analogously, the class table operations for method signature lookup and super class lookup map to corresponding class table requirements.

Finally, standard FJ uses class table duplication to forward the class table to all parts of an FJ program, thus ensuring all parts are checked against the same context. The dual co-contextual operation, $\text{merge}_{CR}(CR_1, CR_2) = CR|S$, if all constraints in $S$ hold.
A Co-contextual Type Checker for Featherweight Java

\[
CR_m = \{(T_1,m : T_1' \rightarrow T_1, cond_1 \cup (T_1 \neq T_2)) \\
\cup (T_2,m : T_2' \rightarrow T_2, cond_2 \cup (T_1 \neq T_2)) \\
\cup (T_1,m : T_1' \rightarrow T_1', cond_1 \cup cond_2 \cup (T_1 = T_2)) \\
| (T_1,m : T_1' \rightarrow T_1', cond_1) \in CR_1 \land (T_2,m : T_2' \rightarrow T_2', cond_2) \in CR_2 \}
\]

\[
S_m = \{(T_1' = T_2' \; i f \; T_1 = T_2) \cup (T_1 = T_2' \; i f \; T_1 = T_2) \\
| (T_1,m : T_1' \rightarrow T_1', cond_1) \in CR_1 \land (T_2,m : T_2' \rightarrow T_2', cond_2) \in CR_2 \}
\]

Figure 7 Merge operation of method requirements \(CR_1\) and \(CR_2\).

class. To merge two sets of requirements, we first identify the field and method names used in both sets and then compare the classes they belong to. The result of merging two sets of class requirements \(CR_1\) and \(CR_2\) is a new set \(CR\) of class requirements and a set of constraints, which ensure compatibility between the two original sets of overlapping requirements. Non-overlapping requirements get propagated unchanged to \(CR\) whereas potentially overlapping requirements receive special treatment depending on the requirement kind.

The full merge definition appears in our technical report [10]. Figure 7 shows the merge operation for overlapping method requirements, which results in a new set of requirements \(CR_m\) and constraints \(S_m\). To compute \(CR_m\), we identify method requirements on the equally-named methods \(m\) in both sets and distinguish two cases. First, if the receivers are different \(T_1 \neq T_2\), then the requirements are not actually overlapping. We retain the two requirements unchanged, except that we remember the failed condition for future reference. Second, if the receivers are equal \(T_1 = T_2\), then the requirements are actually overlapping. We merge them into a single requirement and produce corresponding constraints in \(S_m\).

One of the key benefits of keeping track of conditions in class table requirements is that often these conditions allow us to discharge requirements early on when their conditions are unsatisfiable. In particular, in Section 6 we describe a compact representation of conditional requirements that facilitates early pruning and is paramount for good performance. However, the main reason for conditional class table requirements is their removal, which we discuss subsequently.

3.5 Class Table Construction and Requirements Removal

Our formulation of the contextual FJ type system differs in the presentation of the class table compared to the original paper [8]. Whereas Igarashi et al. assume that the class table is a pre-defined static structure, we explicitly consider its formation through a sequence of operations. The class table is initially empty and gradually extended with class table clauses \(CTcls\) for each class declaration \(L\) of a program. Dual to that, class table requirements are initially unsatisfied and gradually removed. We define an operation for adding clauses to the class table and a corresponding co-contextual dual operation on class table requirements for removing requirements. Figure 8 shows a collection of adding and removing operations for every possible kind of class table clause \(CTcls\).

In general, clauses are added to the class table starting from superclass to subclass declarations. For a given class, the class header with \texttt{extends} is added before the other
Figure 8 Constructing class table and their co-contextual correspondence.

<table>
<thead>
<tr>
<th>Contextual</th>
<th>Co-contextual</th>
</tr>
</thead>
<tbody>
<tr>
<td>Class table empty $CT = \emptyset$</td>
<td>Unsatisfied class requirements $CR$</td>
</tr>
<tr>
<td>Adding extend addExt($L, CT$)</td>
<td>Remove extend removeExt($L, CR$)</td>
</tr>
<tr>
<td>Adding constructor addCtor($L, CT$)</td>
<td>Remove constructor removeCtor($L, CR$)</td>
</tr>
<tr>
<td>Adding fields addFs($L, CT$)</td>
<td>Remove fields removeFs($L, CR$)</td>
</tr>
<tr>
<td>Adding methods addMs($L, CT$)</td>
<td>Remove methods removeMs($L, CR$)</td>
</tr>
</tbody>
</table>

clauses. Dually, we start removing requirements that correspond to clauses of a subclass, followed by those corresponding to clauses of superclass declarations. For a given class, we first remove requirements corresponding to method, fields, or constructor clauses, then those corresponding to the class header `extends` clause. Note that our sequencing still allows for mutual class dependencies. For example, the following is a valid sequence of clauses where A depends on B and vice versa:

```java
class A extends Object; class B extends Object; A.m: () → B; B.m: () → A.
```

The full definition of the addition and removal operations for all cases of clause definition appears in our technical report [10]; Figure 9 presents the definitions of adding and removing method and `extends` clauses.

Remove operations for method clauses. The function removeMs removes a list of methods by applying the function removeM to each of them. removeM removes a single method declaration defined in class $C$. To this end, removeM identifies requirements on the same method name $m$ and refines their receiver to be different from the removed declaration’s defining class. That is, the refined requirement $(T.m: \ldots, cond \cup (T \neq C))$ only requires method $m$ if the receiver $T$ is different from the defining class $C$. If the receiver $T$ is, in fact, equal to $C$, then the condition of the refined requirement is unsatisfiable and can be discharged. To ensure the required type also matches the declared type, removeM also generates conditional constraints in case $T = C$. Note that whether $T = C$ can often not be determined immediately because $T$ may be a placeholder type $U$.

We illustrate the removal of methods using the class declaration of List shown in Section 2.2. Consider the class requirement set $CR = (U_1.size(): () → U_2, \emptyset)$. Encountering the declaration of method `add` has no effect on this set because there is no requirement on `add`. However, when encountering the declaration of method `size`, we refine the set as follows:

```
removeM(List, Int.size(): {}, CR) = \{(U_1.size(): () → U_2, U_1 \neq List)\}|S
```

with a new constraint $S = \{U_2 = \text{Int} \text{ if } U_1 = \text{List}\}$. Thus, we have satisfied the requirement in $CR$ for $U_1 = \text{List}$, only leaving the requirement in case $U_1$ represents another type. In particular, if we learn at some point that $U_1$ indeed represents List, we can discharge the requirement because its condition is unsatisfiable. This is important because a program is only closed and well-typed if its requirement set is empty.

Remove operations for `extends` clauses. The function removeExt removes the class header clauses (`C. extends D`). This function, in addition to identifying the requirements regarding `extends` and following the same steps as above for removeM, duplicates all requirements for fields and methods. The duplicate introduces a requirement the same as the existing one, but
addMs($C, \overline{M}, CT) = \overline{C.m : \overline{C} \rightarrow CT}$

removeM($C, C', m(\overline{C} \pi) \{\text{return } e\}, CR) = CR'|_S$

where $CR' = \{(T.m : T \rightarrow T', \text{cond} \cup (T \neq C)) | (T.m : T \rightarrow T', \text{cond}) \in CR\}$

$\cup (CR \setminus (T.m : \overline{T} \rightarrow T', \text{cond}))$

$S = \{(T' = C' \text{ if } T = C) \cup (T' = \overline{C} \text{ if } T = C) | (T.m : T \rightarrow T', \text{cond}) \in CR\}$

removeMs($C, \overline{M}, CR) = CR'|_S$

where $CR' = \{CR_m | (C' m(\overline{C} \pi) \{\text{return } e\}) \in \overline{M} \wedge \text{removeM}(C, C', m(\overline{C} \pi) \{\text{return } e\}, CR) = CR_m|_{S_m}\}$

$S = \{S_m | (C' m(\overline{C} \pi) \{\text{return } e\}) \in \overline{M} \wedge \text{removeM}(C, C', m(\overline{C} \pi) \{\text{return } e\}, CR) = CR_m|_{S_m}\}$

addExt(class $C$ extends $D, CT) = (C \text{ extends } D) \cup CT$

removeExt(class $C$ extends $D, CR) = CR'|_S$

where $CR' = \{(T\text{.extends} : T', \text{cond} \cup (T \neq C)) | (T\text{.extends} : T', \text{cond}) \in CR\}$

$\cup \{(T.m : T \rightarrow T', \text{cond} \cup (T \neq C)) \cup (D.m : T \rightarrow T', \text{cond} \cup (T = C)) | (T.m : T \rightarrow T', \text{cond}) \in CR\}$

$\cup \{(T.m : T \rightarrow T', \text{cond}) \in CR\}$

$\cup \{(T.m : T \rightarrow T', \text{cond} \cup (T = C)) \cup (D.m : T \rightarrow T', \text{cond}) \cup (T = C)) | (T.m : T \rightarrow T', \text{cond}) \in CR\}$

$S = \{(T' = D \text{ if } T = C) | (T\text{.extends} : T', \text{cond}) \in CR\}$

\begin{itemize}
  \item Figure 9 Add and remove operations of method and extends clauses.
\end{itemize}

with a different receiver, which is the superclass $D$ that potentially declares the required fields and methods. The conditions also change. We add to the existing requirements an inequality condition ($T \neq C$), to encounter the case when the receiver $T$ is actually replaced by $C$, but it is required to have a certain field or method, which is declared in $D$, the superclass of $T$. This requirement should be discharged because we know the actual type of the required field or method, which is inherited from the given declaration in $D$. Also, we add an equality condition to the duplicate requirement $T = C$, because this requirement will be discharged when we encounter the actual declarations of fields or methods in the superclass.

We illustrate the removal of extends using the class declaration LinkedList extends List. Consider the requirement set $CR = \{U_3.\text{size} : () \rightarrow U_4, \emptyset\}$. We encounter the declaration for LinkedList and the requirement set changes as follows:

removeExt(class LinkedList extends List, CR) =

\[\{(U_3.\text{size} : () \rightarrow U_4, U_3 \neq \text{LinkedList}), (\text{List}.\text{size} : () \rightarrow U_4, U_3 = \text{LinkedList})\}\] |_S,

where $S = \emptyset$. $S$ is empty, because there are no requirements on extends. If we learn at some point that $U_3 = \text{LinkedList}$, then the requirement $(U_3.\text{size} : () \rightarrow U_4, U_3 \neq \text{LinkedList})$
is discharged because its condition is unsatisfiable. Also, if we learn that size is declared in List, then \( \text{List}.\text{size} : () \to U_4, U_3 = \text{LinkedList} \) is discharged applying removeM, as shown above, and \( U_4 \) can be replaced by its actual type.

**Usage and necessity of conditions.** As shown throughout this section, conditions play an important role to enable merging and removal of requirements over nominal receiver types and to support inheritance. Because of nominal typing, field and method lookup depends on the name of the defining context and we do not know the actual type of the receiver class when encountering a field or method reference. Thus, it is impossible to deduce their types until more information is known. Moreover, if a class is required to have fields/methods, which are actually declared in a superclass of the required class, then we need to deduce their actual type/signature and meanwhile fulfill the respective requirements. For example, considering the requirement \( U_3.\text{size} : () \to U_4 \), if \( U_3 = \text{LinkedList} \), LinkedList extends List, and size is declared in List, then we have to deduce the actual type of \( U_4 \) and satisfy this requirement. To overcome these obstacles we need additional structure to maintain the relations between the required classes and the declared ones, and also to reason about the partial fulfillment of requirements. Conditions come to place as the needed structure to maintain these relations and indicate the fulfillment of requirements.

4 **Co-Contextual Featherweight Java Typing Rules**

In this section we derive co-contextual FJ's typing rules systematically from FJ's typing rules. The main idea is to transform the rules into a form that eliminates any context dependencies that require top-down propagation of information.

Concretely, context and class table requirements (Section 3) in output positions to the right replace typing contexts and class tables in input positions to the left. Additionally, co-contextual FJ propagates constraint sets \( S \) in output positions. Note that the program typing judgment does not change, because programs are closed, requiring neither typing context nor class table inputs. Correspondingly, neither context nor class table requirements need to be propagated as outputs.

Figure 10 shows the co-contextual FJ typing rules (the reader may want to compare against contextual FJ in Figure 3). In what follows, we will discuss the rules for each kind of judgment.

4.1 **Expression Typing**

Typing rule \( \text{TC-Var} \) is dual to the standard variable lookup rule \( \text{T-Var} \). It marks a distinct occurrence of \( x \) (or the self reference \( \text{this} \)) by assigning a fresh class variable \( U \). Furthermore, it introduces a new context requirement \( \{ x : U \} \), as the dual operation of context lookup for variables \( x \) (\( \Gamma(x) = C \)) in \( \text{T-Var} \). Since the latter does not access the class table, dually, \( \text{TC-Var} \) outputs empty class table requirements.

Typing rule \( \text{TC-Field} \) is dual to \( \text{T-Field} \) for field accesses. The latter requires a field name lookup (field), which, dually, translates to a new class requirement for the field \( f_i \), i.e., \( (T_e.f_i : U, \emptyset) \) (cf. Section 3). Here, \( T_e \) is the class type of the receiver \( e \). \( U \) is a fresh class variable, marking a distinct occurrence of field name \( f_i \), which is the class type of the entire expression. Furthermore, we merge the new field requirement with the class table requirements \( CR_e \) propagated from \( e \). The result of merging is a new set of requirements \( CR \) and a new set of constraints \( S_{cr} \). Just as the context \( \Gamma \) is passed into the subexpression \( e \) in \( \text{T-Field} \), we propagate the context requirements for \( e \) for the entire expression. Finally,
Figure 10 A co-contextual formulation of the type system of Featherweight Java.

we propagate both the constraints $S_e$ for $e$ and the merge constraints $S_f$ as the resulting output constraints.

Typing rule $\text{TC-Inv}$ is dual to $\text{T-Invk}$ for method invocations. Similarly to field access, the dual of method lookup is introducing a requirement for the method $m$ and merge it
with the requirements from the premises. Again, we choose fresh class variables for the method signature \( U \rightarrow U' \), marking a distinct occurrence of \( m \). We type check the list \( \bar{r} \) of parameters, adding a subtype constraint \( \bar{T} <: \bar{U} \), corresponding to the subtype check in \( \text{T-Invk} \). Finally, we merge all context and class table requirements propagated from the receiver \( e \) and the parameters \( \bar{r} \), and all the constraints.

Typing rule \( \text{TC-New} \) is dual to \( \text{T-New} \) for object creation. We add a new class requirement \( C.\text{init}(U) \) for the constructor of class \( C \), corresponding to the \textit{fields} operation in FJ. We cannot look up the fields of \( C \) in the class table, therefore we assign fresh class variables \( \bar{U} \) for the constructor signature. We add the subtyping constraint \( \bar{T} <: \bar{U} \) for the parameters, analogous to the subtype check in \( \text{T-New} \). As in the other rules, we propagate a collective merge of the propagated requirement structures/constraints from the subexpressions with the newly created requirements/constraints.

Typing rules for casts, i.e., \( \text{TC-UCast}, \text{TC-DCast} \) and \( \text{TC-SCast} \) are straightforward adaptations of their contextual counterparts following the same principles. These three type rules do overlap. We do not distinguish them in the formalization, but to have an algorithmic formulation, we implement different node names for each of them. That is, typing rules for casts are syntactically distinguished.

### 4.2 Method Typing

The typing rule \( \text{TC-Method} \) is dual to \( \text{T-Method} \) for checking method declarations. For checking the method body, the contextual version extends the empty typing context with entries for the method parameters \( \bar{r} \) and the self-reference \texttt{this}, which is implicitly in scope. Dually, we remove the requirements on the parameters and self-reference in \( R_e \) propagated from the method body. Corresponding to extending an empty context, the removal should leave no remaining requirements on the method body. Furthermore, the equality constraints \( S_x \) ensure that the annotated class types for the parameters agree with the class types in \( R_e \).

This corresponds to binding the parameters to the annotated classes in a typing context. Analogously, the constraints \( S_c \) deal with the self-reference. For the latter, we need to know the associated class type, which in the absence of the class table is at this point unknown. Hence, we assign a fresh class variable \( U_c \) for the yet to be determined class containing the method declaration. The contextual rule \( \text{T-Method} \) further checks if the method declaration correctly overrides another method declaration in the superclass, that is, if it exists in the superclass must have the same type. We choose another fresh class variable \( U_d \) for the yet to be determined superclass of \( U_c \) and add appropriate supertype and optional method override requirements. We assign to the optional method requirement \( U_d.m \) the type of \( m \) declared in \( U_c \). If later is known that there exists a declaration for \( m \) in the actual type of \( U_d \), the optional requirement is considered and equality constraints are generated. These constraints ensure that the required type of \( m \) in the optional requirement is the same as the provided type of \( m \) in the actual superclass of \( U_c \). Otherwise this optional method requirement is invalidated and not considered. By doing so, we enable the feature of subtype polymorphism for co-contextual FJ. Finally, we add the subtype constraint ensuring that the method body’s type is conforming to the annotated return type.

\[ \text{Note that a parameter } x \text{ occurs in the method body if and only if there is a requirement for } x \text{ in } R_e \text{ (i.e., } x \in \text{dom}(R_e)) \text{, which is due to the bottom-up propagation. The same holds for the self-reference } \texttt{this}. \]
4.3 Class Typing

Typing rule \(\text{TC-Class}\) is used for checking class declarations. A declaration of a given class \(C\) provides definite information on the identity of its superclass \(D\), constructor, fields, and methods signatures. Dual to the fields lookup for superclass \(D\) in \(\text{TC-Class}\), we add the constructor requirement \(D.\text{init}(\overline{D})\). We merge this requirement with all requirements generated from type checking \(C\)'s method declarations \(\overline{M}\). Recall that typing of method \(m\) yields a distinct class variable \(U\) for the enclosing class type, because we type check each method declaration independently. Therefore, we add the constraints \(\{U = C\}\), effectively completing the method declarations with their enclosing class \(C\).

4.4 Program Typing

Type rule \(\text{TC-Program}\) checks a list of class declarations \(\overline{L}\). Class declarations of all classes provide a definite information on the identity of their super classes, constructor, fields, methods signatures. Dual to adding clauses in the class table by constructing it, we remove requirements with respect to the provided information from the declarations. Hence, dually to class table being fully extended with clauses from all class declarations, requirements are empty. The result of removing different clauses is a new set of requirement and a set of constraints. Hence, we use notation \(\sqcup\) to express the union of the returned tuples (requirements and constraints), i.e., \(CR|_S \sqcup CR'|_{S'} = CR \cup CR'|_{S \cup S'}\). After applying remove to the set of requirements, the set should be empty at this point. A class requirement is discharged from the set, either when performing remove operation (Section 3), or when it is satisfied (all conditions hold).

As shown, we can systematically derive co-contextual typing rules for Featherweight Java through duality.

5 Typing Equivalence

In this section, we prove the typing equivalence of expressions, methods, classes, and programs between FJ and co-contextual FJ. That is, (1) we want to convey that an expression, method, class and program is type checked in FJ if and only if it is type checked in co-contextual FJ, and (2) that there is a correspondence relation between typing constructs for each typing judgment.

We use \(\sigma\) to represent substitution, which is a set of bindings from class variables to class types \(\{U \mapsto C\}\). \(\text{projExt}(CT)\) is a function that given a class table \(CT\) returns the immediate subclass relation \(\Sigma\) of classes in \(CT\). That is, \(\Sigma := \{(C_1, C_2) \mid C_1 \text{ extends } C_2 \in CT\}\). Given a set of constraints \(S\) and a relation between class types \(\Sigma\), where \(\text{projExt}(CT) = \Sigma\), then the solution to that set of constraints is a substitution, i.e., \(\text{solve}(S, \Sigma) = \sigma\). Also we assume that every element of the class table, i.e., super types, constructors, fields and methods types are class type, namely ground types. Ground types are types that cannot be substituted.

Initially, we prove equivalence for expressions. Let us first delineate the correspondence relation. Correspondence states that a) the types of expressions are the same in both formulations, b) provided variables in context are more than required ones in context requirements and c) provided class members are more than required ones. Intuitively, an expression to be well-typed in co-contextual FJ should have all requirements satisfied. Context requirements are satisfied when for all required variables, we find the corresponding bindings in context. Class table requirements are satisfied, when for all valid requirements, i.e., all
conditions of a requirement hold, we can find a corresponding declaration in a class of the same type as the required one, or in its superclasses. The relation between the class table and class requirements is formally defined in our technical report [10].

**Definition 1 (Correspondence relation for expressions).** Given judgments $\Gamma; CT \vdash e : C$, $e : T | S | R | CR$, and $\text{solve}(\Sigma, S) = \sigma$, where $\text{projExt}(CT) = \Sigma$. The correspondence relation between $\Gamma$ and $R$, $CT$ and $CR$, written $(C, \Gamma, CT) \vdash \sigma(T, R, CR)$, is defined as:

(a) $C = \sigma(T)$
(b) $\Gamma \supseteq \sigma(R)$
(c) $CT$ satisfies $\sigma(CR)$

We stipulate two different theorems to state both directions of equivalence for expressions.

**Theorem 2 (Equivalence of expressions: $\Rightarrow$).** Given $e$, $C$, $\Gamma$, $CT$, if $\Gamma; CT \vdash e : C$, then there exists $T$, $S$, $R$, $CR$, $\Sigma$, $\sigma$, where $\text{projExt}(CT) = \Sigma$ and $\text{solve}(\Sigma, S) = \sigma$, such that $e : T | S | R | CR$ holds, $\sigma$ is a ground solution and $(C, \Gamma, CT) \vdash \sigma(T, R, CR)$ holds.

**Theorem 3 (Equivalence of expressions: $\Leftarrow$).** Given $e$, $T$, $S$, $R$, $CR$, $\Sigma$, if $e : T | S | R | CR$, $\text{solve}(\Sigma, S) = \sigma$, and $\sigma$ is a ground solution, then there exists $C$, $\Gamma$, $CT$, such that $\Gamma; CT \vdash e : C$, $(C, \Gamma, CT) \vdash \sigma(T, R, CR)$ and $\text{projExt}(CT) = \Sigma$.

Theorems 2 and 3 are proved by induction on the typing judgment of expressions. The most challenging aspect consists in proving the relation between the class table and class requirements. In Theorem 2, the class table is given and the requirements are a collective merge of the propagated requirement from the subexpressions with the newly created requirements. In Theorem 3, the class table is not given, therefore we construct it through the information retrieved from ground class requirements. We ensure class table correctness and completeness with respect to the ground requirements. First, we ensure that the class table we construct is correct, i.e., types of extends, fields, and methods clauses we add in the class table are equal to the types of the same extends, fields, and methods if they already exist in the class table. Second, we ensure that the class table we construct is complete, i.e., the constructed class table satisfies all given requirements.

Next, we present the theorem of equivalence for methods. The difference from expressions is that there is no context, therefore no relation between context and context requirements is required. Instead, the fresh class variable introduced in co-contextual FJ as a placeholder for the actual class, where the method under scrutiny is type checked in, after substitution should be the same as the class where the method is type checked in FJ.

**Theorem 4 (Equivalence of methods: $\Rightarrow$).**

Given $m$, $C$, $CT$, if $C; CT \vdash C_0 \text{m}(\overline{C} \ x) \{\text{return } e\}$

OK, then there exists $S$, $T$, $CR$, $\Sigma$, $\sigma$, where $\text{projExt}(CT) = \Sigma$ and $\text{solve}(\Sigma, S) = \sigma$, such that

$C_0 \text{m}(\overline{C} \ x) \{\text{return } e_0\}$ OK $| S | T | CR$ holds, $\sigma$ is a ground solution and $(C, CT) \triangleright_m \sigma(T, CR)$ holds.

**Theorem 5 (Equivalence of methods: $\Leftarrow$).**

Given $m$, $S$, $CR$, $\Sigma$, if $C_0 \text{m}(\overline{C} \ x) \{\text{return } e_0\}$

OK $| S | T | CR$, $\text{solve}(\Sigma, S) = \sigma$, and $\sigma$ is a ground solution, then there exists $C$, $CT$, such that $C; CT \vdash C_0 \text{m}(\overline{C} \ x) \{\text{return } e\}$ OK holds, $(C, CT) \triangleright_m \sigma(T, CR)$ and $\text{projExt}(CT) = \Sigma$.

Theorems 5 and 6 are proved by induction on the typing judgment. The difficulty increases in proving equivalence for methods because we have to consider the optional requirement,
as introduced in the previous sections. It requires a different strategy to prove the relation between the class table and optional requirements; we accomplish the proof by using case distinction. We have a detailed proof for method declaration, and also how this affects class table construction, and we prove a correct and complete construction of it.

Lastly, we present the theorem of equivalence for classes and programs.

▶ Theorem 6 (Equivalence of classes: ⇒). Given \( C, CT \), if \( CT \vdash \text{class} C \text{ extends } D \{ \overline{C} \overline{J}; K \overline{M} \} \overset{OK}{\rightarrow}, \) then there exists \( S, CR, \Sigma, \sigma \), where \( \text{projExt}(CT) = \Sigma \) and \( \text{solve}(\Sigma, S) = \sigma \), such that \( \text{class} C \text{ extends } D \{ \overline{C} \overline{J}; K \overline{M} \} \overset{OK}{\rightarrow} S \vdash CR \) holds, \( \sigma \) is a ground solution and \( (CT) \triangleright_c \sigma(CR) \) holds.

▶ Theorem 7 (Equivalence of classes: ⇐). Given \( C, CR, \Sigma, \) if \( \text{class} C \text{ extends } D \{ \overline{C} \overline{J}; K \overline{M} \} \overset{OK}{\rightarrow} S \vdash CR \), \( \text{solve}(\Sigma, S) = \sigma \), where \( \sigma \) is a ground solution, then there exists \( CT \), such that \( CT \vdash \text{class} C \text{ extends } D \{ \overline{C} \overline{J}; K \overline{M} \} \overset{OK}{\rightarrow} \) holds, \( (CT) \triangleright_c \sigma(CR) \) holds and \( \text{projExt}(CT) = \Sigma \).

Theorems 8 and 9 are proved by induction on the typing judgment. Class declaration requires to prove only the relation between the class table and class table requirements since there is no context.

Typing rule for programs does not have as inputs context and class table, therefore there is no relation between context, class table and requirements. The equivalence theorem describes that a program in FJ and co-contextual FJ is well-typed.

▶ Theorem 8 (Equivalence for programs: ⇒). Given \( L, \) if \( L \overset{OK}{\rightarrow} \) then there exists \( S, \Sigma, \sigma \), where \( \text{projExt}(L) = \Sigma \) and \( \text{solve}(\Sigma, S) = \sigma \), such that \( L \overset{OK}{\rightarrow} S \) holds and \( \sigma \) is a ground solution.

▶ Theorem 9 (Equivalence for programs: ⇐). Given \( L, \) if \( L \overset{OK}{\rightarrow} S \), \( \text{solve}(\Sigma, S) = \sigma \), where \( \text{projExt}(L) = \Sigma \), and \( \sigma \) is a ground solution, then \( L \overset{OK}{\rightarrow} \) holds.

Theorems 10 and 11 are proved by induction on the typing judgment. In here, we prove that a class table containing all clauses provided from the given class declarations is dual to empty class table requirements in the inductive step.

We refer to our technical report [10] for omitted definitions, lemmas, and proofs.

6 Efficient Incremental FJ Type Checking

The co-contextual FJ model from Section 3 and 4 was designed such that it closely resembles the formulation of the original FJ type system, where all differences are motivated by dually replacing contextual operations with co-contextual ones. As such, this model served as a good basis for the equivalence proof from the previous section. However, to obtain a type checker implementation for co-contextual FJ that is amenable to efficient incrementalization, we have to employ a number of behavior-preserving optimizations. In the present section, we describe these optimization and the resulting incremental type checker implementation for co-contextual FJ. The source code is available online at https://github.com/seba--/incremental.

Condition normalization. In our formal model from Section 3 and 4, we represent context requirements as a set of conditional class requirements \( CR \subseteq Creq \times \text{cond} \). Throughout type checking, we add new class requirements using function merge, but we only discharge class requirements in rule TC-Program at the very end of type checking. Since merge generates
$3 \times m \times n$ conditional requirements for inputs with $m$ and $n$ requirements respectively, requirements quickly become intractable even for small programs.

The first optimization we conduct is to eagerly normalize conditions of class requirements. Instead of representing conditions as a list of type equations and inequations, we map receiver types to the following condition representation (shown as Scala code):

```scala
case class Condition(notGround: Set[CName], notVar: Set[UCName],
                      sameVar: Set[UCName], sameGroundAlternatives: Set[CName]).
```

A condition is true if the receiver type is different from all ground types (CName) and unification variables (UCName) in notGround and notVar, if the receiver type is equal to all unification variables in sameVar, and if sameGroundAlternatives is either empty or the receiver type occurs in it. That is, if sameGroundAlternatives is non-empty, then it stores a set of alternative ground types, one of which the receiver type must be equal to.

When adding an equation or inequation to the condition over a receiver type, we check whether the condition becomes unsatisfiable. For example, when equating the receiver type to the ground type $C$ and notGround.contains($C$), we mark the resulting condition to be unsatisfiable. Recognizing unsatisfiable conditions has the immediate benefit of allowing us to discard the corresponding class requirements right away. Unsatisfiable conditions occur quite frequently because merge generates both equations and inequations for all receiver types that occur in the two merged requirement sets.

If a condition is not unsatisfiable, we normalize it such that the following assertions are satisfied: (i) the receiver type does not occur in any of the sets, (ii) sameGroundAlternatives.isEmpty || notGround.isEmpty, and (iii) notVar.intersect(sameVar).isEmpty. Since normalized conditions are more compact, this optimization saves memory and time required for memory management. Moreover, it makes it easy to identify irrefutable conditions, which is the case exactly when all four sets are empty, meaning that there are no further requisites on the receiver type. Such knowledge is useful when merge generates conditional constraints, because irrefutable conditions can be ignored. Finally, condition normalization is a prerequisite for the subsequent optimization.

**In-depth merging of conditional class requirements.** In the work on co-contextual PCF [6], the number of requirements of an expression was bound by the number of free variables that occur in that expression. To this end, the merge operation used for co-contextual PCF identifies subexpression requirements on the same free variable and merges them into a single requirement. For example, the expression $x + x$ has only one requirement $\{x : U_1\} | \{U_1 = U_2\}$, even though the two subexpressions propagate two requirements $\{x : U_1\}$ and $\{x : U_2\}$, respectively. Note that $U_1 = U_3$ because of the use of this in both subexpressions, but $U_2 = U_4$ because of the in-depth merge.

Unfortunately, the merge operation of co-contextual FJ given in Section 3.2 does not enjoy this property. Instead of merging requirements, it merely collects them and updates their conditions. A more in-depth merge of requirements is possible whenever two code fragments require the same member from the same receiver type. For example, the expression `this.x + this.x` needs only one requirement $\{U_1, x() : U_2\} | \{U_1 = U_3, U_2 = U_4\}$, even though the two subexpressions propagate two requirements $\{U_1, x() : U_2\}$ and $\{U_3, x() : U_4\}$, respectively. Note that $U_1 = U_3$ because of the use of this in both subexpressions, but $U_2 = U_4$ because of the in-depth merge.

However, conditions complicate the in-depth merging of class requirements: We may only merge two requirements if we can also merge their conditions. That is, for conditional requirements $(creq_1, cond_1)$ and $(creq_2, cond_2)$ with the same receiver type, the merged requirement
must have the condition $cond_1 \lor cond_2$. In general, we cannot express $cond_1 \lor cond_2$ using our Condition representation from above because all fields except `sameGroundAlternatives` represent conjunctive prerequisites, whereas `sameGroundAlternatives` represents disjunctive prerequisites. Therefore, we only support in-depth merging when the conditions are identical up to `sameGroundAlternatives` and we use the union operator to combine their `sameGroundAlternatives` fields.

This optimization may seem a bit overly specific to certain use cases, but it turns out it is generally applicable. The reason is that function `removeExt` creates requirements of the form $(D.f : T', cond \cup (T = C_i))$ transitively for all subclasses $C_i$ of $D$ where no class between $C_i$ and $D$ defines field $f$. Our optimization combines these requirements into a single one, roughly of the form $(D.f : T', cond \cup (T = \bigvee_i C_i))$. Basically, this requirement concisely states that $D$ must provide a field $f$ of type $T'$ if the original receiver type $T$ corresponds to any of the subclasses $C_i$ of $D$.

**Incrementalization and continuous constraint solving.** We adopt the general incrementalization strategy from co-contextual PCF [6]: Initially, type check the full program bottom-up and memoize the typing output for each node (including class requirements and constraint system). Then, upon a change to the program, recheck each node from the change to the root of the program, reusing the memoized results from unchanged subtrees. This way, incremental type checking asymptotically requires only $\log n$ steps for a program with $n$ nodes.

In our formal model of co-contextual FJ, we collect constraints during type checking and solve them at the end to yield a substitution for the unification variables. As was discussed by Erdweg et al. for co-contextual PCF [6], this strategy is inadequate for incremental type checking, because we would memoize unsolved constraints and thus only obtain an incremental constraint generator, but even a small change would entail that all constraints had to be solved from scratch. In our implementation, we follow Erdweg et al.’s strategy of continuously solving constraints as soon as they are generated, memoizing the resulting partial constraint solutions. In particular, equality constraints that result from merge and remove operations can be solved immediately to yield a substitution, while subtype constraints often have to be deferred until more information about the inheritance hierarchy is available. In the context of FJ with its nominal types, continuous constraint solving has the added benefit of enabling additional requirement merging, for example, because two method requirements share the same receiver type after substitution.

**Tree balancing.** Even with continuous constraint solving, co-contextual FJ as defined in Section 4 still does not yield satisfactory incremental performance. The reason is that the syntax tree is deformed due to the root node, which consists of a sequence of all class declarations in the program. Thus, the root node has a branching factor only bound by the number of classes in the program, whereas the rest of the tree has a relative small branching factor bound by the number of arguments to a method. Since incremental type checking recomputes each step from the changed node to the root node, the type checker would have to repeat discharging class requirements at the root node after every code change, which would seriously impair incremental performance.

To counter this effect, we apply tree balancing as our final optimization. Specifically, instead of storing the class declarations as a sequence in the root node, we allow sequences of class declarations to occur as inner nodes of the syntax tree:

\[
L ::= T \mid \text{class } C \text{ extends } D \{C \vec{f}; \ K \vec{M}\}
\]
This allows us to layout a program’s class declarations structurally as in
(((C_1 \ C_2) (C_4 C_5)) (C_6 C_7)), thus reducing the costs for rechecking any path from
a changed node to the root node. As part of this optimization, to satisfy requirements of
classes that occur in different tree nodes such as C_1 and C_6, we also need to propagate class
facts such as actual method signatures upwards. As consequence, we can now link classes in
any order without changing the type checking result.

We have implemented an incremental co-contextual FJ type checker in Scala using the
optimizations described here. In the following section, we present our run-time performance
evaluation.

7 Performance Evaluation

We have benchmarked the initial and incremental run-time performance of co-contextual
FJ implementation. However, this evaluation makes no claim to be complete, but rather is
intended to confirm the feasibility and potential of co-contextual FJ for incremental type
checking.

7.1 Evaluation on synthesized FJ programs

Input data. We synthesized FJ programs with 40 root classes that inherit from Object.
Each root class starts a binary tree in the inheritance hierarchy of height 5. Thus, each
root-class hierarchy contains 31 FJ class declarations. In total, our synthesized programs
have 31 \times 40 + 3 = 1243 class declarations, since we always require classes for natural numbers
Nat, Zero, and Succ.

Each class has at least a field of type Nat and each class has a single method that takes
no arguments and returns a Nat. We generated the method body according to one of three
schemes:

- AccumSuper: The method adds the field’s value of this class to the result of calling the
  method of the super class.
- AccumPrev: Each class in root hierarchy k \geq 1 has an additional field that has the type
  of the class at the same position in the previous root hierarchy k - 1. The method adds
  the field’s value of this class to the result of calling the method of the class at the same
  position in the previous root hierarchy k - 1, using the additional field as receiver object.
- AccumPrevSuper: Combines the other two schemes; the method adds all three numbers.

We also varied the names used for the generated fields and methods:

- Unique: Every name is unique.
- Mirrored: Root hierarchies use the same names in the same classes, but names within a
  single root hierarchy are unique.
- Override: Root hierarchies use different names, but all classes within a single root
  hierarchy use the same names for the same members.
- Mir+Over: Combines the previous two schemes, that is, all classes in all root hierarchies
  use the same names for the same members.

For evaluating the incremental performance, we invalidate the memoized results for the
three Nat classes. This is a critical case because all other classes depend on the Nat classes
and a change is traditionally hard to incrementalize.
Table 1 Performance measurement results with $k = 40$ root classes in Milliseconds. Numbers in parentheses indicate speedup relative to (javac/contextual) base lines.

<table>
<thead>
<tr>
<th></th>
<th>javac / contextual</th>
<th>co-contextual init</th>
<th>co-contextual inc</th>
</tr>
</thead>
<tbody>
<tr>
<td>unique</td>
<td>70.00 / 93.99</td>
<td>3117.73 (0.02x / 0.03x)</td>
<td>23.44 (2.9x / 4x)</td>
</tr>
<tr>
<td>mirrored</td>
<td>68.03 / 88.73</td>
<td>1860.18 (0.04x / 0.05x)</td>
<td>15.17 (4.5x / 6x)</td>
</tr>
<tr>
<td>override</td>
<td>73.18 / 107.83</td>
<td>513.44 (0.14x / 0.21x)</td>
<td>16.92 (4.3x / 6x)</td>
</tr>
<tr>
<td>mir+over</td>
<td>72.64 / 132.09</td>
<td>481.07 (0.15x / 0.27x)</td>
<td>16.60 (4.4x / 8x)</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th></th>
<th>javac / contextual</th>
<th>co-contextual init</th>
<th>co-contextual inc</th>
</tr>
</thead>
<tbody>
<tr>
<td>unique</td>
<td>82.16 / 87.66</td>
<td>3402.28 (0.02x / 0.02x)</td>
<td>23.43 (3.5x / 4x)</td>
</tr>
<tr>
<td>mirrored</td>
<td>81.19 / 84.94</td>
<td>2136.42 (0.04x / 0.04x)</td>
<td>15.46 (5.3x / 5x)</td>
</tr>
<tr>
<td>override</td>
<td>81.51 / 120.60</td>
<td>840.14 (0.09x / 0.14x)</td>
<td>17.37 (4.7x / 7x)</td>
</tr>
<tr>
<td>mir+over</td>
<td>79.71 / 120.46</td>
<td>816.16 (0.09x / 0.15x)</td>
<td>16.61 (4.8x / 7x)</td>
</tr>
</tbody>
</table>

Experimental setup. First, we measured the wall-clock time for the initial check of each program using our co-contextual FJ implementation. Second, we measured the wall-clock time for the incremental reanalysis after invalidating the memoized results of the three Nat classes. Third, we measured the wall-clock time of checking the synthesized programs on javac and on a straightforward implementation of contextual FJ for comparison. Contextual FJ is the standard FJ described in Section 2, that uses contexts and class tables during type checking. Our implementation of contextual FJ is up to 2-times slower than javac, because it is not production quality. We used ScalaMeter\(^3\) to take care of JIT warm-up, garbage-collection noise, etc. All measurements were conducted on a 3.1GHz duo-core MacBook Pro with 16GB memory running the Java HotSpot 64-Bit Server VM build 25.111-b14 with 4GB maximum heap space. We confirmed that confidence intervals were small.

Results. We show the measurement results in table 1. All numbers are in milliseconds. We also show the speedups of initial and incremental run of co-contextual type checking relative to both javac and contextual type checking.

As this data shows, the initial performance of co-contextual FJ is subpar: The initial type check takes up to 68-times and 61-times longer than using javac and a standard contextual checker respectively.

However, co-contextual FJ consistently yields high speedups for incremental checks. In fact, it only takes between 3 and 21 code changes until co-contextual type checking is faster overall. In an interactive code editing session where every keystroke or word could be considered a code change, incremental co-contextual type checking will quickly break even and outperform a contextual type checker or javac.

The reason that the initial run of co-contextual FJ induces such high slowdowns is because the occurrence of class requirements is far removed from the occurrence of the

\(^3\) [https://scalameter.github.io/](https://scalameter.github.io/)
corresponding class facts. This is true for the Nat classes that we merge with the synthesized code at the top-most node as well as for dependencies from one root hierarchy to another one. Therefore, the type checker has to propagate and merge class requirements for a long time until finally discovering class facts that discharge them. We conducted an informal exploratory experiment that revealed that the performance of the initial run can be greatly reduced by bringing requirements and corresponding class facts closer together. On the other hand, incremental performance is best when the changed code occurs as close to the root node as possible, such that a change entails fewer rechecks. In future work, when scaling our approach to full Java, we will explore different layouts for class declarations (e.g., following the inheritance hierarchy or the package structure) and for reshuffling the layout of class declarations during incremental type checking in order to keep frequently changing classes as close to the root as possible.

7.2 Evaluation on real Java program

Input data. We conduct an evaluation for our co-contextual type checking on realistic FJ programs. We wrote about 500 SLOCs in Java, implementing purely functional data structures for binary search trees and red black trees. In the Java code, we only used features supported by FJ and mechanically translated the Java code to FJ. For evaluating the incremental performance, we invalidate the memoized results for the three Nat classes as in the experiment above.

Experimental setup. Same as above.

Results. We show the measurements in milliseconds for the 500 lines of Java code.

<table>
<thead>
<tr>
<th></th>
<th>javac / contextual</th>
<th>co-contextual init</th>
<th>co-contextual inc</th>
</tr>
</thead>
<tbody>
<tr>
<td>14.88 / 3.74</td>
<td>48.07 (0.31x / 0.08x)</td>
<td>9.41 (1.6x / 0.39x)</td>
<td></td>
</tr>
</tbody>
</table>

Our own non-incremental contextual type checker is surprisingly fast compared to javac, and not even our incremental co-contextual checker gets close to that performance. When comparing javac and the co-contextual type checker, we observe that the initial performance of the co-contextual type checker improved compared to the previous experiment, whereas the incremental performance degraded. While the exact cause of this effect is unclear, one explanation might be that the small input size in this experiment reduces the relative performance loss of the initial co-contextual check, but also reduces the relative performance gain of the incremental co-contextual check.

8 Related work

The work presented in this paper on co-contextual type checking for OO programming languages, specifically for Featherweight Java, is inspired by the work on co-contextual type checking for PCF [6]. OO languages and FJ impose features like nominal typing, subtype polymorphism, and inheritance that are not covered in the work for co-contextual PCF [6]. In particular, here we developed a solution for merging and removing requirements in presence of nominal typing.

Introducing type variables as placeholders for the actual types of variables, classes, fields, methods is a known technique in type inference [11, 12]. The difference is that we introduce a fresh class variable for each occurrence of a method \( m \) or fields in different branches of the
A Co-contextual Type Checker for Featherweight Java

typing derivation. Since fresh class variables are generated independently, no coordination is
required while moving up the derivation tree, ensuring context and class table independence.
Type inference uses the context to coordinate type checking of \( \nu \) in different branches,
by using the same type variable. In contrast to type inference where context and class
table are available, we remove them (no actual context and class table). Hence, in type
inference inheritance relation between classes and members of the classes are given, whereas
in co-contextual FJ we establish these relations through requirements. That is, classes are
required to have certain members with unknown types and unknown inheritance relation,
dictated from the surrounding program.
Also, in contrast to bidirectional type checking [4, 5] that uses two sets of typing rules one for
inference and one for checking, we use one set of co-contextual type rules, and the direction of
type checking is all oriented bottom-up; types and requirements flow up. As in type inference,
bidirectional type checking uses context to look up variables. Whereas co-contextual FJ
has no context or class table, it uses requirements as a structure to record the required
information on fields, methods, such that it enables resolving class variables of the required
fields, methods to their actual types.

Co-contextual formulation of type rules for FJ is related to the work on principal
typing [9, 17], and especially to principal typing for Java-like languages [2]. A principal
typing [2] of each fragment (e.g., modules, packages, or classes) is associated with a set of
type constraints on classes, which represents all other possible typings and can be used to
check compatibility in all possible contexts. That is, principle typing finds the strongest
type of a source fragment in the weakest context. This is used for type inference and
separate compilation in FJ. They can deduce exact type constraints using a type inference
algorithm. We generalize this and do not only infer requirements on classes but also on method
parameters and the current class. Moreover, we developed a duality relation between the
class table and class requirements that enables the systematic development of co-contextual
type systems for OO languages beyond FJ.

Related to our co-contextual FJ is the formulations used in the context of compositional
compilation [1] (continuation of the work on principal typing [2]) and the compositional
explanation of type errors [3]. This type system [1] partially eliminate the class table,
only inside a fragment, and does not eliminate the context. Hence, type checking of
parameters and \textit{this} is coordinated and subexpressions are coupled through dependencies on
the usage of context. In our work, we eliminate both class table (not only partially) and
context, therefore all dependencies are removed. By doing so we can enable compositional
compilation for individual methods. To resolve the type constraints on classes, compositional
compilation [2] needs a linker in addition to an inference algorithm (to deduce exact type
constraints), whereas, we use a constraint system and requirements. We use duality to derive
a co-contextual type system for FJ and we also ensure that both formulations are equivalent
(5). That is, we ensure that an expression, method, class, or program is well-typed in FJ if
and only if it is well-typed in co-contextual FJ, and that all requirements are fulfilled. In
contrast, compositional compilation rules do not check whether the inferred collection of
constraints on classes is satisfiable; they actually allow to derive judgments for any fragment,
even for those that are not statically correct.

Refactoring for generalization using type constraints [16, 15] is a technique Tip et al. used
to manipulate types and class hierarchies to enable refactoring. That work uses variable
type constraints as placeholders for changeable declarations. They use the constraints to
restrict when a refactoring can be performed. Tip et al. are interested to find a way to
represent the actual class hierarchy and to use constraints to have a safe refactoring and a
well-typed program after refactoring. The constraint system used by Tip et al. is specialized to refactoring, because different variable constraints and solving techniques are needed. In contrast, in our work, we use class variables as placeholders for the actual type of required extends, constructors, fields, and methods of a class, in the lack of the class table. We want to gradually learn the information about the class hierarchy. We are interested in the type checking technique and how to co-contextualize it and use constraints for type refinement.

Adapton [7] is a programming language where the runtime system traces memory reads and writes and selectively replays dependent computations when a memory change occurs. In principle, this can be used to define an “incremental” contextual type checker. However, due to the top-down threading of the context, most of the computation will be sensitive to context changes and will have to be replayed, thus yielding unsatisfactory incremental performance. Given a co-contextual formulation as developed in our paper, it might be possible to define an efficient implementation in Adapton.

The works on smart/est recompilation [13, 14] have a different purpose from ours, namely to achieve separate compilation they need algorithms for the inference and also the linking phase specific to SML. In contrast, we use duality as a guiding principle to enable the translation from FJ to co-contextual FJ. This technique allows us to do perform a systematic (but yet not mechanical) translation from a given type system to the co-contextual one. Our type system facilitates incremental type checking because we decouple the dependencies between subexpressions and the smallest unit of compilation is any node in the syntax tree. Moreover, we have investigated optimizations for facilitating the early solving of requirements and constraints.

9 Conclusion and Future Work

In this paper, we presented a co-contextual type system for FJ by transforming the typing rules in the traditional formulation into a form that replaces top-down propagated contexts and class tables with bottom-up propagated context and class table requirements. We used duality as a technique to derive co-contextual FJ’s typing rules from FJ’s typing rules. To make the correspondence between class table and requirements, we presented class tables that are gradually extended with information from the class declarations, and how to map operations on contexts and class tables to their dual operations on context and class table requirements. To cover the OO features of nominal typing, subtype polymorphism, and implementation inheritance, co-contextual FJ uses conditional requirements, inequality conditions, and conditional constraints. Also, it changes the set of requirements by adding requirements with the different receiver from the ones defined by the surrounding program, in the process of merging and removing requirements as the type checker moves upwards and discovers class declarations. We proved the typing equivalence of expressions, methods, classes, and programs between FJ and co-contextual FJ.

The co-contextual formulation of FJ typing rules enables incremental type checking because it removes dependencies between subexpressions. We implemented an incremental co-contextual FJ type checker. Also, we evaluated its performance on synthesized programs up to 1243 FJ classes and 500 SLOCs of java programs.

There are several interesting directions for future work. In short term, we want to explore parallel co-contextual type checking for FJ. A next step would be to develop a co-contextual type system for full Java. Another interesting direction is to investigate co-contextual formulation for gradual type systems.
References


