A two-stage numerical analysis approach for the assessment of the settlement response of the pre-damaged historic Hoca Pasha Mosque

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Abstract

The current paper presents a case study of the settlement response of the historic Hoca Pasha Mosque that involves uncertainties arising from the complex excavation activities, soil properties, building materials and geometry and the presence of pre-existing cracks in the mosque’s walls. The objective is to demonstrate the added value of a two-stage numerical analysis approach for the assessment of the settlement response of the building. The first stage comprises analyses of the structural behaviour using the monitored settlements for each wall. The second stage examines the behaviour of the complete building as a whole. The effects of soil-structure interaction and the pre-existing cracks are considered through discrete interface elements. It is shown that executed simulations can reasonably reproduce the overall settlement response, resulting stresses and the pre-existing crack activities. The parametric analyses in the second stage also produce generalizable results, of use beyond the specific case. Namely, as the soil/structure stiffness ratio increases the settlement-induced vulnerability increases. Including soil-structure interaction in the analyses reduces tensile strains due to differential settlements. Including pre-existing cracks reduces tensile strains in the vicinity of the cracks but results in an increase of stresses in neighbouring sections.

Key words: Settlement, masonry, damage, interface, soil, historic structure, monitoring, tunnelling
1. Introduction

Large excavation works such as for tunnels, underground stations and access shafts can result in significant amount of ground movements. The main reasons are deformations of the excavation support structure, alternation in the stress state in the soil depending on the soil removal and changes in groundwater pressure and drainage conditions (Boscardin, 1980). Additionally, the excavation size, construction technique and the details of supporting system are influential on the magnitude of the resultant ground movements (Son, 2003). Differential vertical settlements resulted from one or more of these sources are more critical than the uniform settlements and can damage nearby buildings by acting on their foundations. In response, the buildings resist with their overall stiffness. Eventually, the building response becomes a function of the interaction between soil and building.

Well-documented case studies in which different types of excavation, soil and building conditions are examined offer a great resource to understand this complicated interaction problem. A number of case studies representing various circumstances from different countries have been published (Burland et al., 2011; Finno et al., 2002; Bryson and Kotheimer, 2011; Korff et al., 2012; Amorosi et al., 2014; Fu et al., 2014; Pujades et al., 2015). In many studies (Burd et al., 2000; Pickhaver et al., 2010; Losacco et al., 2014; Giardina et al., 2015; Fargnoli et al., 2015), finite element simulations are used with different levels of sophistication of the geometrical and material modelling. In some numerical studies (Giardina et al., 2015; Son and Cording, 2011), the effect of initial building damage is also considered. However, due to lack of detailed information and other uncertainties regarding excavations, foundations, soil properties and structures, a series of assumptions and simplifications are required to simulate the actual case, which are difficult to be verified.

The current paper also presents a typical case study in which several uncertainties are shown along with the considered assumptions and simplifications. Table 1 characterizes the
present case with regard to excavation and construction works, soil, building deformation, building structure and pre-existing damages. It indicates the complexity and the availability of (monitoring) data for each aspect. Typical for this case study is that the initial damage is relatively well known; the building has clearly localized cracks, which have been monitored during the excavation works. By contrast, the excavation history is relatively complicated.

The originality is to simulate and assess the settlement response of the pre-damaged historic Hoca Pasha Mosque using a two-stage numerical analysis approach. According to this, firstly the structural model with and without pre-existing cracks is verified in a way that each façade wall is loaded separately using the measured settlements and taking into account flange affects (stiffness contribution) of other connecting walls. This stage to a large extent reduces modelling uncertainties. In the second stage, the effects of other parameters, i.e. the building stiffness, bedding stiffness and combined settlement field due to sequential excavation works are investigated. This naturally increases the modelling uncertainties, but it more closely resembles the practice of predicting settlement responses. Although the mentioned stages are not dependent directly on each other, the staging approach helps to verify the building model. Besides an examination of the specific case, more generic results are obtained through parametric analyses performed in the second stage.

**Table 1:** Characterizing the Hoca Pasha Mosque case study in terms of its geotechnical and structural complexity and the availability of (monitoring) data

<table>
<thead>
<tr>
<th>Aspect</th>
<th>Complexity level</th>
<th>Data availability level</th>
</tr>
</thead>
<tbody>
<tr>
<td>Excavations activities</td>
<td>High</td>
<td>Detailed (through the continuous monitoring data and reports regarding tunnel and shaft construction and supporting)</td>
</tr>
<tr>
<td>Soil structure</td>
<td>Moderate</td>
<td>Standard (through the reports derived from the basic in-situ soil tests)</td>
</tr>
<tr>
<td>Building deformation (building settlement and crack progress)</td>
<td>Moderate</td>
<td>Detailed (through the continuous settlement and crack monitoring data)</td>
</tr>
<tr>
<td>Building structure (geometry and material properties)</td>
<td>Low</td>
<td>Standard (through the in-situ drawings, previous expertise and publications on similar historic structures in the region)</td>
</tr>
<tr>
<td>Existing damages (crack locations and initial crack severity)</td>
<td>Moderate</td>
<td>Detailed (through the conditional building survey)</td>
</tr>
</tbody>
</table>
2. Description of the mosque and the neighbouring excavation works

A comprehensive railway transportation project, namely Marmaray, was implemented in Turkey between 2006 and 2013. As part of this project, intensive tunnel and shaft excavations were carried out in the most historic parts of Istanbul.

In the Hoca Pasha district, 135 buildings were inspected in total. Fifty eight out of 135 buildings were considered to be of moderate or high risk. These buildings were re-investigated more precisely in the detailed assessment stage. Furthermore, during the subsequent stages of the tunnel and shaft construction, evaluations were revised for some of these buildings according to increasing displacements, developing damages and the state of excavation. The Hoca Pasha Mosque as a listed historic structure was one of these buildings affected by the shaft and tunnel excavations of the Sirkeci Station in the Hoca Pasha district.

The Hoca Pasha Mosque was rebuilt in 1868 replacing the previous one destroyed by a fire (Sefer and Ahunbay, 2015). As seen in as-is drawings shown in Fig. 1a, the main structural system of the mosque relies on plastered 900 mm thick load bearing masonry walls made of solid bricks and mortar joints. An outbuilding with a separate reinforced concrete frame system was built next to the main building (Fig. 1a). The mosque has large arched windows (w×h: 1840×3860 mm) in all of the façades and doors in the northwest (NW) and northeast (NE) façades (Figs. 1b, c and d). An internal wall of almost half of the storey height divides the narthex and prayer hall. The mosque is actually a one-storey building, but there is a mezzanine floor inside. The mezzanine floor, that is constructed with steel and timber joists, and the roof are both supported by slender steel columns, situated inside the mosque, and the external masonry walls. The overall wall height is 8.25 m from the wall bottom to the eave.

During the examinations, any particular foundation system was not observed except for the main walls extending approximately 1 m downwards into the ground as common as in the
masonry buildings constructed in the same era. On the other hand, it is assumed that the single footings are present under the internal steel columns.

![Diagram of the ground floor elevation of the Hoca Pasha mosque and section views](image)

**Fig. 1:** (a) As-is drawing of the ground floor elevation of the Hoca Pasha mosque and (b,c,d) section views (dimensions in cm) (Akgun, D., 2016)

The location of the mosque was considered as critical due to closeness of intensive excavation works carried out during the construction of the Sirkeci underground station. The location of the mosque and nearby excavations with excavation advancement directions are illustrated in Fig. 2a. Monitoring results revealed that the mosque was affected to a varying extent by the indicated elliptic ventilation shaft (WVS), the pilot tunnel (NPLT) in the north platform tunnel (NPF) and the north and south ventilation chambers (NPFV and SPFV, respectively). It was observed that other excavations, namely the south platform tunnel excavation (SPF), the enlargements in north & south platform tunnels (NPF and SPF, respectively), the centre walkway tunnel excavation (CE), the short connection excavations (CNVs) between NPF and SPF, and the upwardly inclined south entrance tunnel excavation...
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(ISH) had no or less impact on the settlement response (Monthly Monitoring Reports, 2008-2013) (Figs. 2a and 3).

The WVS excavation wall approximates the southeast (SE) façade at 10m. The shaft diameter is 26.4 m on the long axis and 22.8 m on the short axis. The entire shaft depth is 58 m. The first 21 m of the shaft excavation (the upper shaft) was constructed using a secant pile wall technique. For this purpose, grouted and reinforced concrete piles with 900 mm diameter were consecutively cast on the perimeter of the elliptic shaft. Then, their tips were capped with a rigid reinforced concrete ring beam (b×h: 1000×1500 mm). As the excavation proceeds, piles were connected circumferentially by reinforced concrete ring beams (b×h: 1000×1000 mm) cast at every 1500 mm. The ring beams significantly increase the radial rigidity of the circular shaft. The remaining 37 m of the excavation (the lower shaft) was carried out in the bedrock as a stepwise open face excavation, supported by a thick wall consisting of wire meshed shotcrete and HEB 200/100 steel profiles, fixed via rock bolts. No internal cross strutting was used at any stage of the shaft excavation, not to block the equipment access through the shaft (Method Statements for Excavation and Support Works, 2008).

The excavations of the tunnels (NPF, SPF, hereinafter referred to together as PFs, and CE) and the ventilation chambers (NPFV and SPFV, hereinafter referred to together as PFVs) were carried out using the New Austrian Tunnelling Method (NATM), approximately 50 m beneath the ground surface. The PFVs have the largest cross-section with 17 m diameter among all tunnels excavated for the Sirkeci Station. The length of the PFVs is 35 m. While the NPFV partly under-passes the mosque at a skewed angle, the centre line of the SPFV is at a 40 m in plan distance from the closest corner of the mosque (Figs. 2a and 3). In order to increase the face stability and limit deformations, tunnel cross-sections larger than 50 m² (as the PFs and PFVs) were divided into sub-sections (Fig. 2b). Then, each sub-section was
excavated sequentially starting from the pilot tunnel sub-section (respectively succeeded by the excavation of the top heading, the medium heading, the bench cut and the invert). The NPLT, which became quite influential on the mosque settlements, was actually a sub-section excavation of the NPF having a 27 m² cross-sectional area (Method Statements for Excavation and Support Works, 2008).

Table 2 presents starting and completion dates of the neighbouring excavations. Observations regarding the influence of these excavations on the mosque behaviour are listed in the last column. Before the tunnel and ventilation chamber excavations started, the WVS excavation had been completed on 31 July 2008. After taking down the excavation machines through the WVS, the pilot tunnelling works in the PFs (SPLT and NPLT, respectively) started from the inside of the WVS. After following a curvilinear route, they proceeded eastwards, moving away from the WVS and accordingly from the mosque (Fig. 2a). The sequentially enlargement excavations were then started for SPLT and NPLT excluding the curvilinear sections near to the mosque. Afterwards, the pilot tunnel excavation backward into
the SPFV commenced and it was followed by the enlargement excavations in this section.

Finally, the pilot tunnel and enlargement excavations in the NPFV were completely carried out. The difference in timing of the excavation of the WVS, NPLT and NPFV excavations particularly offers an opportunity to investigate the accumulating effects on the mosque.

Table 2. Starting and completion dates of neighbouring excavations

<table>
<thead>
<tr>
<th>Excavation name (by sequence)</th>
<th>Starting date</th>
<th>Completion date</th>
<th>Observed influence on the mosque</th>
</tr>
</thead>
<tbody>
<tr>
<td>WVS</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Secant piled wall installation + Upper shaft excv. (21 m) + archaeological surveys</td>
<td>February 2006</td>
<td>February 2008</td>
<td>Negligible impact. Settlements up to max. 1.5 mm at the southeast façade</td>
</tr>
<tr>
<td>Lower shaft excavation (37 m)</td>
<td>February 2008</td>
<td>July 2008</td>
<td>Influential from start to the end</td>
</tr>
<tr>
<td>SPF (SPLT and other sub-section enlargements)</td>
<td>November 2008</td>
<td>June 2010</td>
<td>No influence, neither from pilot nor from enlargement excavations</td>
</tr>
<tr>
<td>NPF (NPLT and other sub-section enlargements)</td>
<td>December 2008</td>
<td>August 2010</td>
<td>Substantial influence, especially from the curvilinear part of the pilot excavation</td>
</tr>
<tr>
<td>SPFV</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Pilot</td>
<td>January 2010</td>
<td>February 2010</td>
<td>The pilot tunnel excavation was not influential</td>
</tr>
<tr>
<td>Sub-section enlargements</td>
<td>March 2010</td>
<td>July 2010</td>
<td>The enlargements were influential</td>
</tr>
<tr>
<td>NPFV</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>NPFV pilot</td>
<td>April 2010</td>
<td>July 2010</td>
<td>Substantial influence for all excavation stages</td>
</tr>
<tr>
<td>Top heading</td>
<td>August 2010</td>
<td>October 2010</td>
<td></td>
</tr>
<tr>
<td>Medium</td>
<td>October 2010</td>
<td>December 2010</td>
<td></td>
</tr>
<tr>
<td>Bench &amp; Invert</td>
<td>December 2010</td>
<td>January 2011</td>
<td></td>
</tr>
</tbody>
</table>

3. Local site condition

Borehole results revealed that the underlying geological structure in the vicinity of the mosque consists of three main layers (Geological Report, 2008; Pressuremeter Test Results, 2009). For the A-A section, indicated in Fig. 2a, the obtained soil profile is shown in Fig. 3. The first 15 m from the ground surface is man-made fill, consisting of sand, gravel and clay (I). Measurements made in surrounding wells (in 2013) showed that the ground water table is also around 15 m beneath the surface. The second layer (II), which is not thicker than 10 m, is composed of clayey silty sand with shell fragments. The third layer (III) is identified as a
greywacke mass, comprised of mudstone, sandstone and claystone, which are the components of the Trakya Formation. The sections shown with IV are identified as diabase.

The mechanical properties of the main geological layers are listed in Table 3. In this table, \( E_s \), \( v \), \( y_s \), \( c \) and \( \varphi \) show the Young’s modulus, Poisson’s ratio, volumetric weight, cohesion and angle of internal friction, respectively. Note that these are the values reported in the borehole test reports (Pressuremeter Test Results, 2009).

**Table 3: Reported mechanical properties of the geological layers (Geological Report, 2008; Pressuremeter Test Results, 2009)**

<table>
<thead>
<tr>
<th>Soil Layer</th>
<th>Depth (m)</th>
<th>( E_s ) (MPa)</th>
<th>( v )</th>
<th>( y_s ) (kN/m(^3))</th>
<th>( c ) (kN/m(^2))</th>
<th>( \varphi ) (degree)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Man-made fill (I)</td>
<td>0-15</td>
<td>33.0</td>
<td>0.30</td>
<td>19.0</td>
<td>0.00</td>
<td>30.0</td>
</tr>
<tr>
<td>Clayey silty sand (II)</td>
<td>10-15</td>
<td>56.0</td>
<td>0.30</td>
<td>19.0</td>
<td>0.00</td>
<td>34.0</td>
</tr>
<tr>
<td>Greywacke (III)</td>
<td>15 to deeper</td>
<td>150</td>
<td>0.35</td>
<td>21.0</td>
<td>200</td>
<td>30.0</td>
</tr>
</tbody>
</table>

**Fig. 3:** Sectional view of the excavation site and geological sections (A-A section in Fig. 2a) (modified from Method Statements for Excavation and Support Works, 2008).
4. Monitoring results and observed response

An intensive monitoring program was performed, starting from 2008 to the end of 2013. Settlements of the mosque were measured via levelling instruments by reading the vertical displacements of the monitoring bolts (SB monitoring points in Fig. 2a) attached to the external walls. Because of the absence of an effective foundation system to inhibit or reduce the ground movements which will be transferred to the walls and by means of the placement of the monitoring bolts to the bottom of the walls, just few centimeters away from the ground surface, any significant modification in the settlement readings would not be expected. Free-field ground settlements could not be measured effectively due to building congestion and traffic in the region. Instead, estimated free-field settlements are used in the analyses to be explained in the following sections.

The settlement time history taken from SB monitoring points are shown in Fig. 4. Excavation and construction activities which are influential on the settlement response of the mosque are also marked in this figure. Note that the settlements that occurred during the secant piled wall installation and the upper WVS excavation (i.e. the cut and cover excavation of the first 21 m) are not included in this figure. However, the monitoring reports (Monthly Monitoring Reports, 2008-2013) show that the settlements at that stage were negligible (≤ 1.5 mm).

As expected, settlement readouts measured on the southeast (SE) (where SB14, 17 and 18 were attached) and southwest (SW) (where SB8 and 19 were attached) façades which were relatively closer to the WVS, NPLT and NPFV excavations have been higher than the other readouts. After the completion of the WVS excavation, the rate of measured settlements of the
mosque decreased, until the pilot tunnel excavations SPLT and NPLT started. Sudden increases in the slopes of the settlement versus time curves point out that the NPLT excavation, specifically the curvilinear section, has become quite influential. Between February 2009 and April 2010, an increase presumably due to CE pilot tunnel excavation and enlargement excavations in the PFs was observed. From April 2010 onwards, the settlements significantly increased again. This time, the reason was the pilot tunnel and enlargement excavations in the PFVs. It should be particularly highlighted that the pilot tunnel and the enlargement excavations in the NPFV played a major role in this increase. In order to limit the settlements at that stage, two ground stabilizations and a following uplifting application were carried out. The first ground stabilization attempt was a cement injection procedure performed horizontally from the inside of the WVS towards the mosque. In addition to cement injection, horizontal steel rods were driven into the soil in order to compact the ground under the mosque. The second attempt was aiming at both ground stabilization and uplifting the severely settled parts of the mosque. For this purpose, vertical steel rods, 7 m long and 36 mm in diameter, were driven into the soil with an inclined angle at every 40 cm around the main external masonry walls. After performing a primer polyurethane (PU) injection, uplifting was performed through a secondary and deeper PU injection. Consequently, an upward movement (up to 3 mm) around SB13, 14 and 19 was obtained. The effect of uplifting can be seen in the settlement time history of SB13 in Fig.4 between September and November 2010. All of the excavation works in SPFV and NPFV tunnels were finalized towards January 2011.
4.1 Conditional survey prior to excavations

A conditional survey conducted before the commencement of the excavations revealed the presence of pre-existing localized cracks (C1, C2, C3-1, C3-2, C5, C6 and C10) in all of the façades (see Fig 5) (Detail Survey Report, 2008). These cracks all began at the door and window arches, either at the vertices or closer to the bottom of the arches. They have propagated upwards to the eaves almost vertically. The cracks were also visible from the inside of the mosque. While C1 and C2 above the arched door of the NE façade were the widest, C3-2 and C10 above the arched windows in the NW and SE façades were the narrowest cracks. The observed initial width of these cracks varied from 5 to 10 mm. The locations of the pre-existing localized cracks in the ground plan are also given in Fig. 5. As is, the building was classified as moderately damaged by the inspection team considering its “prior to all excavations” and estimated post condition.
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4.2 Settlement response during the construction and excavation activities

The mosque’s response was regularly inspected and reported as the construction and excavation works progress (ITU Evaluation Reports, 2008-2011). At the visual inspection dated 21 January 2009, slight widening of the mentioned pre-existing cracks due to the WVS and curvilinear NPLT excavation were observed. Increases in crack widths were recorded from 12 February 2009 onwards. Two different methods were adopted to measure the crack openings and closures throughout the excavations. Until 23 June 2010, digital callipers were used to measure the crack widths. As of June 2010, the frequency of crack measurements was increased with regard to increasing settlements due to the NPFV excavations. A separation between the main building and the outbuilding was also observed. Considering the continuing NPFV excavations, from 23 June 2010 onwards, more precise scale type crack meters were bonded and used to measure the crack widths. Although a few new cracks formed around the localized pre-existing cracks during the NPFV excavations, their widths remained relatively insignificant (none of them exceeded 0.9 mm until the end of the excavations).

Fig. 6 shows the variation of the widths (crack activity) of the major pre-existing localized cracks. Although a trend cannot be given for the initial data obtained by the digital
callipers for the period before 23 June 2010, the final digital calliper readouts are added to the data obtained by scale type crack meters. No measurements for crack C3-2 were carried out.

![Graph showing crack opening (mm) over time](image)

**Fig. 6: Opening and closures of the pre-existing localized cracks**

Fig. 6 shows that crack C3-1 widens and closes significantly during the NPFV excavations. As the mosque settlements slow down towards March 2011, a closing is observed for this crack. Another increase in the activities of C1 and C2 is noted during the top heading and medium sub-section excavations of NPFV. The C5 and C6 cracks seem to be influenced least by the NPFV excavations. However, an increase in their widths is observed as of June 2011 possibly due to the CNV excavations. Crack C10 shows minor variation throughout the excavations.

### 4.3 Evaluation of the Mosque’s response based on the conventional deformation measures

Monitored settlement response of each external masonry wall is examined by the authors using conventional deformation measures, namely angular distortion, deflection ratio and rigid rotation. For this purpose, the monitored wall settlement profiles are provided in Fig. 7 considering seven key dates i.e. after the completion of the WVS excavation (15 September 2008), after the completion of the curvilinear NPLT excavation (24 March 2009), before the
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NPFV excavations (18 March 2010), after the completion of the NPFV pilot tunnel excavation (29 July 2010), after the completion of the entire NPFV excavations (3 January 2011) and before and after the CNV excavations (21 July 2011 and 1 March 2012). As seen, while the SE façade experiences sagging (a convex settlement profile), the others experience hogging (a concave settlement profile) throughout the excavations.

**Fig. 7:** Monitored settlements along the main masonry walls

Based on the wall settlements at these considered dates, the maximum angular distortion ($\beta_{max}$), the deflection ratio ($\Delta/L$) and the rigid rotation ($\omega$) values of the façade walls are calculated (Figs. 8a, b and c, respectively). $\beta_{max}$ is the largest angular distortion value ($\beta$) calculated as the rotation of the straight line connecting two adjacent monitoring points relative to their tilt (Boscardin, 1980). $\Delta/L$ is the ratio of relative deflection between two monitoring points to the distance between them (Burland and Wroth, 1974). $\omega$ is the rigid rotation of the façade wall defined by the settlement readouts of two outmost monitoring points. Calculation of these measures are schematically explained in Fig. 8d. Three internationally accepted empirical limit values $\beta_{max} = 0.0005 \ (1/2000)$ (Meyerhof, 1982), $\Delta/L =0.0003 \ (1/3300)$ (Polshin and Tokar, 1957) and $\omega = 0.002 \ (1/500)$ (Rankin, 1988) are also
indicated in Figs. 8a, b and c. The first two values show the cracking limit of unreinforced load-bearing masonry walls in hogging. Note that the $\Delta/L = 0.0003$ value is obtained by interpolating the linear wall length to wall height ratio ($L/H$) versus $\Delta/L$ relationship of Polshin and Tokar (1957). For the derivation of $\Delta/L = 0.0003$, $L/H$ is taken as 3. Note that the cracking limits for sagging would be higher (i.e. more tolerant). $\omega = 0.002$ suggests the limit between negligible and slight damage.

![Graphs](image)

**Fig. 8:** Calculated wall distortions: (a) angular distortion, (b) deflection ratio and (c) rigid rotations

The $\beta_{max}$ versus time and $\Delta/L$ versus time graphs in Figs. 8a and 8b show that the wall distortions due to WVS (according to values dated 15 September 2008) and curvilinear NPLT (according to values dated on 24 March 2009) excavations are lower than the proposed limit
values. Enlargement excavations in CE and SPFV result in an increase in $\beta_{\text{max}}$ and $\Delta/L$ values of the NE and NW walls (see the variation between 24 March 2009 and 18 March 2010). The pilot tunnel excavation in NPFV became very influential between April 2010 and July 2010. In this period, a sharp increase in the distortion values of the most of the walls is observed. Until the completion of the NPFV excavations in January 2011, the wall distortions continue increasing with the exception of the NE wall. In the last two periods (3 January - 21 July 2011 and 21 July 2011 - 1 March 2012), the NE and NW walls experience both increases and decreases in their distortions. Conversely, the distortions of the SW wall monotonically increases in these two periods. The distortions of the SE wall are relatively small. On the other hand, while the NE wall experiences the highest rigid rotation, the NW wall has the lowest value (Fig. 8c). The calculated maximum rigid rotation is 0.0028 (1/345) for the NE wall and slightly exceeds the limit proposed by Rankin. From 3 January 2011 onwards, rigid rotation values almost level off. At the end of the PFV excavations (January 2011), considerably different rigid rotations are experienced by the parallel NE and SW walls. Presumably, this situation might have resulted in additional shear forces in the connecting SE and NW walls and at the corner connections.

Note that the crack activities given in Fig. 6 are in general agreement with the wall distortions given in Fig. 8. For instance, the lowest activity in the C10 crack is in line with the lowest distortions experienced by the SE wall and the variations of the width of crack C3-1 are in line with the increases and decreases in the distortions of the NW wall. However, a direct comparison between crack activities (openings and closings) and variations of calculated wall distortions may not always be straightforward due to:

- Used crack measurement system: The crack width measurements are carried out at only one single location on the crack line, which is selected where the initial crack
width is the largest. This kind of a measurement method may easily overlook the detailed crack activities (openings and closings) that can vary along the crack line.

- Distortion calculation method: The pre-existing cracks are local features within the entire wall and their openings and closings partly depend on local mechanisms. On the contrary, the conventional evaluation technique (Fig. 8) based on the variations of two different distortion measures (angular distortion and deflection ratio) is not expected to predict such detailed and local mechanisms. Distortion measures are basically calculated to obtain a global idea regarding the settlement response of the wall. Therefore, they are mostly related to the overall response of the wall rather than a localized crack.

- The settlement variation between monitoring points is assumed linear. In reality, this is not perfect linear.

- 3D effects: There might also be out of plane bending behaviour due to three dimensional effect of ground movements and specifications of the structural load-bearing system that will eventually cause partial crack openings or closings. (Such a numerical observation will be presented in the Section 5)

5. Proposed Two-Stage Numerical Assessment Approach

The response of the Hoca Pasha Mosque to the complicated spatial ground settlements is examined by 3D finite element modelling (DIANA v10.1, 2016). For this purpose, a two-stage numerical analysis approach is used. In the first stage (in section 5.1), the adequacy of the building model with and without pre-existing cracks is primarily verified by using monitored wall settlements. In this way, the issue of setting a realistic soil-structure interaction is temporarily put off. In the second stage, verified building model is analysed using estimated free-field ground movements considering soil-structure interaction.
The geometry of the used building model is shown in Fig. 9a. Recalling that the walls have a thickness of 900 mm and diaphragm actions of the roof is not relevant for the type of loading, the mezzanine floor, the roof, the internal columns and the minaret are not included in this model since their contribution to the overall stiffness is considered as negligible. These sections might have minor damage due to differential settlements. Since this damage will be less critical, the investigation of the response of these sections is out of focus of the current study. The masonry walls are modelled using solid tetrahedron (3 sides, 4 nodes) elements (TE12L). Meshed element size is 250 mm in all dimensions. Bricks and mortar joints are not considered separately in the model and masonry is represented homogenously using linear elastic material properties (the continuum model described previously by Lourenco, 1996) (Table 4). Due to the historical character of the mosque, no destructive test on the masonry could be performed to determine the actual mechanical properties. Instead, three different Young’s modulus ($E_{m1}$, $E_{m2}$ and $E_{m3}$) are adopted. $E_{m1}$ and $E_{m2}$ (350 and 1000 MPa, respectively) are assumed to cover the range of representative values of these typical load bearing masonry walls, constructed in the same era with similar techniques and materials (Ispir and Ilki, 2013). The higher $E_{m3}$ (10000 MPa) is included to distinguish the effect of Young’s modulus (Table 4).

The localized and already open pre-existing cracks are simulated with vertically aligned linear elastic discrete interfaces. The interface elements are triangular elements (T18IF) which are inserted between two planes in a 3D configuration. They have 3 opposite nodes on each side of the interface and each node has 3 translation degrees of freedom in $x$, $y$ and $z$ axes. In order to reveal the effect of localized cracks, two extreme conditions are considered: cracks with very low interface stiffness (almost zero) and excluding the crack interfaces from the model (no cracks). For the former, interface stiffness values in the normal direction $k_{czi}$ are calculated theoretically using Eq. (1). That is, the interface stiffness is set as
the equivalent stiffness of an fictitious masonry tie of length \( L_f \). The very low interface (almost open) stiffness is obtained by considering \( L_f \), arbitrarily, as \( 10^{10} \) mm. The crack interface stiffness in the tangential \( x \) and \( y \) directions (\( k_{cxi} \) and \( k_{cyi} \), respectively) is taken as relatively small, although not extremely small, (\( E_{mi} \times 10^3 \) in kN/m\(^3\)) to take into account small frictional effects between crack faces and to avoid large unrealistic out-of-plane drifts of the wall portions between the cracks (Table 4).

\[
k_{cxi} = \frac{E_{mi}}{L_f} \times 10^6 (kN/m^3) \approx 0 \text{ for any } E_{mi}
\]

<table>
<thead>
<tr>
<th>Property</th>
<th>( E_{mi} ) (MPa)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Young’s modulus (MPa)</td>
<td>350</td>
</tr>
<tr>
<td></td>
<td>1000</td>
</tr>
<tr>
<td></td>
<td>10000</td>
</tr>
<tr>
<td>Poisson ratio</td>
<td>0.2</td>
</tr>
<tr>
<td>Unit weight (kg/m(^3))</td>
<td>1800</td>
</tr>
<tr>
<td>Interface stiffness in normal direction</td>
<td>( k_{czi} ) ( (E_{mi}/L_f) \times 10^6 \equiv 0 )</td>
</tr>
<tr>
<td>Interface stiffness in tangential directions</td>
<td>( k_{cxi} = k_{cyi} ) ( E_{mi} \times 10^3 )</td>
</tr>
</tbody>
</table>

Monitored wall settlements (considered in the first stage analyses) and estimated free-field ground settlements (used in the second stage analyses) are imposed to the bedding interfaces at the bottom surfaces of the solid walls. The same element type (T18IF) as used to model the pre-existing cracks is used for the bedding. Figure 9b schematically explains the relationship between applied and resultant displacements on the each side of the bedding interfaces. In this figure, \( \delta_p(x,y) \) is the applied vertical prescribed deformation and \( \delta_{wall}(x,y) \) is the resultant displacement at the bottom of the walls of the structure. For the increasing values of \( k_{bz} \) the modulus of subgrade reaction (referred to as bedding stiffness hereafter)
δ_{wall} approaches to δ_v, i.e. for k_{bz} → ∞, δ_{wall} = δ_v. The latter is equivalent to excluding the bedding interface from the model. Lower values of k_{bz} (corresponds to a softer soil) will lead to relative displacements in the normal direction of the bedding interface, δ_v-δ_{wall}. The effect of using a nonlinear soil model in the analyses has been investigated by the previous researchers (Burd et al., 2000 & Fargnoli et al., 2015). It was shown that more realistic simulations are possible by considering small-strain nonlinearity and stiffness reduction with increasing deformation in the soil model. However, in this study, a linear elastic material model with a constant bedding stiffness is used. Although the bedding stiffness is not a specific material property for soil, Bowles (1996) suggested that guide values given in Table 5 can be used to estimate the correct order of this quantity. Utilizing Bowles’s guide values, four different bedding stiffness values varying in a broad range are considered in the parametric analyses (5000, 20000, 40000 and 80000 kN/m³) (Table 4). Among these, k_{bz3}=40000 kN/m³ is determined as the reference value considering the depth and type of underlying soil layers in the region. The bedding stiffness in transverse direction is assumed close to zero. Note that the bedding interface does not contribute to the flexural stiffness of the wall; its main function will be the monitoring of the relative displacement distribution underneath the walls and to simulate the effect of soil layers underneath the walls.

Table 5: Guide values proposed by Bowles (1996) for bedding stiffness

<table>
<thead>
<tr>
<th>Soil type</th>
<th>k_{bz} (kN/m³)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Loose sand</td>
<td>4800-16000</td>
</tr>
<tr>
<td>Medium dense sand</td>
<td>9600-80000</td>
</tr>
<tr>
<td>Dense sand</td>
<td>64000-128000</td>
</tr>
<tr>
<td>Clayey medium dense sand</td>
<td>32000-80000</td>
</tr>
<tr>
<td>Silty medium dense sand</td>
<td>24000-48000</td>
</tr>
<tr>
<td>Clayey soil</td>
<td>12000-24000</td>
</tr>
<tr>
<td>q_a ≤ 200 kPa</td>
<td>24000-48000</td>
</tr>
<tr>
<td>200 &lt; q_a ≤ 800 kPa</td>
<td>&gt;48000</td>
</tr>
<tr>
<td>q_a &gt; 800 kPa</td>
<td></td>
</tr>
</tbody>
</table>

Note: q_a is the allowable bearing pressure.
A two-stage numerical analysis approach for the assessment of the settlement response of the pre-damaged historic Hoca Pasha Mosque

![Diagram](image)

**Fig. 9:** (a) Mosque model geometry (b) Interface model and (c) interface configuration for the isolated SW wall

### 5.1 The first stage analysis results for building model verification by using measured settlements

In order to verify the building model, this section presents preliminary analysis results. These analysis results are based on two temporary simplifications of the numerical model:

1. The critical issue of defining the settlement fields and a realistic bedding stiffness are avoided, by using measured wall settlements as displacement loads at the bottom of the building.

2. The response of each load-bearing wall to the displacements imposed at the bottom of that wall is analysed for each wall separately, by ignoring the loading effects from the three remaining walls, but by including the flange effects (stiffness contribution) of other connecting walls.

As an example, Fig. 9c presents the modified analysis model for the SW wall. No bedding interface is assigned at the bottom of this wall: the applied prescribed deformations (i.e. the measured settlements) will be transferred directly to the wall. The analyses performed in this section are based on the measured settlements at the end of July 2011 when NPLT, SPFV and NPFV tunnels were completed (Figs. 4 and 7b). The measured settlements are distributed along the wall length based on the assumption that the settlements are varying linearly...
between the monitoring points SB8, SB19 and SB18. On the other hand, an extremely soft bedding interface stiffness (1 kN/m$^3$) is assigned to the bottom of the remaining walls. In this way, the rest of the structure still exerts a stiffness influence on wall SW. The Young’s modulus $E_{m1}$ and $E_{m3}$ for the masonry walls are used in successive analyses. The SW wall includes the C5 and C6 cracks (defined with a very low normal stiffness). In a variation study, these cracks are excluded. The cracks on the other walls are always excluded from the model.

Figures 10 and 11 show the deformation and crack opening results obtained for the SW wall without and with crack interfaces (C5 and C6), respectively. In the first case, it is seen that the major principal tensile strains ($\varepsilon_p$) concentrate around the small niche at the upper side of the wall as well as the bottom parts of the central windows. The maximum principal tensile strain ($\varepsilon_{p\text{max}}$) reaches about 0.080%. This value exceeds slightly the tensile strain range (0.038% - 0.060%) that was previously reported by Burhouse (1969) as the onset of visible cracking in the brick masonry walls. The presence of the C5 and C6 cracks in the second case results in a remarkable change in $\varepsilon_p$ distribution. It is seen that the C5 and C6 cracks reduce the strain levels in their vicinity, however they result in an increase in the strain levels at the bottom parts of the central windows. The maximum principal tensile strain reaches about 0.1%. In both cases, the damage class of SW wall is assessed slight damage based on the comparison made between $\varepsilon_{p\text{max}}$ and the suggested limiting tensile strain intervals of Boscardin and Cording (1989) (see Table A.1 in appendix).

The variation of the relative crack displacements ($\delta_{cz}$) along the height of the C5 and C6 cracks are shown in Figs. 11b and c, respectively. Crack C6 is opening more uniformly and widely, whereas C5 widens more at the upper part and relatively less. A direct comparison of numerical and monitored crack openings is not straightforward due to aforementioned restrictions. Instead, making comparisons based on the summed crack openings of the two cracks makes sense. The analysis yields that the total crack opening of C5
and C6 (C5 + C6) ranges from 7 to 9.5 mm from the bottom to the top of the cracks. The sum of the monitored crack openings (C5+C6) (at the end of July 2011 in Fig. 6) is 5.3 mm.

![Fig. 10: ε_p distribution in SW without C5 and C6 crack interfaces (E_m = 350 MPa)](image)

**Fig. 10:** ε_p distribution in SW without C5 and C6 crack interfaces (E_m = 350 MPa)

![Fig. 11: (a) ε_p distribution in SW wall with crack interfaces and relative crack displacements of (a) C5 and (b) C6 cracks (E_m = 350 MPa)](image)

(a) ![Crack displacement (mm)](image)
(b) ![Crack displacement (mm)](image)
(c) ![Crack displacement (mm)](image)

**Fig. 11:** (a) ε_p distribution in SW wall with crack interfaces and relative crack displacements of (a) C5 and (b) C6 cracks (E_m = 350 MPa)

Similar modelling and analysis procedures are executed for the NE, NW and SE walls. The results obtained from these analyses are summarized in Table 6. As seen, the magnitude of shown ε_pmax values are relatively low as in the case of SW wall. This would result in negligible to slight damages for these walls (Table A.1).

An in-plane rotation is observed for the wall portion between the C1 and C2 cracks in NE wall (Fig. 12a). Due to this rotation, while the C1 closes at the upper part C2 widens and
the other way around at the bottom part as observed from the outside of the mosque. For these crack interfaces, the overall relative crack displacement ($\delta_{cz}$) from bottom to upper tip varies between -0.33 mm (closing) and 4.71 mm (opening). On the other hand, a diagonal out-of-plane rotation is observed for the C3-2 crack in the NW wall (Fig. 12b). Finally, the SE wall experiences the lowest distortion compared to other walls in which the C10 crack tends to close.

![Fig. 12: Rotation of crack interfaces from (a) perspective (C1&C2) and (b) side view (C3-2)](image)

Table 6: Numerical results for NE, NW and SE walls (with and without pre-existing cracks)

<table>
<thead>
<tr>
<th>Wall</th>
<th>Max. principal strain (without cracks) ($E_m = 350$ MPa)</th>
<th>Max. principal strain (with cracks) ($E_m = 350$ MPa)</th>
<th>Remarks for relative crack displacements</th>
<th>Estimated damage class according to Table A.1</th>
</tr>
</thead>
<tbody>
<tr>
<td>NE</td>
<td>$\varepsilon_{p_{\text{max}}} = 0.060%$ Near to upper and lower section of the central part of the wall</td>
<td>$\varepsilon_{p_{\text{max}}} = 0.055%$ Near to upper and lower section of the central part of the wall</td>
<td>Fig. 12a</td>
<td>Very slight damage in both cases</td>
</tr>
<tr>
<td>NW</td>
<td>$\varepsilon_{p_{\text{max}}} = 0.075%$ Observed at several sections near to window and wall corners</td>
<td>$\varepsilon_{p_{\text{max}}} = 0.075%$ Observed at several sections near to window and wall corners</td>
<td>Fig. 12b</td>
<td>Slight damage in both cases</td>
</tr>
<tr>
<td>SE</td>
<td>$\varepsilon_{p_{\text{max}}} = 0.025%$</td>
<td>$\varepsilon_{p_{\text{max}}} = 0.025%$</td>
<td>C10 uniformly closes</td>
<td>Negligible damage in both cases</td>
</tr>
</tbody>
</table>

Note that varying the Young’s modulus of the masonry from 350 MPa ($E_m^1$) to 10000 MPa ($E_m^3$) results in insignificant changes in the magnitudes of the principal strains and crack openings. As seen in Table 6, the obtained crack activities and determined damage classes based on the tensile strain levels are in line with the actual monitoring results and in-situ
building observations. Recall that, during the excavation and construction works, while the pre-existing cracks were active a few new cracks of insignificant extent have occurred. The agreement between the results of the first stage analyses and reality shows the suitability of the building model and choice of the range of the elastic material parameters.

5.2 Second stage parametric analyses performed by using estimated free-field ground settlements

In this sub-section, the settlement response of the mosque will be examined using parametric analyses based on generated settlement fields. The rational of this kind of analyses compared to the previous ones, in which measured settlements are used as input, is to offer an opportunity to examine the crack activities and overall response without having the knowledge of the building settlements. Furthermore, the effect of different masonry and bedding properties and modelling configurations (i.e. with or without crack and bedding interfaces) are investigated in this section.

Due to aforementioned limitations of in-situ free-field ground settlement data, 3D settlement fields have to be estimated. For the shaft excavation, WVS, 3D settlement field (Fig. 13b) is produced based on empirical 2D free-field settlement profile curve (Fig. 13a). For NPLT, SPFV and NPFV tunnels, 3D settlement fields (Figs. 13c, d and e) are based on reported 2D finite element models (Fig. 13a). Each settlement field is formed as a vertical settlement displacement matrix and applied as a prescribed deformation load to the interfaces at the bottom of the walls. The combined settlement field (Fig. 13f) is the superposition of all of the matrices formed for each separate excavation (WVS, NPLT, SPFV and NPFV). Details of the sub-studies to estimate 3D settlement fields for WVS and tunnels are explained in the following sections 5.2.1 and 5.2.2.
5.2.1 Derivation of the 3D settlement field for WVS from the calculated empirical ground settlements

For the estimation of free-field ground settlements and the derivation of corresponding settlement field due to the shaft excavation, the study of Moorman (2004), in which 530 case histories of retaining walls and ground movements due to deep excavations are analysed, is used. Moorman shows that the movements of the shaft wall and the surrounding ground seem to be largely independent of the stiffness of the retaining wall system. According to the author, once a sufficient stiffness is provided, the movements are governed by other relevant factors. Thus, an additional increase of the system stiffness does not lead to a corresponding decrease of movements. Similar conclusions were obtained by Clough and O’Rourke (1990) and Long (2001). Considering this, the mixed type wall construction of the current shaft can be considered as single type wall and empirical settlement relationships proposed for uniform retaining wall constructions can be used for the entire depth of the shaft ($H_e = 58$ m).

Moorman (2004) also shows that the maximum ground settlements ($\delta_{vm}$) behind an excavation wall can vary in a wide range. For relatively stiff clays (undrained shear strength $c_u \geq 0.075$ MPa), he observed that the maximum ground settlement ($\delta_{vm}$) to excavation depth ($H_e$) ratio takes a value between 0% (no ground settlement) and 0.90%. The average $\delta_{vm}/H_e$ ratio is reported as 0.18%. A similar range (0.00-0.20%) for the average value of $\delta_{vm}/H_e$ was also previously proposed by Clough and O’Rourke (1990) and Long (2001).

In the current study, considering the magnitude of measured settlements, an average value of $\delta_{vm}/H_e = 0.12 \%$ which is in the proposed range can be assumed. In this case, $\delta_{vm}$ is calculated as 69.6 mm for $H_e = 58$ m. In order to calculate the corresponding ground settlement profile for $\delta_{vm}/H_e = 0.12 \%$, Peck’s (1969) Gaussian formula [Eq. (2)] can be used as introduced in the study of Lee et al. (2007). This curve was originally suggested to estimate free-field ground settlement profiles due to tunnelling. Afterwards, Lee et al. (2007)
used this function to predict the excavation-induced ground settlement profile behind an excavation wall assuming that the wall stands at the inflection point of the Gauss curve. In Eq. (2), \( \delta_v \) is the ground settlement at any distance \( r \) from the shaft wall and \( W \) shows the settlement trough width proposed by Caspe (1966). \( W \) can be calculated using Eq. (3). Therein, \( H_i \) is settlement influence depth below the excavation level and \( \varphi \) is the friction angle of the soil. \( H_i \) is calculated according to Eq. (4) for soils with \( \varphi > 0 \). \( \varphi \) is assumed to be 30° in the current case. \( B \) shows the excavation width and can be taken as 24.6 m as the average diameter of the elliptical shaft in the current study.

\[
\delta_v = \delta_{vm} \cdot e^{0.5 - 0.5 \left(1 + \frac{2r}{W}\right)^2} \tag{2}
\]

\[
W = (H_e + H_i) \tan(45 - \frac{\varphi}{2}) \tag{3}
\]

\[
H_i = 0.5B \tan(45 - \frac{\varphi}{2}) \tag{4}
\]

Fig. 13b shows the contours of the settlement field which is produced for the shaft excavation based on the Peck’s (1969) Gaussian curve (Fig. 13a). Note that the 3D settlement field was constructed by applying the 2D Gaussian curves in radial directions of the elliptical shape of the shaft starting from the position of the shaft wall.

5.2.2 Derivation of the 3D settlement fields for NPLT, SPFV and NPFV tunnels from the 2D numerical results

Free-field ground settlements due to tunnel excavations were obtained from the numerical analysis results reported by the contractor company (Fig. 13a) (Prediction of Ground Surface Settlement Report, 2011). In these analyses, 2D plane strain conditions were considered. Man-made fill (I) and clayey silty sand (II) layers were modelled using an elasto-plastic Mohr-Coulomb model. Besides the elastic properties, anisotropic damage parameters were
used to reduce the shear modulus of the greywacke (III). Damage parameters were determined through back analyses based on the monitored crown and spring line settlements of the concerned tunnels. Fig. 13c, d, and e show the contours of the settlement fields which are produced based on the numerical simulations (Fig. 13a). As seen, the curvilinear NPLT excavation yields curved settlement contours and the SPFV and NPFV form skewed line contours corresponding to the geometry and position of these tunnels. In line with the monitoring results of the mosque (Fig. 4), the settlement contours resulting from the NPFV excavation indicate much higher settlements in comparison with the NPLT and SPFV excavations. Figure 13f shows the combination of all settlement contours resulting from the WVS shaft and NPLT, SPFV and NPFV tunnels. Note that this combined settlement field corresponds to a site settlement stage when the NPLT, SPFV and NPFV tunnels were completed (at the end of July 2011). A sagging due to combination of the settlement contours of the WVS and NPLT can be noted for the SE wall. The other walls are hogging. This situation is also in line with the monitored responses of these walls. However, two discrepancies between estimated and actual settlements should be highlighted and the probable reasons should be discussed:

- Although the estimated settlements are increasing towards the SE-SW corner (SB18) due to closeness of this corner to the WVS, SPFV and NPFV excavations (see Fig. 2a and Figs. 13b, d and e), a more severe settlement was measured in reality for the SE-NE corner (SB14). The reason of reading higher settlement from SB14 monitoring bolt might be due to a possible local discontinuity and stiffness difference in the relatively thick and loose man-made fill. The region has been a trade and residential centre over the centuries and many archaeological relics including ancient building parts and wells have been discovered (Fig. 14) (Iwano et al., 2013).
Since the influence of other neighbouring tunnels (SPF, CE and ISL) cannot be considered in the generation of the combined settlement field, the magnitudes of the estimated combined settlements is slightly lower than the measured values. Although these excavations contributed to an extent to the settlement of the mosque, they cannot be included in the settlement field calculations due to geometrical difficulties. In order to consider the effect of SPF and CE, interaction between SPF&CE and shaft wall should be investigated by further analyses. Similarly, accounting for the effect of ISL excavation that have a different alignment (sloping upward to the ground surface) would require physical modelling of this excavation in 3D.

Despite these limitations, the generated settlement fields are believed to reflect the basics of the ground movements near the Hoca Pasha Mosque.

**Fig. 13:** (a) Reported or derived 2D free-field ground settlement estimations which are used to produce settlement fields and 3D settlement field contours generated for (b) WVS, (c) NPLT, (d) SPFV, (e) NPFV and (f) combination of WVS, NPLT, SPFV and NPFV excavations
A two-stage numerical analysis approach for the assessment of the settlement response of the pre-damaged historic Hoca Pasha Mosque

Fig. 14: Archaeological building remains in a shaft excavation in the region

Table 7: The features of the parametric analyses

<table>
<thead>
<tr>
<th>Property</th>
<th>Analysis 1 (reference)</th>
<th>Analysis 2</th>
<th>Analysis 3</th>
<th>Analysis 4</th>
<th>Analysis 5</th>
<th>Analysis 6</th>
<th>Analysis 7</th>
<th>Analysis 8</th>
<th>Analysis 9</th>
</tr>
</thead>
<tbody>
<tr>
<td>Young’s modulus of the masonry ($E_m$) (MPa)</td>
<td>350</td>
<td>1000</td>
<td>10000</td>
<td>350</td>
<td>350</td>
<td>350</td>
<td>350</td>
<td>350</td>
<td>350</td>
</tr>
<tr>
<td>Bedding stiffness ($k_{bd}$) (kN/m$^3$)</td>
<td>40000</td>
<td>40000</td>
<td>40000</td>
<td>5000</td>
<td>20000</td>
<td>80000</td>
<td>40000</td>
<td>No</td>
<td>No</td>
</tr>
<tr>
<td>Presence of pre-existing cracks</td>
<td>Yes</td>
<td>Yes</td>
<td>Yes</td>
<td>Yes</td>
<td>Yes</td>
<td>Yes</td>
<td>No</td>
<td>Yes</td>
<td>No</td>
</tr>
<tr>
<td>Used settlement field</td>
<td>Combined (Fig. 13f)</td>
<td>Combined (Fig. 13f)</td>
<td>Combined (Fig. 13f)</td>
<td>Combined (Fig. 13f)</td>
<td>Combined (Fig. 13f)</td>
<td>Combined (Fig. 13f)</td>
<td>Combined (Fig. 13f)</td>
<td>Combined (Fig. 13f)</td>
<td>Combined (Fig. 13f)</td>
</tr>
</tbody>
</table>

5.2.3 Second stage analysis results

The second stage analyses are performed using the combined 3D settlement field shown in Fig. 13f (Table 7). The Analyses 1 (reference), 2 and 3 aim to investigate the effect of the Young’s modulus of the masonry. Analyses 1, 4, 5 and 6 investigate the effect of the bedding stiffness using a constant Young’s modulus of the masonry. Analyses 7 and 8 study the effect of the leaving out the pre-existing crack and bedding interfaces, respectively. In analysis 9 both interfaces have been left out.
A two-stage numerical analysis approach for the assessment of the settlement response of the pre-damaged historic Hoca Pasha Mosque

Note that, all these are linear analyses, based on the following assumptions:

i) The bedding interface will remain under compression when considering all loads: any potential separation between soil and building is surpassed.

ii) The crack interfaces will remain open: the need for an increased stiffness value in case of a crack closure is left out.

Using constant stiffness properties for these interfaces is then justified. It has been verified that with the inclusion of the building weight all bedding interfaces will indeed remain under compression for all analyses. The crack interfaces represent cracks with an initial crack opening in the range of 5 to 10 mm. No detailed information about the exact openings is available. For some of the cracks and for some analyses a maximum closure is observed of 10 mm for a part of the crack, which thus suggests a full closure of cracks at some locations and would demand for an increase of interface stiffness. However, this effect has been left out in the analyses, since the occurrence of possible crack closures is very limited and because of the limited available data on initial cracks openings. An additional advantage of linear analyses is that superposition allows to analyse only the effect of the settlement loads which will facilitate the interpretation of the results.

The contours of the principal tensile strain ($\varepsilon_p$) and relative displacements of the crack and bedding interfaces ($\delta_{cz}$) obtained through the Analyses 1-9 are presented in Figs. 15-17. In addition, the ranges of the variation of the openings and closings throughout the concerned crack and bedding interfaces are shown comparatively in the Appendix in Fig. A.1 for each analysis. Note that, in Fig. A.1, while negative values show closings positive values show either openings in the crack interfaces or partial unloading of bedding interface from one compressed state of the soil to another. The values illustrated by the red circles are the in-situ crack measurements at the end of July 2011.
The results of Analyses 1, 2 and 3 show that an increasing structural stiffness through the increase of the Young’s modulus of the masonry walls affects the conformity of the walls to the applied prescribed deformations. The more homogenous distribution of the bedding displacements (relative displacements of the bedding interface are being close to zero) in Analysis 1 indicates that the structure, which has the lowest stiffness, mostly conforms to the applied prescribed deformations (Figs. 15 and A.1). This situation eventually results in higher principal tensile strains within the structure. Increasing structural stiffness results in increased relative displacements in the bedding interface (Figs. 15 and A.1). The magnitude of the maximum principal tensile strain decreases and the structure tends to remain undeformed. This result is completely in line with the findings of previous studies of Potts and Addenbrooke (1997) and Son and Cording (2005). They established a relationship between soil/structure stiffness ratio and potential building distortions and observed that as this ratio decreases, the building distortions decrease.

As the structural stiffness increases, C1 tends to widen at its bottom part and close at its upper part in a more pronounced manner. The C2 acts the other way around due to rotation of the wall portion between C1 and C2 crack interfaces as observed in the first stage analysis of NE wall in section 5.1. The summed magnitude of the relative displacements of C5 and C6 crack interfaces decreases slightly. Cracks C3-1 and C3-2 have the lowest relative displacement regardless increasing stiffness. As the Young’s modulus increases, C10 changes to a partial opening from a closure (Figs. 15 and A.1).
A two-stage numerical analysis approach for the assessment of the settlement response of the pre-damaged historic Hoca Pasha Mosque

Analysis 1 (reference case)  Analysis 2  Analysis 3

$\varepsilon_{p_{\text{max}}} = 0.075\%$  $\varepsilon_{p_{\text{max}}} = 0.070\%$  $\varepsilon_{p_{\text{max}}} = 0.045\%$

Increase of the soil stiffness is simulated with the increase of bedding stiffness. As the bedding stiffness is increased from $k_{bz1}$ to $k_{bz4}$ (through the Analyses 4, 5, 1 and 6, respectively) a remarkable increase of principal tensile strain in the walls is observed (Figs. 15 and 16). This is because higher bedding stiffness yields higher stress in comparison to a soft bedding subjected to same magnitude of prescribed settlement deformation. Recall that increasing soil/structure stiffness ratio results in increases of the structural distortions. On the other hand, a stiffer bedding interface leads to a more uniform relative displacement distribution which almost equals to zero in magnitude (see Analysis 6). As the bedding stiffness increases, the relative displacements of the localized cracks change insignificantly. Analysis 8 can be considered as the extreme case in terms of the bedding stiffness ($k_{bz} \to \infty$).
For this analysis, while an increase in the tensile principal strain values is observed, the relative displacements of the localized cracks are similar to those obtained for other bedding stiffness values.

![Analysis Results](image)

**Fig. 16**: The results of the Analyses 4, 5 and 6 (Variation of the bedding stiffness)

Finally, comparing the results of Analyses 1 & 7 and 8 & 9 shows that the presence of pre-existing cracks reduces the principal tensile strains in the close vicinity of the cracks, but results in an increase in other neighbouring sections (Fig. 17). This result was also observed in the previous section 5.1 in which each wall was examined separately. Since the model used in Analysis 9 does not include crack interfaces, a concentration of principal tensile strain appears at the upper sections of the SW and NE walls. Although principal tensile strains reach the highest magnitude in Analysis 8 and 9, the maximum principal tensile strain does usually not
A two-stage numerical analysis approach for the assessment of the settlement response of the pre-damaged historic Hoca Pasha Mosque exceed 0.14 % which corresponds to slight damage according to Table A.1. This result is also in line with the results found in previous section and site observations.

<table>
<thead>
<tr>
<th>Analysis 7</th>
<th>Analysis 8</th>
<th>Analysis 9</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\varepsilon_p = 0.060%$</td>
<td>$\varepsilon_p^{\text{max}} = 0.080%$</td>
<td>$\varepsilon_p = 0.065%$</td>
</tr>
</tbody>
</table>

Fig. 17: The results of the Analyses 7, 8 and 9 (Variations of pre-existing cracks and bedding)

6. Conclusions

The settlement response of the historic Hoca Pasha Mosque to a nearby network of shaft and tunnel excavations is numerically examined. The problem has a series of challenges due to uncertainties regarding mostly the excavation activities, soil properties, building material and pre-existing damages. These typical difficulties are inherently encountered in such case studies. In order to put off some of these uncertainties a two-stage analysis approach is adopted. First the 3D structural model (with and without existing cracks) is verified in a way
that each façade wall is loaded separately using the measured settlements and taking into account flange affects (stiffness contribution) of other connecting walls. This stage to a large extend reduces modelling uncertainties. In the second stage, the effects of other parameters i.e. the building stiffness, bedding stiffness and combined settlement field due to sequential excavation works are investigated. This naturally increases the modelling uncertainties, but is closer to the practice of predicting settlement responses.

The following conclusions can be derived from the reproduced response of the mosque:

- Using a two-stage analysis approach, the actual response of the building can be satisfactorily represented. Despite the serious simplifications in modelling, the overall settlements and crack activities could be simulated realistically. In accordance with the site observations, analysis results showed that the tensile strains in the walls are usually of relatively limited magnitude: a few new cracks of insignificant extent occurred due to settlements.

- Including existing cracks into modelling through the discrete interfaces reduces tensile strains in the close vicinity but results in an increase in the tensile strains of other neighbouring sections. While the activity of the existing cracks is considerably influenced by the increase of the Young’s modulus of masonry, the variation of the bedding stiffness in the considered range has a limited effect.

- Excluding both bedding and existing crack interfaces during modelling results in the most severe case in terms of tensile strain level and tensile strain distribution.

Besides the examination of the specific case of historic Hoca Pasha Mosque, the performed parametric analyses supported by the sub-studies regarding the determination of 3D settlement fields also provide useful outputs to reach more generalizable results.

The obtained results confirm the previous findings in the literature:
- Increased structural stiffness through the increase of the Young’s modulus of the masonry walls reduces the conformity of the structure to the applied prescribed settlements and leads to lower tensile strains.

- Increase of the soil stiffness is simulated with the increase of the bedding stiffness. The higher the bedding stiffness is the more the structure conforms to the applied prescribed settlements. This eventually results in increased tensile strains. As an extreme condition, excluding bedding interface corresponds to a case with infinite bedding stiffness.

**Acknowledgements**

The authors would like to express their thanks to DLH Marmaray Directorate General for their permission to use the project information. Special thanks are due Mr. Gokbora Akay, control manager of the project, who generously gave of his time to help with the project details. The architectural suggestions of Ms. Nurcan Sefer and in-situ drawings of Mr. Dogan Akgun is appreciated. The authors also thank to Mr. Maziar Partovi and Mrs. Hee-Jeong Kang from DIANA FEA BV for the technical support.
Appendices

Fig. A.1: The ranges of variation of relative displacements of crack and bedding interfaces
A two-stage numerical analysis approach for the assessment of the settlement response of the pre-damaged historic Hoca Pasha Mosque

**Table A.1:** Damage classification table (modified from Burland et al., 1977 and Boscardin and Cording, 1989)

| Category of damage | Damage class | Description of typical damage and ease of repair\(^a\)\(^b\) | Approximate crack width\(^c\) (mm) | Limiting tensile strain boundaries (%)
<table>
<thead>
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<tbody>
<tr>
<td></td>
<td>0-Negligible</td>
<td>Hairline cracks</td>
<td>Up to 0.1 mm</td>
<td>$\varepsilon_{lim(low)}$ $\varepsilon_{lim(up)}$</td>
</tr>
<tr>
<td>Aesthetic damage</td>
<td>I-Very slight</td>
<td>Fine cracks that can easily be treated during normal decoration.</td>
<td>Up to 1 mm</td>
<td>0.050             0.075</td>
</tr>
<tr>
<td></td>
<td>II-Slight</td>
<td>Cracks can be easily filled. Cracks are visible externally.</td>
<td>Up to 5 mm</td>
<td>0.075             0.150</td>
</tr>
<tr>
<td>Functional damage</td>
<td>III-Moderate</td>
<td>The cracks require some opening up and can be patched by a mason.</td>
<td>5 to 15 mm or a number of cracks larger than 3 mm</td>
<td>0.150             0.300</td>
</tr>
<tr>
<td>affecting</td>
<td>IV-Severe</td>
<td>Includes large cracks. Extensive repair work is required.</td>
<td>15 to 25 mm but also depends on the number of cracks</td>
<td>0.300</td>
</tr>
<tr>
<td>serviceability</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Structural damage</td>
<td>V-Very severe</td>
<td>Beams lose bearing, walls lean and require shoring, and there is a danger of structural instability.</td>
<td>Usually larger than 25 mm but also depends on the number of cracks</td>
<td>0.300</td>
</tr>
<tr>
<td>affecting stability</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Notes:
\(^a\) Location of damage in the building or structure must be considered when classifying the degree of damage.
\(^b\) Descriptions are shortened for brevity. Refer to Burland et al. (1977) for full descriptions.
\(^c\) Crack width is only one aspect of damage and should not be used alone as a direct measure of it.

**Funding:** This work was financially supported by the Scientific and Technological Research Council of Turkey (TUBITAK) [2214-A scholarship reference number: 1059B141500705].

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