

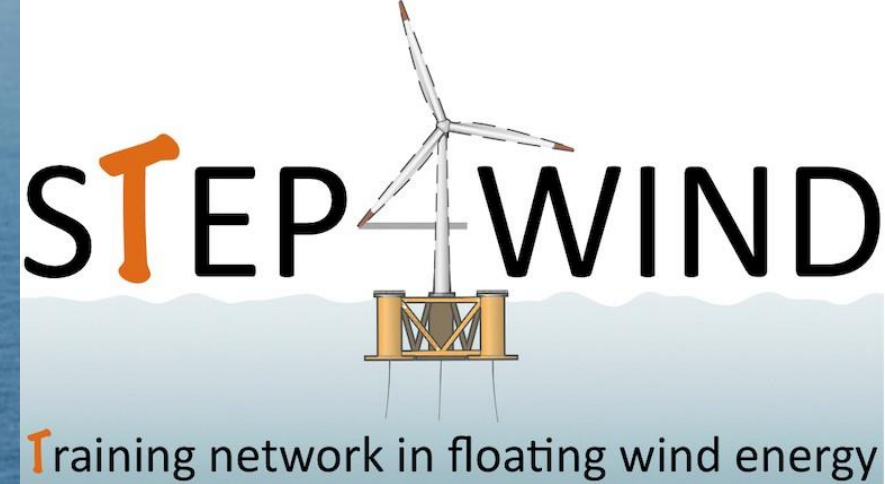
# Data-Driven Surrogate Models for (Floating) Offshore Wind Turbines



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Photo: Principle Power



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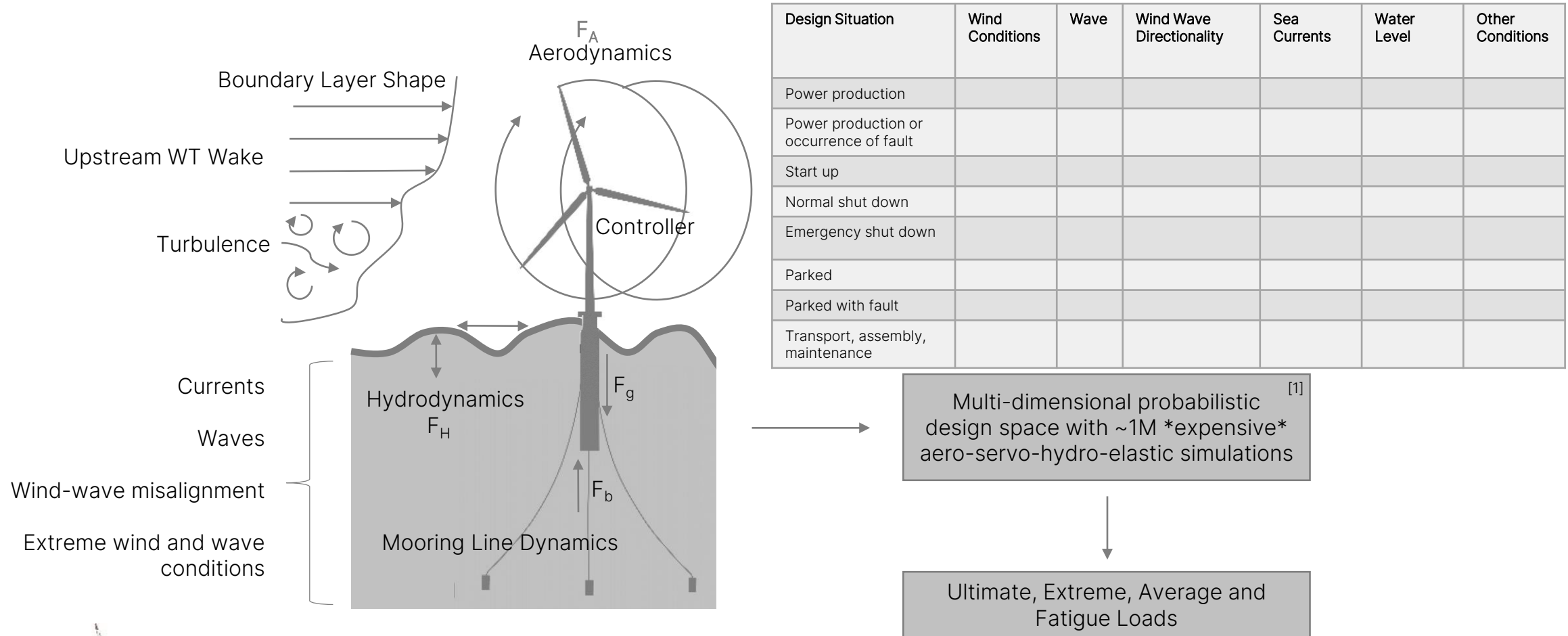


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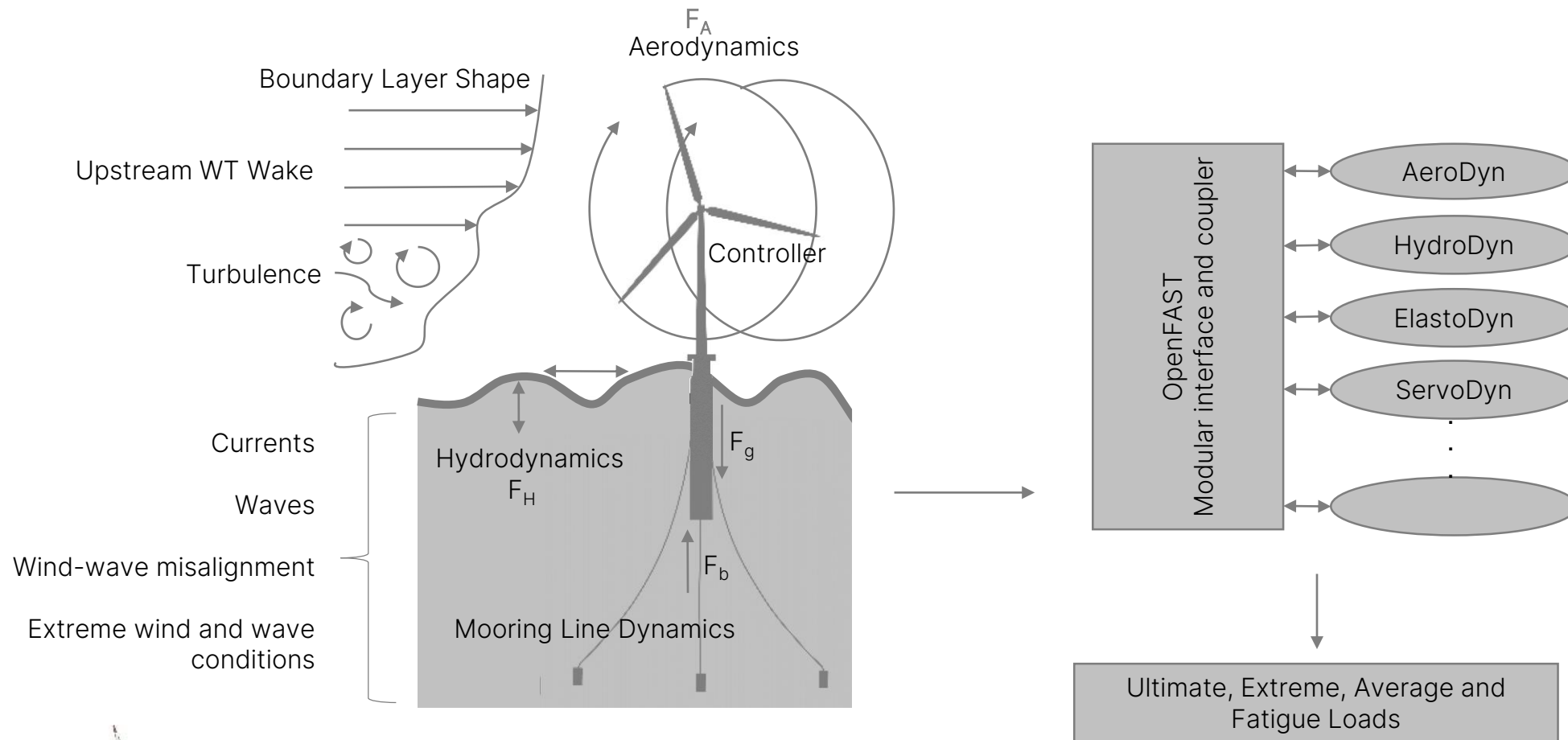
# Structure

- WHAT and WHY: FOWT design challenges
- HOW: machine learning framework and stochastic models

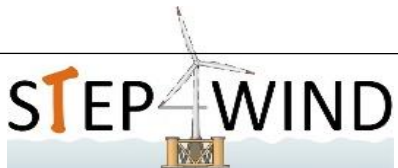
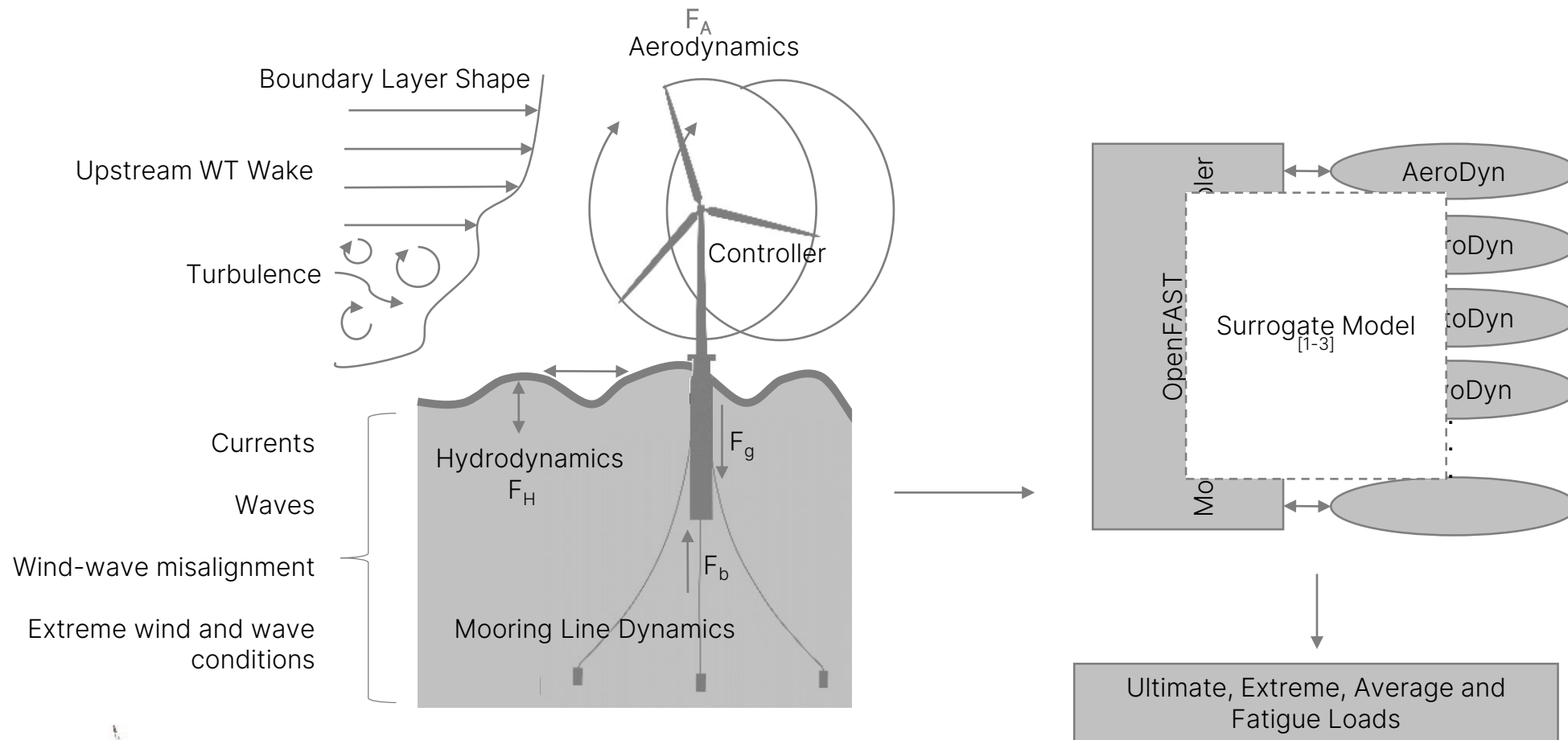
# Wind Turbine Design Challenges



# Wind Turbine Design Challenges



# Proposed Solution



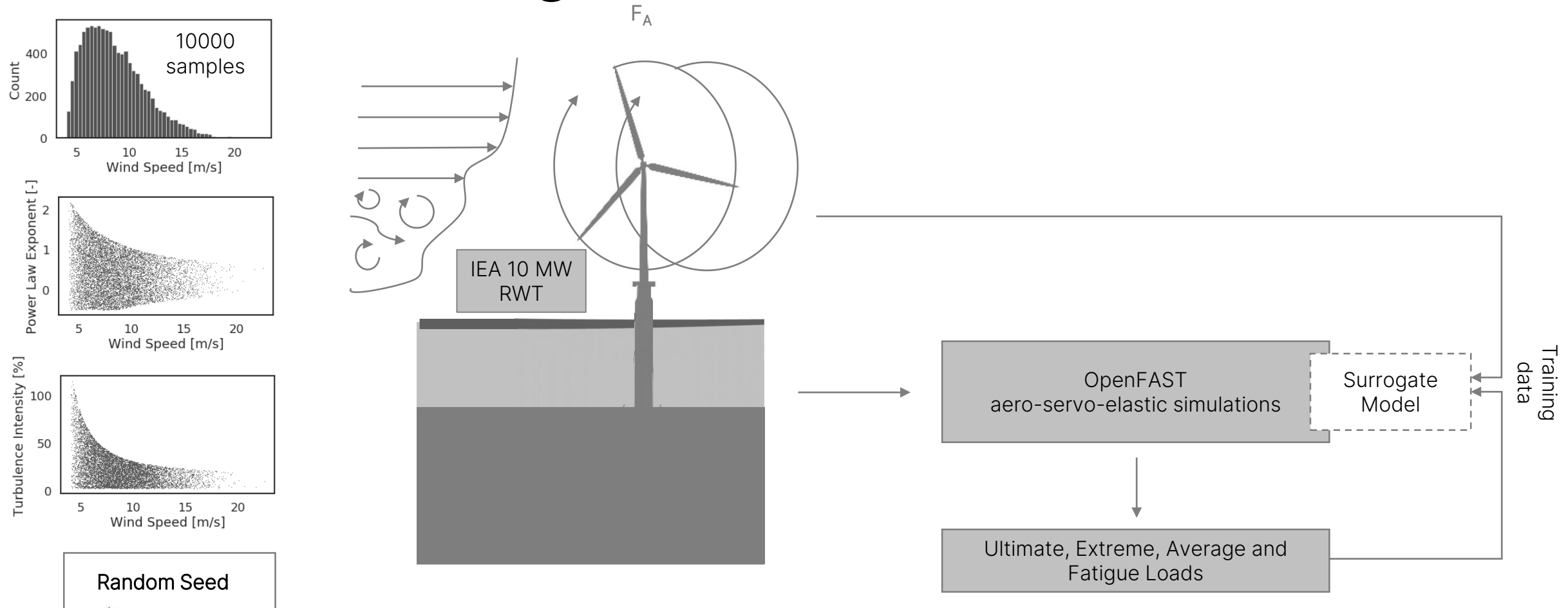
- Ref** [1] Dimitrov, N. K., Kelly, M., Vignaroli, A., Berg, J., From wind to loads: wind turbine site-specific load estimation with surrogate models trained on high-fidelity load databases (2018) Wind Energy Science
- [2] Schröder, L., Dimitrov, N. K., Verelst, D. R., A surrogate model approach for associating wind farm load variations with turbine failures (2020) Wind Energy Science
- [3] Zhu, X., Sudret, B. Global sensitivity analysis for stochastic simulators based on generalized lambda surrogate models (2021) Reliability Engineering & System Safety



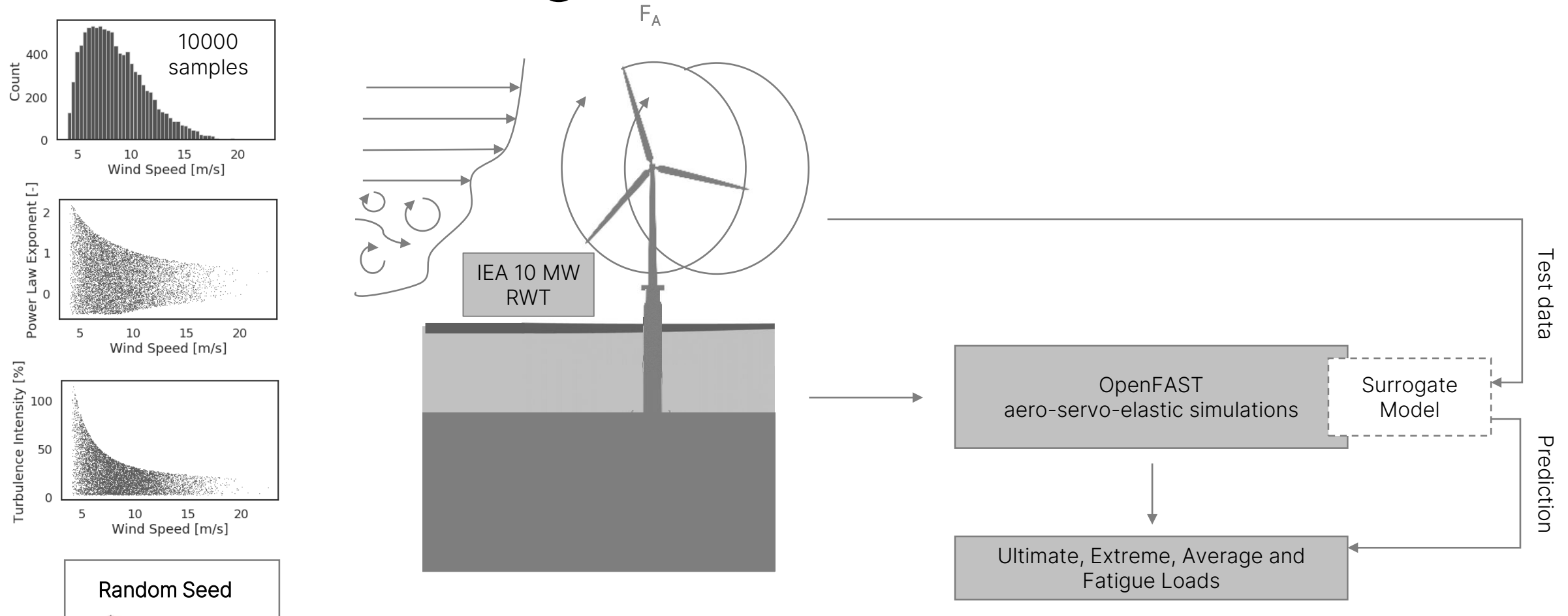
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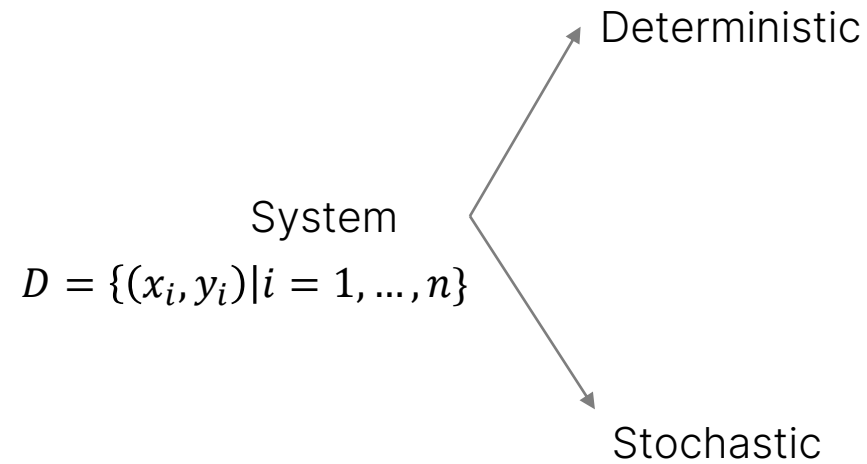
# Machine Learning Framework



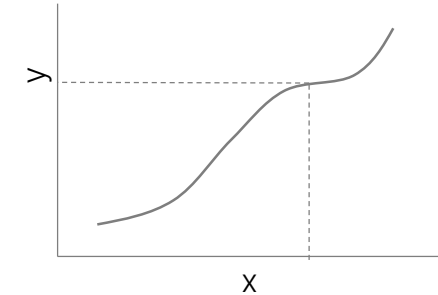
# Machine Learning Framework



# System Behaviour

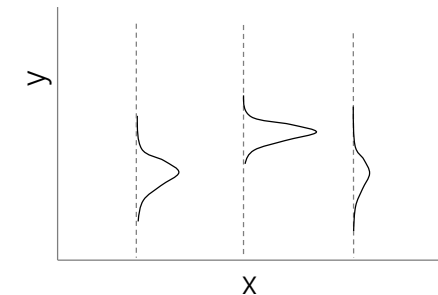


$$M_d: x \mapsto y$$



$$M_s: D_x \times \Omega \rightarrow \mathbb{R}$$

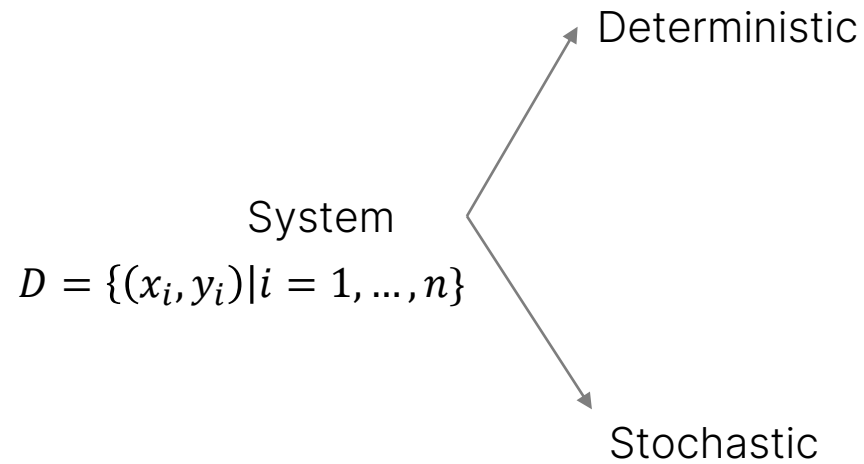
$$(x, z) \mapsto M_s(x, z)^{[1]}$$



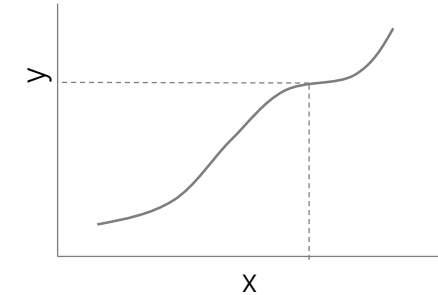
Ref [1] Zhu et. al., Replication-based emulation of the response distribution of stochastic simulators using generalized lambda distributions (2020) International Journal for Uncertainty Quantification



# System Behaviour

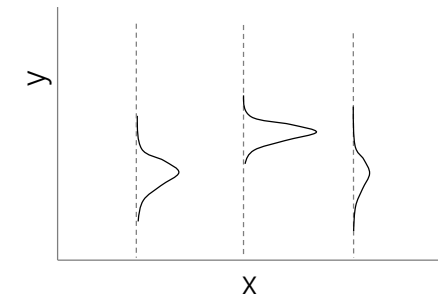


$$M_d: x \mapsto y$$



$$M_s: D_x \times \Omega \rightarrow \mathbb{R}$$

$$(x, z) \mapsto M_s(x, z)^{[1]}$$



If  $x = x_0$ :

$$(Y|X = x_0) \equiv M_s(x_0, z)$$

If  $z = z_0$ :

$$x \mapsto M_s(x, z_0)$$

Ref [1] Zhu et. al., Replication-based emulation of the response distribution of stochastic simulators using generalized lambda distributions (2020) International Journal for Uncertainty Quantification

# Stochastic Models

Dataset  $D = \{(x_i, y_i) | i = 1, \dots, n\}$

- Gaussian Process Regression/ Kriging<sup>[1]</sup>

Gaussian process is a class of probability distribution over possible functions that fit a set of points, and represents prior knowledge about  $f$

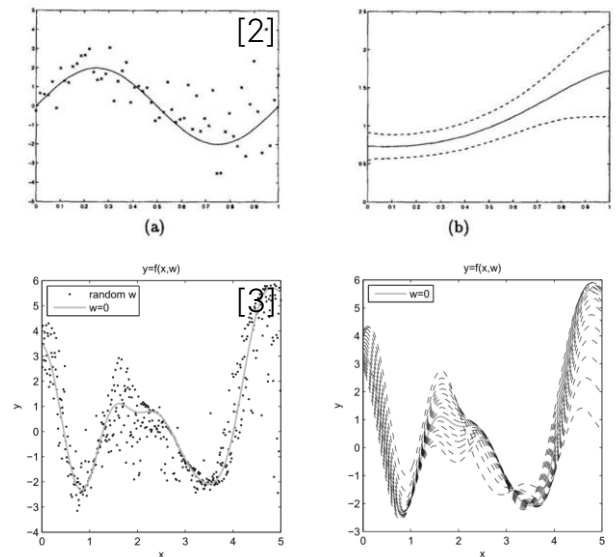
$$\begin{aligned} y_i &= f(x_i) + \epsilon_i \\ \epsilon_i &= N(0, \sigma^2) \\ cov(y_i, y_j) &= \eta^2 \exp\left(-\frac{1}{2} \frac{|x_i - x_j|^2}{l^2}\right) + \sigma^2 \delta_{ij} \\ y|D &= N(\hat{\mu}, \hat{\Sigma}) \end{aligned}$$

- Gaussian Process with a latent variance<sup>[2]</sup>

$$\begin{aligned} y_i &= f(x_i) + \epsilon_i \\ z_i &= \log\left(SD(\epsilon(x_i))\right) = r(x_i) + J_i \end{aligned}$$

- Gaussian Process with a latent covariate<sup>[3]</sup>

$$\begin{aligned} y_i &= g(x_i, z_i) + \zeta_i \\ f(x) &= \int g(x, z) p(z) dz \\ cov(y_i, y_j) &= \eta^2 \exp\left(-\sum_{k=1}^p \frac{1}{2} \frac{|x_i - x_j|^2}{l_k^2} - \frac{(z_i - z_j)^2}{l_{p+1}^2}\right) + \sigma^2 \delta_{ij} \end{aligned}$$

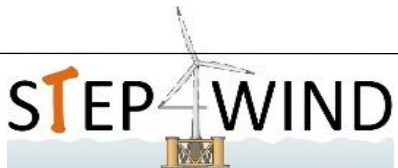


Ref [1] C. E. Rasmussen & C. K. I. Williams, Gaussian Processes for Machine Learning (2006) MIT Press. ISBN 026218253X

Useful: <https://aerodynamics.lr.tudelft.nl/~rdwight/cfddiv/Videos/04/index.html>

[2] Goldberg, P. W., Williams, C. K. I., Bishop, C. M., Regression with input dependent noise: A Gaussian process treatment (1998) Advances in neural information Processing Systems

[3] Wang, C., Neal, R., Gaussian Process Regression with Heteroscedastic or Non-Gaussian Residuals (2012) arXiv:1212.6246v1



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# Stochastic Models

Dataset  $D = \{(x_i, y_i) | i = 1, \dots, n\}$

- Stochastic gradient variational Bayes<sup>[1]</sup>
- Conditional generative model<sup>[2]</sup>

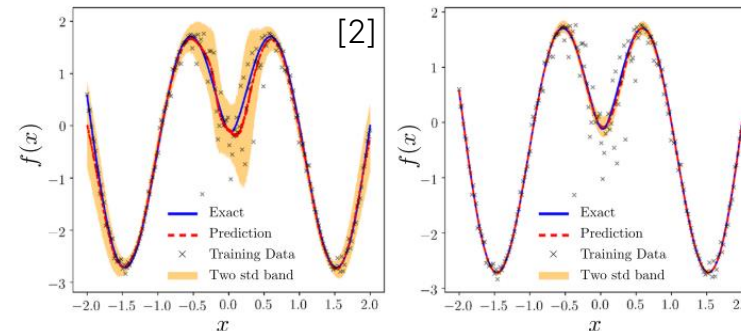
$$y = f_{\theta}(x, z)$$

$$p(y|x) = \int p(y|x, z) p(z|x, y) dz$$

$p(y|x, z)$  parametrized to  $p_{\theta}(y|x, z)$  -> decoder

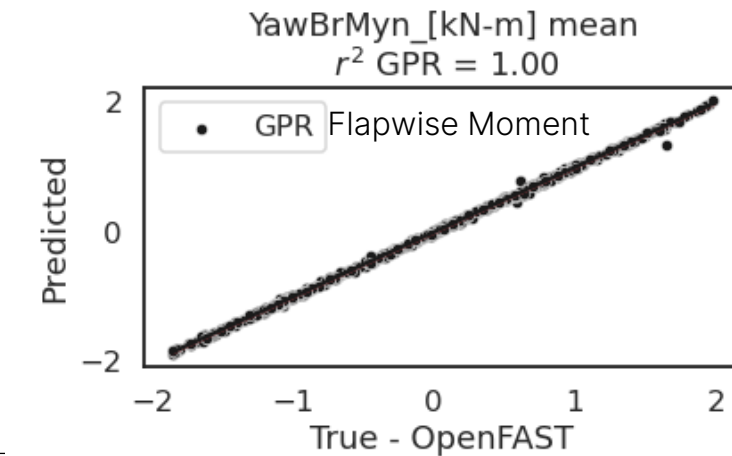
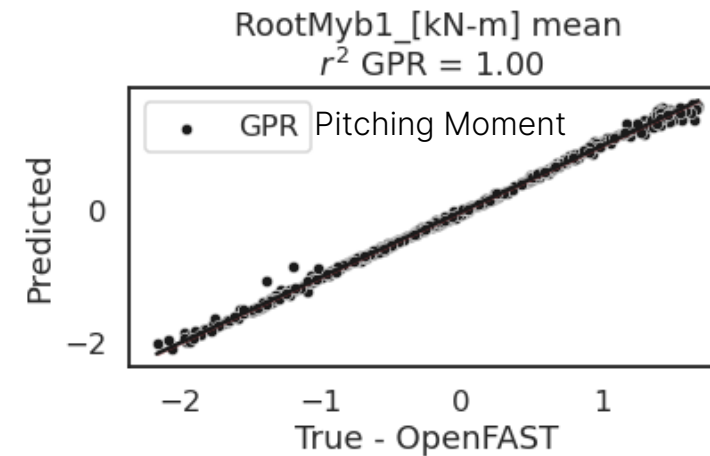
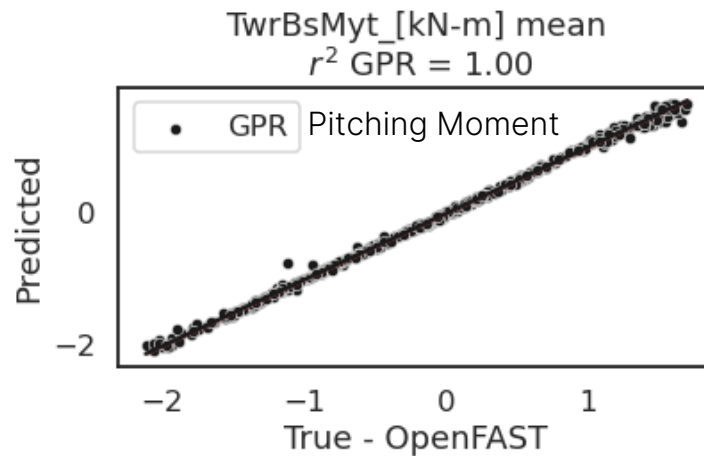
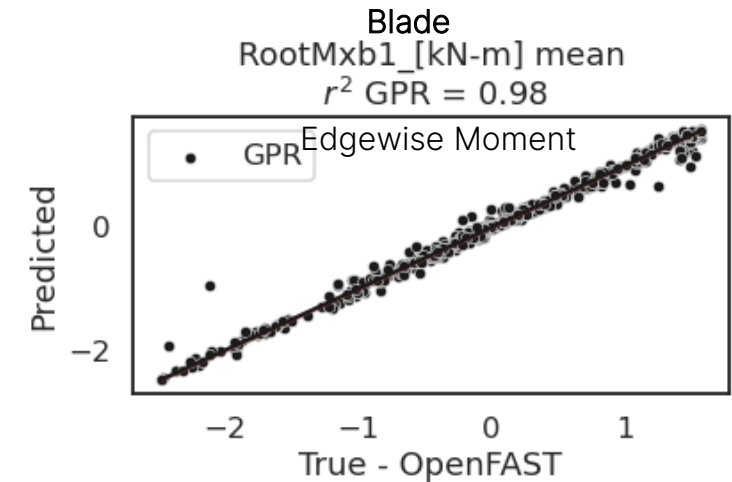
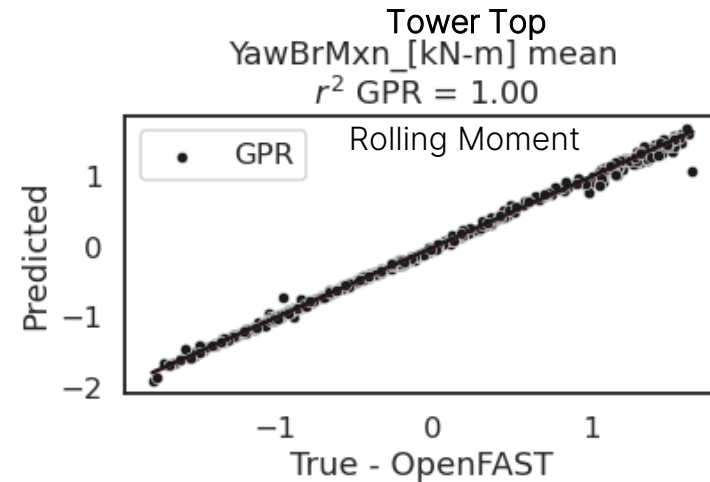
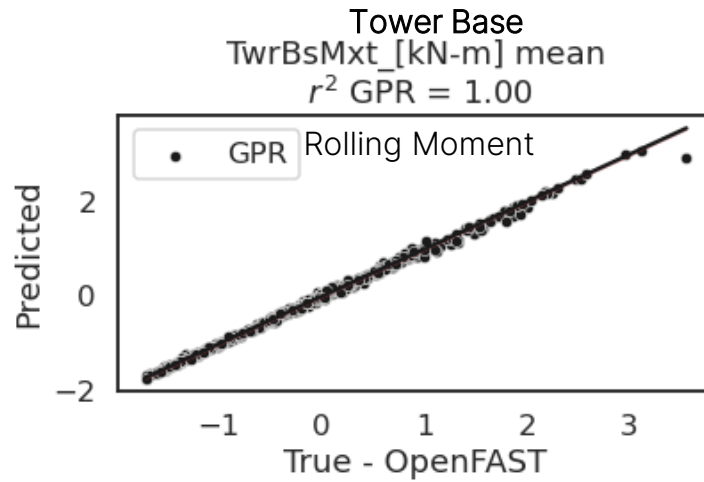
$p(z|x, y)$  parametrized to  $q_{\phi}(z|x, y)$  -> encoder

The model is trained by minimizing difference between the joint distribution of the generated data  $p_{\theta}(x, y)$  and the joint distribution of the observed data  $q(x, y)$

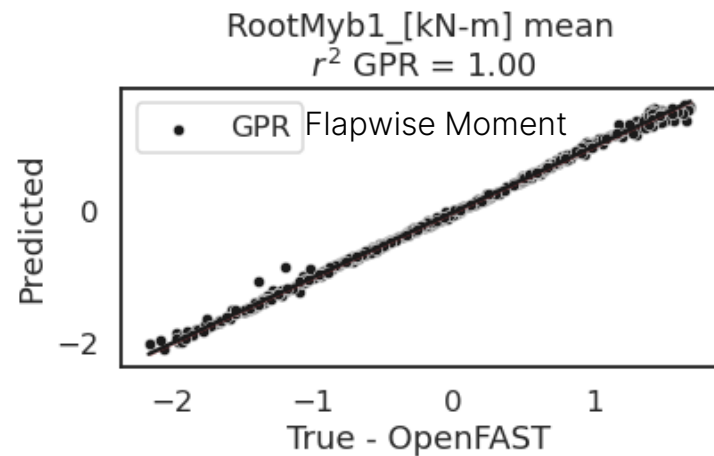
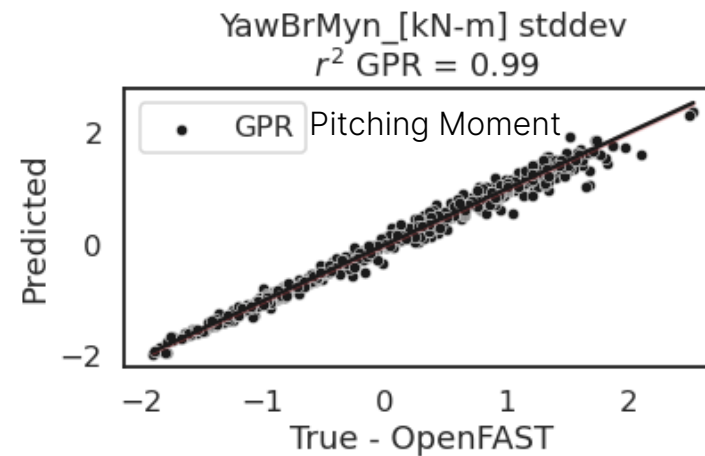
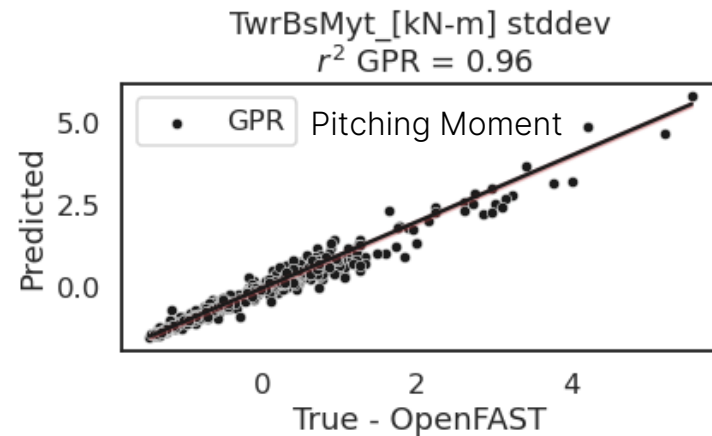
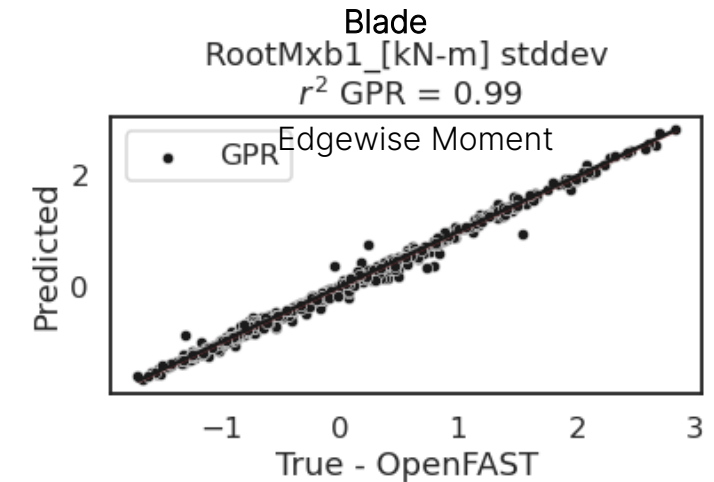
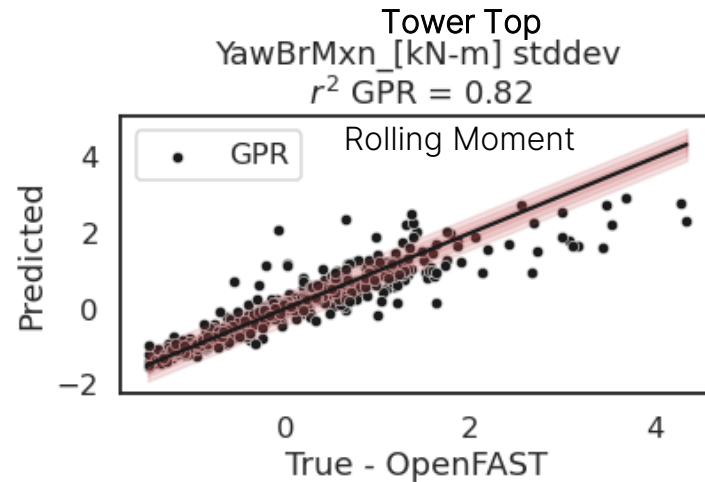
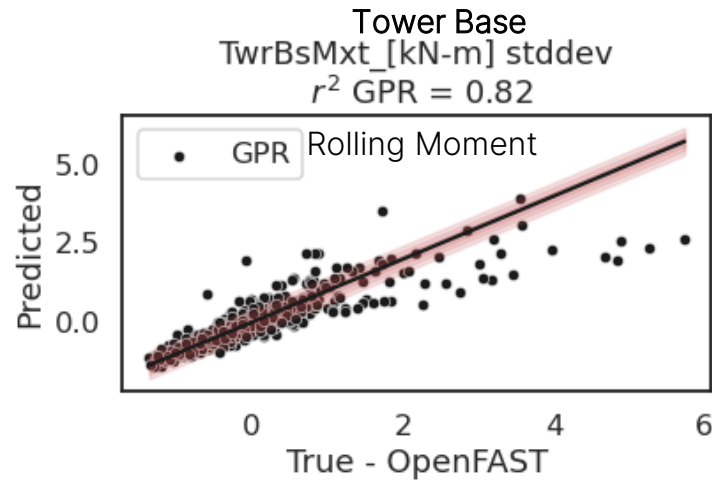


- Replication based models<sup>[3]</sup>
  - Regression performed over the parameters of a generalizable PDF
- Overview of other interesting methods: reference<sup>[4]</sup>

# Results - averaged loads



# Results – stddev loads



# Questions

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