

Integrated phononic waveguides in diamond

Ding, Sophie Weiyi; Pingault, Benjamin; Shao, Linbo; Sinclair, Neil; Machielse, Bartholomeus; Chia, Cleaven; Maity, Smarak; Lončar, Marko

DOI

[10.1103/PhysRevApplied.21.014034](https://doi.org/10.1103/PhysRevApplied.21.014034)

Publication date

2024

Document Version

Final published version

Published in

Physical Review Applied

Citation (APA)

Ding, S. W., Pingault, B., Shao, L., Sinclair, N., Machielse, B., Chia, C., Maity, S., & Lončar, M. (2024). Integrated phononic waveguides in diamond. *Physical Review Applied*, 21(1), Article 014034. <https://doi.org/10.1103/PhysRevApplied.21.014034>

Important note

To cite this publication, please use the final published version (if applicable).
Please check the document version above.

Copyright

Other than for strictly personal use, it is not permitted to download, forward or distribute the text or part of it, without the consent of the author(s) and/or copyright holder(s), unless the work is under an open content license such as Creative Commons.

Takedown policy

Please contact us and provide details if you believe this document breaches copyrights.
We will remove access to the work immediately and investigate your claim.

Integrated phononic waveguides in diamond

Sophie Weiye Ding^{1,*}, Benjamin Pingault,^{1,2} Linbo Shao^{1,3}, Neil Sinclair,¹
Bartholomeus Machielse,^{1,4,‡} Cleaven Chia,¹ Smarak Maity,¹ and Marko Lončar^{1,†}

¹*John A. Paulson School of Engineering and Applied Sciences, Harvard University, Cambridge, Massachusetts 02138, USA*

²*QuTech & Kavli Institute of Nanoscience, Delft University of Technology, PO Box 5046, 2600 Georgia Delft, Netherlands*

³*Bradley Department of Electrical and Computer Engineering, Virginia Tech, Blacksburg, Virginia 24061, USA*

⁴*AWS Center for Quantum Networking, Boston, Massachusetts 02135, USA*



(Received 1 August 2023; revised 27 November 2023; accepted 22 December 2023; published 19 January 2024)

Efficient generation, guiding, and detection of phonons, or mechanical vibrations, are of interest in various fields, including radio-frequency communication, sensing, and quantum information. Diamond is a useful platform for phononics because of the presence of strain-sensitive spin qubits, and its high Young's modulus, which allows for low-loss gigahertz devices. We demonstrate a diamond phononic waveguide platform for generating, guiding, and detecting gigahertz-frequency surface acoustic wave (SAW) phonons. We generate SAWs using interdigital transducers integrated on AlN/diamond and observe SAW transmission at 4–5 GHz through both ridge and suspended waveguides, with wavelength-scale cross sections (approximately 1 m^2) to maximize spin-phonon interaction. This work is a crucial step for developing acoustic components for quantum phononic circuits with strain-sensitive color centers in diamond.

DOI: [10.1103/PhysRevApplied.21.014034](https://doi.org/10.1103/PhysRevApplied.21.014034)

I. INTRODUCTION

Acoustic devices at microwave frequencies have been studied intensively because of the advantages they offer over their electromagnetic counterparts: smaller wavelengths, and hence reduced sizes, lower crosstalk, and lower losses [1–3]. These properties also make them good candidates for applications in quantum science and technology since they can provide efficient interfaces between microwave signals and qubits. As a result, quantum phononics, or quantum acoustodynamics (QAD), which relies on phonons as information carriers, has emerged as an active field of study [4–11]. One promising QAD approach uses surface acoustic waves (SAWs) to control and read out qubit states. SAW-based quantum interfaces have been demonstrated for various qubits, including color centers in diamond [12,13] and silicon carbide [14,15], quantum dots [16], and superconducting qubits [17,18].

Among these, the electron spin qubit associated with the negatively charged silicon-vacancy (SiV) color center in diamond has drawn a lot of interest. Diamond, with its high Young's modulus ($>1000 \text{ GPa}$), is an ideal platform for gigahertz-frequency phononics; SiV itself is a

promising quantum memory [19,20] that can be efficiently interfaced with phonons owing to its high strain susceptibility of approximately 100 THz [21,22] while giving access to long-lived nuclear spin-based quantum registers [23]. It has been shown that SAW generated with integrated IDTs can control a single SiV electron spin with a high Rabi rate approximately 30 MHz, as well as a nuclear spin in diamond, using power orders of magnitude lower than for standard microwave control [12]. However, these works are performed in bulk diamond without any waveguiding of the SAW and poor optical collection efficiency, thereby limiting the scalability of this approach and its integrability with other devices. To develop an integrated platform comprising multiple spin qubits with enhanced spin-phonon interaction and to more efficiently guide and detect SAWs, integrating IDTs with micro- and nanostructures such as phononic waveguides or cavities is a necessary step. This furthermore allows for leveraging recent progress with diamond photonic structures for both on-chip spin-phonon and long-distance spin-photon networking of multiple spins.

Here, we experimentally demonstrate integrated phononic waveguides with a ridge as well as suspended structures in single-crystal diamond, which can support phonon modes at high frequencies over 4 GHz. The ridge waveguides, fabricated into AlN-on-diamond, are advantageous for structural stability and strong thermal contact

*wding@g.harvard.edu

†loncar@seas.harvard.edu

‡Work done prior to joining Amazon.

with the diamond substrate. We further develop these structures and fabricate ridge crossing waveguides and observe a large suppression of the crosstalk between the two intersecting waveguides. To realize better confinement of both phonons and photons in waveguides, we demonstrate suspended AlN/diamond nanobeam waveguides and observe SAW transmission. Our results using integrated phononic waveguides pave the way not only for efficient generation, guiding, and detection of SAW on diamond, but also for manipulating spin qubits using SAW with low loss and low-power consumption combined with future photonic integration.

II. ACOUSTIC RIDGE WAVEGUIDE: DESIGN AND FABRICATION

An optical micrograph of the fabricated ridge-waveguide device is shown in Fig. 1(a). Interdigitated transducers (IDTs), patterned on AlN, are used for bidirectional conversion between SAWs and microwaves and are used to generate and detect acoustic waves. We pattern the AlN film to form an acoustic waveguide between the two IDTs: since diamond has a higher speed of sound (12–18 km/s) than AlN (6–10 km/s) [24,25], the traveling wave is bound to the interface between AlN and diamond. Thus, as the width of the AlN region is reduced, the SAW becomes more confined in both AlN and in the diamond beneath.

To design our waveguides, acoustic wave mode simulations have been performed using the finite-element method (FEM) in COMSOL Multiphysics. Figure 1(b) shows the cross section of fundamental shearing and fundamental Rayleigh modes, along with their normalized displacement in the coupler region. Figure 1(c) shows the two modes at the ridge waveguide. In Fig. 1(b), the acoustic wavelength is $2.4\ \mu\text{m}$, which corresponds to shearing and Rayleigh mode frequencies of 3.1, 3.3, and 4.4 GHz, respectively.

Fabrication of the device begins by sputtering 700 nm of AlN on a single-crystal diamond substrate. The AlN thickness is chosen to maximize the electromechanical coupling efficiency, k^2 , for a AlN/diamond interface (Appendix). To pattern the $2\text{-}\mu\text{m}$ -wide waveguide, we first define an etch mask in HSQ using electron-beam lithography (EBL). Then the AlN layer is etched down using reactive-ion etching (RIE) with argon and chlorine gases. Finally, the IDTs and the contact pads are written by EBL using PMMA resist, and created by a liftoff process after depositing a 100-nm-thick Al layer using electron-beam (EB) evaporation.

III. ACOUSTIC RIDGE WAVEGUIDE: CHARACTERIZATION

The device is characterized in the frequency and time domains using the setup shown in the inset of Fig. 2(b).

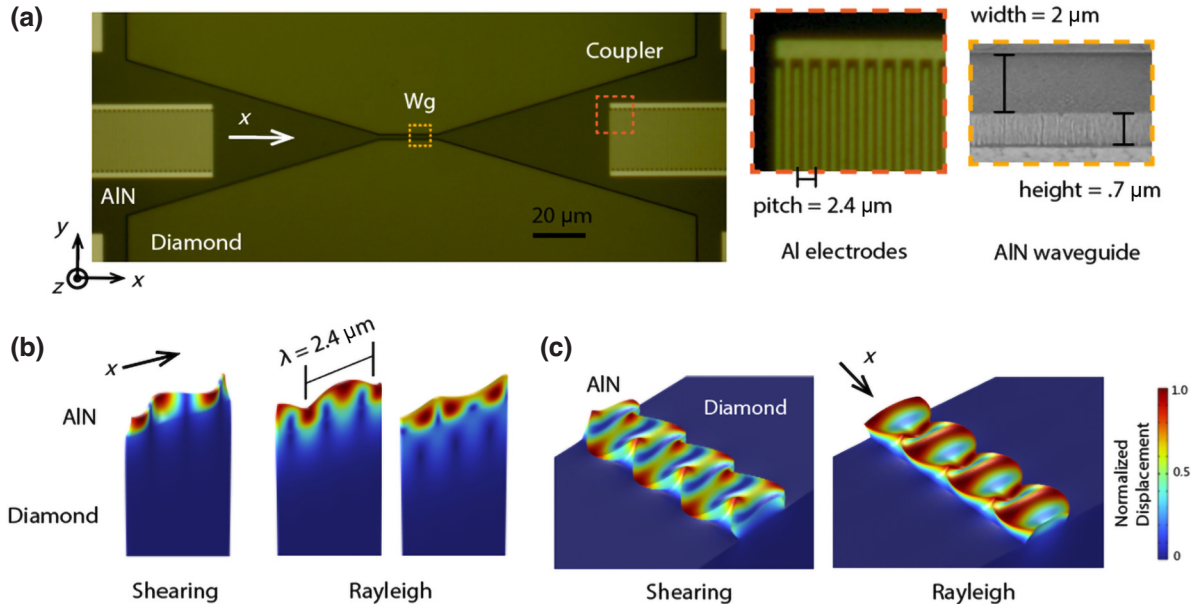


FIG. 1. A surface acoustic ridge-waveguide device using AlN-on-diamond. (a) Images of the device. The microscope image on the left shows a top-down view of the entire device. The enlarged pictures illustrate the detail of the electrodes (microscope image) and the side profile of the waveguide (SEM image, taken at 60° tilt). (b) The cross section of the fundamental SAW modes, shearing and two Rayleigh modes, in the coupler region. An “x” indicates the propagation direction of the wave. (c) The SAW modes propagate in the waveguide section. The fundamental Rayleigh mode is shown.

The measurement reveals three transmission peaks, around 3.2, 4.4, and 7.1 GHz [Fig. 2(a)]. The first two peaks correspond to fundamental shearing and Rayleigh modes and are in good agreement with numerical modeling shown in Fig. 1(b). The shearing mode is suppressed intentionally by selecting a wavelength with respect to the AlN thickness, to achieve its low k^2 (Appendix), but in general can be excited at other wavelengths. The third peak with the highest frequency is a higher-order Rayleigh mode. The Rayleigh 2 mode, shown in Fig. 2(b), has the largest transmission because it has the highest k^2 among the modes (Appendix). The 3-dB bandwidth of the Rayleigh 2 mode is 10 MHz, which is smaller than the predicted IDT bandwidth. This measured bandwidth is loss limited and associated with the presence of the taper and waveguide. The maximum transmission ($|S_{21}|$) of the Rayleigh mode is measured to be -22.4 dB at 4.45 GHz, which is comparable to previous ridge phononic waveguides in low-loss thin-film platforms [26–28]. This gives a speed of sound of 10.7 km/s, which matches the simulated value of $2.4 \text{ } \mu\text{m} \times 4.35 \text{ GHz} = 10.4 \text{ km/s}$.

The time-domain measurement is performed using the setup in the inset of Fig. 2(c). We excited our waveguide with a 5- and a 20-ns pulse at 4.45 GHz, which

correspond to a pulse width of 200 and 50 MHz in frequency, respectively. The measured transmission shown in Fig. 2(c) has several key features. The first pulse (light blue) observed in the time domain corresponds to direct crosstalk between microwave cables used to connect two IDTs, since microwave signals in free space propagate faster than acoustic waves. This pulse has the profile of the input microwave pulse with vestigial noise. The pulse that is delayed by approximately 15 ns from the crosstalk (dark blue, pulse 1) is the SAW transmission. The delay time corresponds to the distance between the IDTs divided by the acoustic velocity, which is $200 \text{ } \mu\text{m}/(11 \text{ km/s}) \sim 18 \text{ ns}$. The SAW transmission is broadened compared to the input pulse due to dispersion imparted by the waveguide. The second pulse (dark blue, pulse 2) is attributed to the SAW reflected by IDTs and is delayed by approximately $45 = 3 \times 15 \text{ ns}$, which corresponds to the time it takes for the SAW to travel the distance between the IDTs for 3 times. The reflection can be mitigated by an asymmetric design, or can be enhanced through phononic structures to make high-quality factor SAW cavities [14,29]. This time-domain measurement confirms the acoustic nature of the signal that can be used to drive SiV spin qubits mechanically.

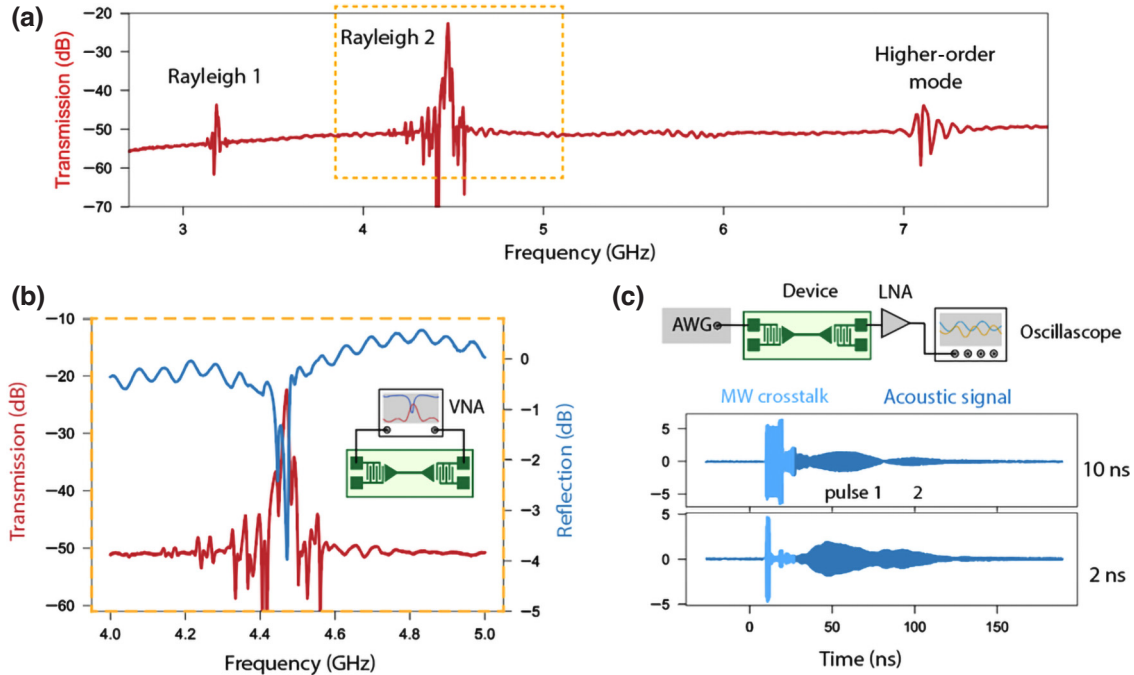


FIG. 2. Characterization of an AlN-on-diamond acoustic waveguide. (a) Frequency-domain measurement of the waveguide. The scan shows three transmission peaks. The Rayleigh mode has the highest transmission. (b) Frequency-domain measurement of the Rayleigh mode. The peak frequency is 4.45 GHz and the 3-dB bandwidth is 10 MHz. The inset depicts the measurement setup. VNA: vector network analyzer. (c) Time-domain measurement setup and response for the Rayleigh mode in arbitrary units. The light blue pulse that arrives first is the microwave crosstalk, pulse 1 is the transmitted SAW, and pulse 2 is the reflected SAW. The end of the crosstalk and the onset of the transmitted SAW signals have some overlap. AWG, arbitrary waveform generator; LNA, low noise amplifier.

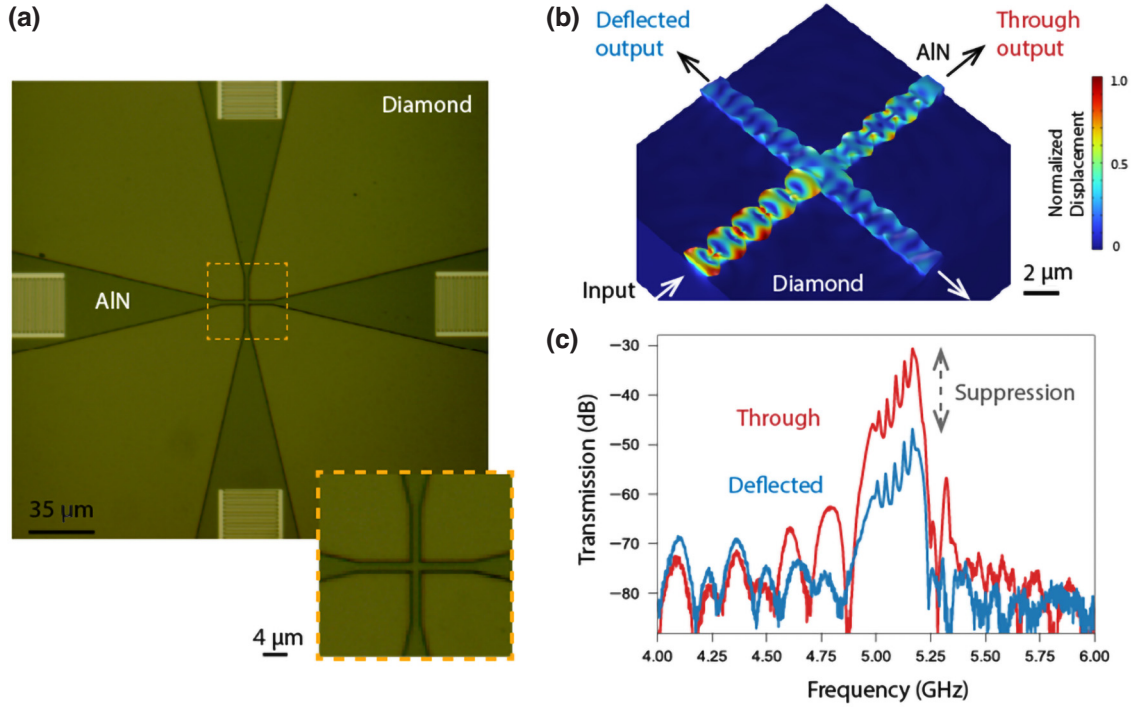


FIG. 3. Acoustic waveguide crossing and crosstalk measurement. (a) Optical microscope image of the cross-waveguide device used to evaluate crosstalk. There is an IDT placed at the end of each waveguide for excitation and collection of SAWs. The inset shows the enlargement into the cross. (b) Simulation of the acoustic Rayleigh mode propagating through the waveguide crossing. (c) Transmission spectra of SAWs of the through and one of the deflected ports of the cross, indicating a maximum crosstalk of -16.3 dB. The transmission data is gated to suppress the microwave crosstalk background.

Based on the realized ridge waveguides, we also demonstrate low-crosstalk waveguide crossings for efficient routing of acoustic waves. The crossing functions as a phononic circuit component to cross gigahertz signals on one plane without significant crosstalk for compact design and routing, as analogous to crossings in photonic circuits. Figure 3(a) shows the structure of the waveguide crossings consisting of two perpendicular waveguides with IDTs at their ends. We first simulate the transmission property in the waveguide crossings by exciting one of the ports with the Rayleigh waveguide mode [Fig. 3(b)] while monitoring SAW transmission into the remaining three waveguide ports. By comparing the energy transmitted into through and cross ports, we estimate crosstalk to be -15.8 dB. We also experimentally characterize fabricated devices and measure a maximum transmission of -30.6 and -46.9 dB into through and cross ports, respectively, resulting in a crosstalk of -16.3 dB [Fig. 3(c)]. This is in good agreement with the simulations. The crosstalk can be further reduced by employing designs inspired by photonic components such as multimode interference (MMI) crossings and subwavelength gratings (SWGs), along with inverse design methods or other design techniques. The transmission into the through port is lower than that in a simple waveguide geometry shown in Fig. 2, because of deflection and scattering loss at the crossing points.

IV. FREE-STANDING ACOUSTIC WAVEGUIDES

One of the loss channels of the ridge waveguide approach is scattering into the substrate, which does not exist for a suspended phononic waveguide. Furthermore, these AIN-on-diamond devices do not support confined optical modes (optical waveguides or cavities) that could be used to, e.g., efficiently collect photons emitted by SiV [20]. For more general acousto-optical applications, we also would like to explore tighter confinement of both optical and acoustic modes [30,31]. To address these points, we consider suspended acoustic waveguides (Fig. 4).

Our device consists of an IDT that is used to excite a SAW, followed by a linear taper used to focus the acoustic energy into the free-standing region and excite its acoustic modes. The dispersion diagram for the modes supported by the suspended waveguide are shown in Fig. 4(b). The two fundamental modes are shown in blue and red, corresponding to flexural versions of the shearing and Rayleigh SAW modes in the ridge waveguide, respectively. Acoustic energy transmitted through the free-standing section is then collected using another tapered section and finally detected using an IDT. The coupler region is designed in a similar fashion as in the case of Figs. 2 and 3.

Device fabrication starts with the deposition of AIN. Next, the electrodes are defined by electron-beam

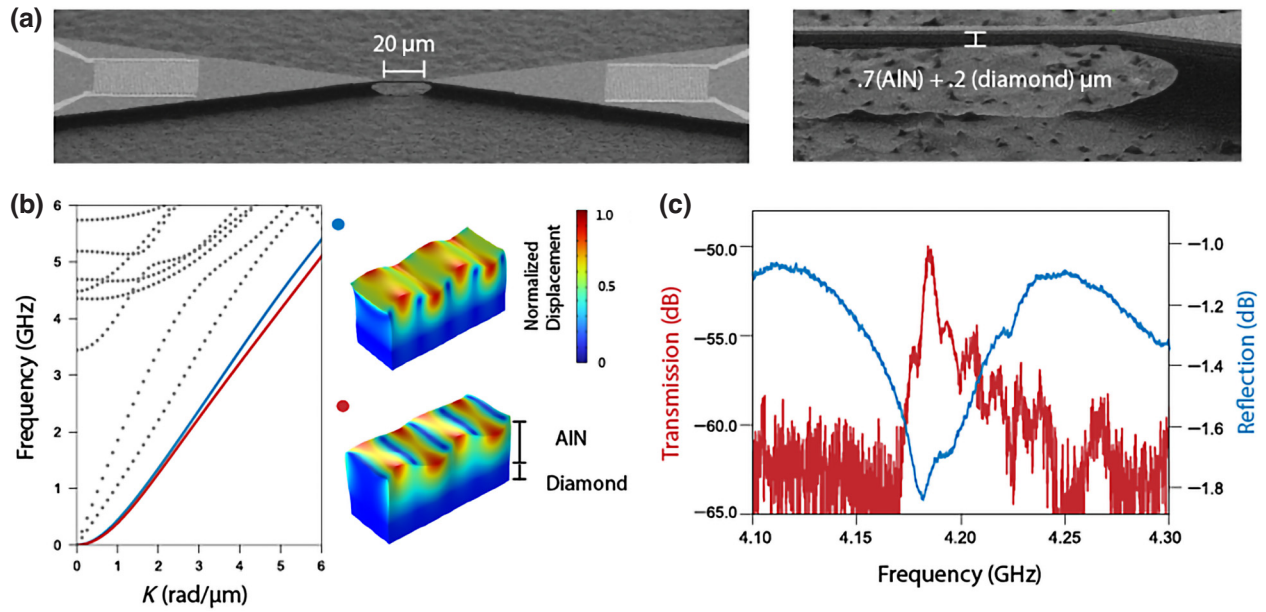


FIG. 4. Suspended acoustic AIN-on-diamond waveguide device and measurement. (a) SEM images (taken at 60° tilt) of a suspended acoustic waveguide. The waveguide is excited using IDTs defined on nonsuspended regions. The enlarged figure shows the details of the taper and the composition of the waveguide: 700 nm of AIN on 200 nm of diamond. The lighter top region is an AIN chamfer from mask erosion. The bottom darker sleeve is AIN and diamond. (b) Dispersion diagram for acoustic modes supported by the suspended waveguide. The red and blue lines correspond to the flexural versions of shearing and Rayleigh modes, respectively, of the ridge waveguide. (c) Frequency-domain transmission spectra of the fundamental modes showing a maximum transmission and reflection of -50 and -1.8 dB, respectively. The transmission data is gated to suppress the microwave crosstalk background.

lithography and liftoff using Cr/Au (100 nm). The coupler and waveguide patterns are defined using EBL with HSQ resist. Next, RIE with O_2 plasma is used to etch the pattern into the diamond, followed by quasi-isotropic etching to undercut the waveguide and release it from the diamond substrate [32,33]. The suspended section is a 1- μm waveguide, consisting of 700 nm of AIN on 200 nm of diamond [Fig. 4(a)]. This thickness of the diamond is suitable for implantation and study of defects for quantum experiments. We note that tapering between the coupling region and the free-standing section is three dimensional: both laterally and orthogonally from the diamond surface.

We perform scattering-parameter measurements and observe a mode at 4.18 GHz with a 3-dB bandwidth of 7 MHz. The transmission and reflection are measured to be -50 and -1.8 dB at the peak, respectively, comparable to previous only-AIN-suspended-phononic-waveguide works [30,34]. We found that the resonance frequency is different from the ridge waveguide of the same IDT pitch (4.45 GHz). This is due to the suspended waveguide and the use of Cr/Au electrodes, which are heavier. Cr/Au is chosen over Al for the suspended structure to avoid etching by HF in the step to remove the HSQ etch mask. The lower transmission compared to the ridge-waveguide device is due to a smaller modal overlap of the SAW modes in the coupler region and the suspended waveguide mode. The roughness on the bottom of the

waveguide introduced by the quasi-isotropic etch also results in reflection and scattering into other waveguide modes, thus reducing the overall transmission. These challenges are associated with other suspended platforms as well, particularly at the μm -wavelength scales, as active research is being conducted on improving and harnessing their unique properties [30,31,35].

In this case, to overcome the challenges associated with injecting SAWs from the wide section into the suspended narrow waveguide, we consider the structure shown in Fig. 5 as a prospective device. Here, IDTs are defined directly on the free-standing waveguide and can be used to excite the Rayleigh-like mode of the suspended region [Fig. 5(a)], and can be eventually coupled to a phononic crystal for enhanced spin-phonon interaction [Fig. 5(b)]. We expect more efficient coupling because of the elimination of the taper (Appendix), but the challenge associated with this design is impedance matching of narrow IDTs, which is fundamentally limited by k^2 . An example fabricated device is shown in Fig. 5(c). The device is measured but does not show a resonance transmission feature above the noise floor likely due to the large impedance matching.

To enable such a geometry, we can use materials with higher electromechanical coupling (e.g., lithium niobate and Sc-AIN) as the piezoelectric layer, or implement an external impedance matching circuits for better impedance matching [36]. Additionally, we can fabricate the entire

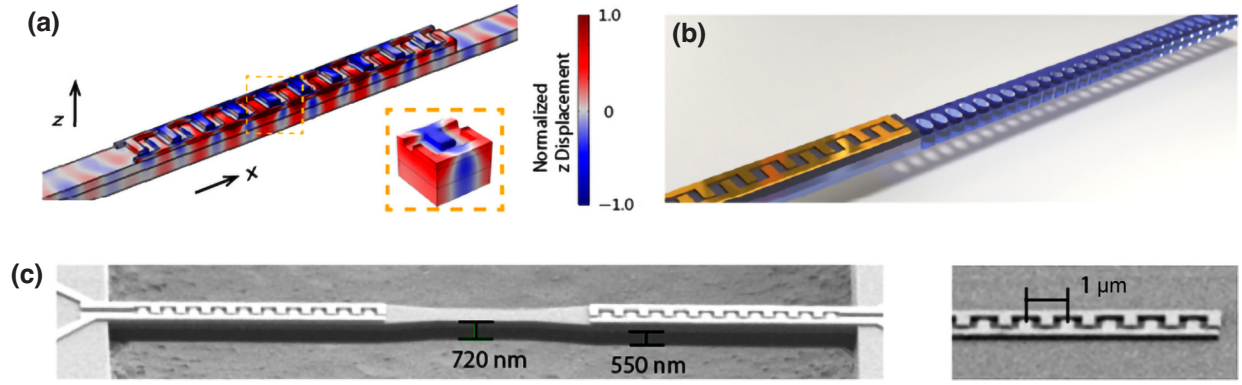


FIG. 5. Fully suspended acoustic AIN-on-diamond waveguide device. (a) Simulation of the mode excited by the IDTs. The frequency of the mode is 6.15 GHz, and the wavelength is 1 μm . (b) A rendered image of the suspended IDT coupled to a mechanical resonator. (c) An SEM image (taken at 60° tilt) of suspended IDT couplers and a suspended waveguide. The enlarged figure shows the metal fingers after the liftoff before the etch.

device on a suspended diamond thin film to reduce loss in tapering and allow for larger capacitance [37].

V. SPIN-PHONON COUPLING BETWEEN AN SiV AND THE ACOUSTIC WAVEGUIDE

The mode frequencies above are designed to match an SiV spin-qubit splitting of about 5 GHz [Fig 6(a)], that can be readily accessed with an applied magnetic field and is typically used for qubit control [20,38]. Based on the simulated waveguide modes and transmission measurements, we can calculate the spin-phonon coupling rate between the fabricated waveguide and an SiV. The acoustic mode is evanescently coupled through the generated strain

to an SiV implanted 50–100 nm below the diamond surface underneath the waveguide.

The spin-phonon coupling rate is given by $g = \sum_{ij} d_{ij} \epsilon_{ij}$, where i, j are indices for the coordinate axes, ϵ is the strain experienced by the SiV produced by a single phonon, d is the spin level strain susceptibility. The strain profile is obtained from the waveguide simulation and the susceptibility has been measured in previous work [21]. For the ridge case, the single-phonon strain is on the order of $10^{-10} - 10^{-12}$, with $\epsilon_{zz} = 5.0 \times 10^{-10}$. The susceptibility is approximately 100 THz/strain for the spin levels of the SiV, depending on the symmetry of the strain and also the spin level splitting, which can be tuned by an external magnetic field [21]. For the ridged waveguide

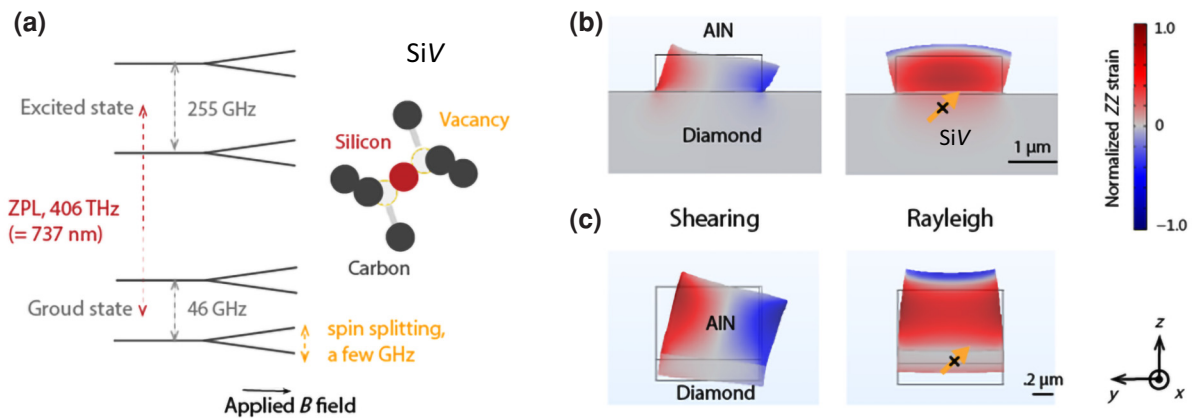


FIG. 6. SiV and the strain profile of the ridge and suspended waveguide mode. (a) SiV energy level diagram and its atomic structure. The spacings between the levels are not drawn to scale. The spin level of interest is tunable by an applied magnetic field, usually around 3–10 GHz. ZPL, zero phonon line. (b) The cross-section profile of the ZZ strain in the ridge waveguide for shearing and Rayleigh modes. ZZ strain often contributes the most to the coupling with the given orientations of the SiV spin in diamond. The values are normalized to the maximum ZZ strain for visualization. The displacement of the mode is shown by the exaggerated deformation. In both cases, the SAW is guided by the waveguide, propagating in the x direction. In the Rayleigh case, strain can be more effectively delivered to the SiV near the surface. (c) The cross-section profile of the ZZ strain in the suspended waveguide region for shearing and Rayleigh mode.

[Fig. 6(b)], the calculated value for a single-phonon Rabi rate is 12–15 kHz for the Rayleigh mode; for the suspended waveguide [Fig. 6(c)], the rate is 15–20 kHz.

To compare the rates to previous SAW works [12,23], we can calculate the Rabi frequency while the SiV is driven in the waveguide, using the measured values for transmission. For 1-mW input power, with empirical external losses taken into consideration (10 dB per port), the projected Rabi frequency is 5.5 GHz for the ridge structure, which is more than 2 orders of magnitude higher than previous works [12,23]. In practice, this means we can drive the SiV efficiently at even lower powers. The calculation details are in the Appendix.

VI. CONCLUSION AND OUTLOOK

We present the fabrication and measurements of a GHz-phononic circuit on diamond for applications in quantum acoustic dynamics (QAD). To improve upon the current bulk diamond platform, we demonstrate the fabrication of both ridge and suspended phononic waveguides, for effective guiding and detection of coherent phonons, as well as for enhanced spin-phonon coupling, 2 orders of magnitude higher than previous works.

This demonstration allows for the injection and collection of phonons from other diamond structures with state-of-the-art phononic properties, such as diamond cantilevers and optomechanical crystals [39,40]. With the platform improvements and the prospect of combining such devices with SiVs, we hope to open up opportunities for exploration of the physics of spin-phonon coupling and its applications.

ACKNOWLEDGMENTS

This work is supported by National Science Foundation (NSF) Science and Technology Center for Quantum Materials (Grant No. DMR-1231319), NSF Engineering Research Center for Quantum Networks (Grant No. DMR EEC-1941583), Office of Naval Research (Grant No. DMR N00014-20-1-2425), Air Force Office of Scientific Research (AFOSR) MURI on Quantum Phononics, and AFOSR (Grant No. DMR W911NF-23-1-0235). B.P. acknowledges funding from the European Union's Horizon 2020 research and innovation programme under the Marie Skłodowska-Curie Grant Agreement No. 840968. The views and conclusions contained in this document are those of the authors and should not be interpreted as representing the official policies, either expressed or implied, of the Army Research Office or the U.S. Government. The U.S. Government is authorized to reproduce and distribute reprints for Government purposes notwithstanding any copyright notation herein.

APPENDIX A: IDT DESIGN

In order to achieve an efficient acoustic spin interface, it is helpful to optimize the geometry of the IDTs used. For example, a large IDT bandwidth (BW) is needed to allow for fast control of SiV spins. This in turn limits the number of IDT pairs (N), that can be used, since $BW \sim f_0/N$, where f_0 is the operating frequency. However, larger N is needed to match the impedance (Z) of the IDT to the standard 50 Ω , thus minimizing the reflection of microwave signals used to excite SAWs. In our design, we chose $N = 30$, which aims at $BW \sim 150$ MHz and $Z \sim 170$ Ω . Notice, because of the symmetric nature of the device, the theoretical maximum transmission would be -6 dB, since each set of the IDTs has a loss of 3 dB. With insertion losses from the tapering and other sources, the measured value is always lower.

The impedance of an IDT is theoretically determined by the real part of its inverse admittance G , which is given by $G = 8k^2 c_s w f_0 N^2$, where k^2 is the electromechanical coupling coefficient, c_s is the capacitance per length, w is the IDT width, f_0 is the SAW central frequency, and N is the number of fingers of the IDT. We experimentally determined that $N = 30$ yields the highest microwave transmission in our device geometry. In practice, the best N is usually less than that given by the impedance matching condition because of loss related to the SAW generation. This geometry yields an impedance of around 170 Ω with the above expression, which gives a reflection signal of -5.2 dB. In our case, because of the low k^2 of thin-film AlN, combined with the need to taper into a narrow waveguide (which limits the width and thus the geometry and total area of the IDT), an exact 50- Ω impedance matching is challenging to achieve.

APPENDIX B: k^2 SIMULATION

The electromechanical coupling coefficient is calculated from the phase velocity difference between the cases where the boundary condition at the IDT coupler surface is electrically free or shorted:

$$k^2 = 2(v_{\text{free}} - v_{\text{shorted}})/v_{\text{free}}.$$

A large k^2 means higher conversion efficiency between electrical and acoustic energy in a piezoelectric material. The following phase velocity and k^2 simulations are performed using COMSOL. Modes 1, 2, and 3 correspond to the shearing and Rayleigh modes presented in the main text, and Rayleigh has the highest transmission because it has the highest k^2 at the given h/λ (Fig. 7).

APPENDIX C: CALCULATING SINGLE SPIN-PHONON COUPLING AND RABI RATE

The simulation produces the strain at a selected location and the total amount of energy in the simulation

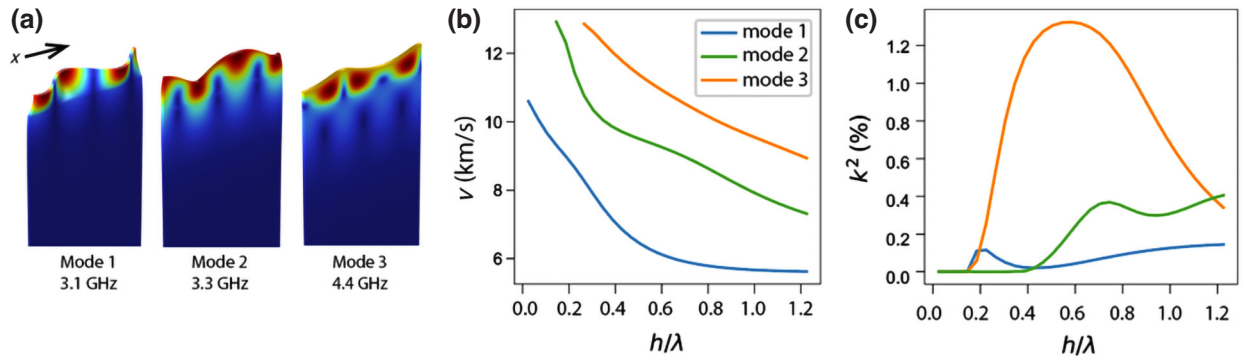


FIG. 7. (a) The three fundamental modes and their frequencies for $\lambda = 2.4 \mu\text{m}$. (b) The phase velocity of the AlN/diamond SAW (free) as a function of AlN thickness and wavelength ratio. (c) The k^2 of the AlN/diamond SAW as a function of AlN thickness and wavelength ratio. Mode 1 is Rayleigh and has the highest k^2 , where $h \approx 0.55\lambda$ and $k^2 \approx 1.2\%$.

domain. We can obtain the single-phonon Rabi rate: $g = \text{strain} \times d/\sqrt{n}$, where d is the strain susceptibility of the spin, normalized by the number of phonons: $n = E_{\text{total}}/hf$, with frequency $f = 4.5 \text{ GHz}$ in the ridge case. The susceptibility is approximately 100 THz/strain for the spin levels of the SiV, depending on the symmetry of the strain [21] and also the spin level splitting, which can be tuned by an external magnetic field [21]. We calculate the coupling rate for a [111] SiV 100 nm below the diamond surface, where the SiV is in the middle of the waveguide Rayleigh mode, as shown in Fig. 6(b). The single-phonon Rabi is calculated to be $g = 12 - 15 \text{ kHz}$. Similarly for the suspended mode, the single-phonon coupling rate to the spin is $g = 15 - 20 \text{ kHz}$ for the Rayleigh mode. This coupling is larger because the mode is more confined than for the ridge waveguide.

To compare to previous SAW works [12,23], the figure of merit is how large the Rabi rate can be while the SiV is driven with a small input power. Assume an input power of 1 mW and a transmission of -20 dB for the ridge waveguide, as measured. We add another -10 dB per port insertion loss from wire bonding and other connection losses for a realistic setup. The power of a single phonon is $p_0 = hf/t_p = 5.96 \times 10^{-17} \text{ W}$, where t_p , the duration of the phonon, is 50 ns, as calculated from the measured 10–20 MHz bandwidth in a typical ridge device, and $f = 4.5 \text{ GHz}$. Assume 1% (k^2) of the power delivered to the waveguide is converted to the phonons, so the number of phonons in the waveguide is $n = 1.68 \times 10^{11}$, and the corresponding Rabi rate is $\sqrt{ng} = 5.5 \text{ GHz}$, which is more than 2 orders of magnitude faster than the

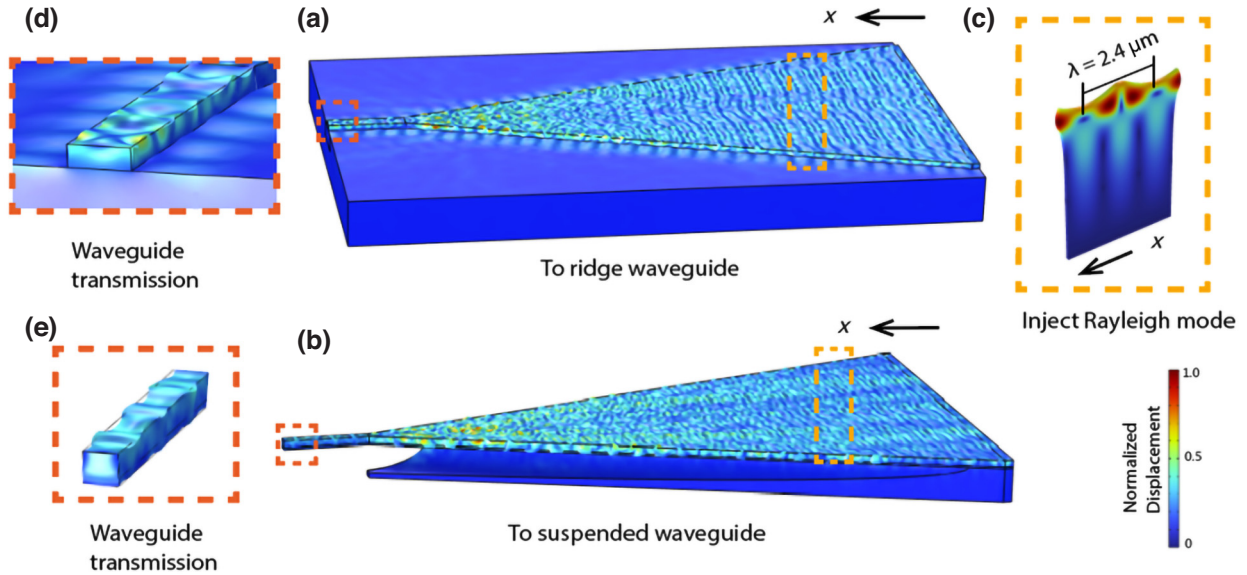


FIG. 8. Simulation of the tapering loss in the ridge and suspended devices. (a) Ridge-waveguide SAW transmission simulation domain. Normalized displacement is plotted. (b) Suspended waveguide SAW transmission simulation domain. (c) Rayleigh mode that is injected from the taper side. (d) An enlarged view of the ridge-waveguide side where the transmission is measured. (e) An enlarged view of the suspended waveguide side.

experimentally measured values in previous SAW works with the same power. The Rabi rate scales with the square root of the input power. Therefore, in practice, driving the SiV in this waveguide geometry requires much less power than 1 mW.

APPENDIX D: SIMULATING TAPERING LOSS

The taper is simulated to provide an estimate for the coupling efficiency in both the ridge and suspended device, as shown in Fig 8. The Rayleigh mode is injected into the coupling region, and the transmitted energy is measured at the waveguide cross section. The coupling efficiency for the ridge waveguide is 34.6%, which converts to a $-4.61 \times 2 = -9.22$ dB in transmission. The coupling efficiency for the suspended waveguide is 9.57%, which converts to a $-10.2 \times 2 = -20.4$ dB in transmission.

The theoretical max transmission is -6 dB since the IDT is bidirectional. The impedance is approximately 170Ω , which contributes -1.6 dB. Therefore, for the ridge device, the theoretical transmission is -16.8 dB, which is close to the measured -22.4 dB. The rest comes extra IDT loss and propagation loss. For the suspended devices, the theoretical transmission is -28.0 dB. Compared to the ridge case, the extra loss is likely due to the fabrication imperfection introduced by undercutting.

- [1] S. Gong, R. Lu, Y. Yang, L. Gao, and A. E. Hassanien, Microwave acoustic devices: Recent advances and outlook, *IEEE J. Microwaves* **1**, 601 (2021).
- [2] C. Campbell, *Surface Acoustic Wave Devices and Their Signal Processing Applications* (Elsevier, 2012).
- [3] P. Delsing, *et al.*, The 2019 surface acoustic waves roadmap, *J. Phys. D: Appl. Phys.* **52**, 353001 (2019).
- [4] P. Arrangoiz-Arriola, E. A. Wollack, Z. Wang, M. Pechal, W. Jiang, T. P. McKenna, J. D. Witmer, R. Van Laer, and A. H. Safavi-Naeini, Resolving the energy levels of a nanomechanical oscillator, *Nature* **571**, 537 (2019).
- [5] E. A. Wollack, A. Y. Cleland, R. G. Gruenke, Z. Wang, P. Arrangoiz-Arriola, and A. H. Safavi-Naeini, Quantum state preparation and tomography of entangled mechanical resonators, *Nature* **604**, 463 (2022).
- [6] U. von Lüpke, Y. Yang, M. Bild, L. Michaud, M. Fadel, and Y. Chu, Parity measurement in the strong dispersive regime of circuit quantum acoustodynamics, *Nat. Phys.* **18**, 794 (2022).
- [7] Nathan R. A. Lee, Yudan Guo, Agnetta Y. Cleland, E. Alex Wollack, Rachel G. Gruenke, Takuma Makiyara, Zhaoyou Wang, Taha Rajabzadeh, Wentao Jiang, Felix M. Mayor, Patricio Arrangoiz-Arriola, Christopher J. Sarabalis, and Amir H. Safavi-Naeini, Strong dispersive coupling between a mechanical resonator and a fluxonium superconducting qubit, <http://arxiv.org/abs/2304.13589>.
- [8] L. R. Sletten, B. A. Moores, J. J. Viennot, and K. W. Lehnert, Resolving phonon Fock states in a multimode cavity with a double-slit qubit, *Phys. Rev. X* **9**, 021056 (2019).
- [9] S. Meesala, S. Wood, D. Lake, P. Chiappina, C. Zhong, A. D. Beyer, M. D. Shaw, L. Jiang, and O. Painter, Non-Classical microwave-optical photon pair generation with a chip-scale transducer, <http://arxiv.org/abs/2303.17684>.
- [10] H. Zhao, A. Bozkurt, and M. Mirhosseini, Electro-optic transduction in silicon via GHz-frequency nanomechanics, arXiv Preprint [arXiv:2210.13549](https://arxiv.org/abs/2210.13549) (2022).
- [11] P. Ouartchaiyapong, K. W. Lee, B. A. Myers, and A. C. B. Jayich, Dynamic strain-mediated coupling of a single diamond spin to a mechanical resonator, *Nat. Commun.* **5**, 4429 (2014).
- [12] S. Maity, L. Shao, S. Bogdanović, S. Meesala, Y.-I. Sohn, N. Sinclair, B. Pingault, M. Chalupnik, C. Chia, L. Zheng, K. Lai, and M. Lončar, Coherent acoustic control of a single silicon vacancy spin in diamond, *Nat. Commun.* **11**, 193 (2020).
- [13] D. A. Golter, T. Oo, M. Amezcua, K. A. Stewart, and H. Wang, Optomechanical quantum control of a nitrogen-vacancy center in diamond, *Phys. Rev. Lett.* **116**, 143602 (2016).
- [14] S. J. Whiteley, Gary Wolfowicz, Christopher P. Anderson, Alexandre Bourassa, He Ma, Meng Ye, Gerwin Koolstra, Kevin J. Satzinger, Martin V. Holt, F. Joseph Heremans, Andrew N. Cleland, David I. Schuster, Giulia Galli, David D. Awschalom, Spin-phonon interactions in silicon carbide addressed by Gaussian acoustics, *Nat. Phys.* **15**, 490 (2019).
- [15] J. R. Dietz, B. Jiang, A. M. Day, S. A. Bhawe, and E. L. Hu, Spin-acoustic control of silicon vacancies in 4H silicon carbide, <http://arxiv.org/abs/2205.15488>.
- [16] P. Imany, Zixuan Wang, Ryan A. DeCrescent, Robert C. Boutelle, Corey A. McDonald, Travis Autry, Samuel Berweger, Pavel Kabos, Sae Woo Nam, Richard P. Mirin, and Kevin L. Silverman, Quantum phase modulation with acoustic cavities and quantum dots, *Optica* **9**, 501 (2022).
- [17] R. Manenti, A. F. Kockum, A. Patterson, T. Behrle, J. Rahamim, G. Tancredi, F. Nori, and P. J. Leek, Circuit quantum acoustodynamics with surface acoustic waves, *Nat. Commun.* **8**, 975 (2017).
- [18] K. J. Satzinger, Y. P. Zhong, H.-S. Chang, G. A. Peairs, A. Bienfait, Ming-Han Chou, A. Y. Cleland, C. R. Conner, É. Dumur, J. Grebel, I. Gutierrez, B. H. November, R. G. Povey, S. J. Whiteley, D. D. Awschalom, D. I. Schuster, and A. N. Cleland, Quantum control of surface acoustic-wave phonons, *Nature* **563**, 661 (2018).
- [19] A. Sipahigil, R. E. Evans, D. D. Sukachev, M. J. Burek, J. Borregaard, M. K. Bhaskar, C. T. Nguyen, J. L. Pacheco, H. A. Atikian, C. Meuwly, R. M. Camacho, F. Jelezko, E. Bielejec, H. Park, M. Lončar, and M. D. Lukin, An integrated diamond nanophotonics platform for quantum-optical networks, *Science* **354**, 847 (2016).
- [20] P.-J. Stas *et al.*, Robust Multi-Qubit Quantum Network Node with Integrated Error Detection, <http://arxiv.org/abs/2207.13128>.
- [21] S. Meesala, Young-Ik Sohn, Benjamin Pingault, Linbo Shao, Haig A. Atikian, Jeffrey Holzgrafe, Mustafa Gündoğan, Camille Stavrakas, Alp Sipahigil, Cleaven Chia, Ruffin Evans, Michael J. Burek, Mian Zhang, Lue Wu, Jose L. Pacheco, John Abraham, Edward Bielejec, Mikhail D. Lukin, Mete Atatüre, and Marko Lončar, Strain

- engineering of the silicon-vacancy center in diamond, *Phys. Rev. B* **97**, 205444 (2018).
- [22] Y.-I. Sohn *et al.*, Controlling the coherence of a diamond spin qubit through its strain environment, *Nat. Commun.* **9**, 2012 (2018).
- [23] S. Maity, B. Pingault, G. Joe, M. Chalupnik, D. Assumpção, E. Cornell, L. Shao, and M. Lončar, Mechanical control of a single nuclear spin, *Phys. Rev. X* **12**, 011056 (2022).
- [24] M. E. Levinshtein, S. L. Rumyantsev, and M. S. Shur, *Properties of Advanced Semiconductor Materials: GaN, AlN, InN, BN, SiC, SiGe* (John Wiley & Sons, 2001).
- [25] C. M. Flannery, M. D. Whitfield, and R. B. Jackman, Acoustic wave properties of CVD diamond, *Semicond. Sci. Technol.* **18**, S86 (2003).
- [26] L. Shao, S. W. Ding, Y. Ma, Y. Zhang, N. Sinclair, and M. Lončar, Thermal modulation of gigahertz surface acoustic waves on lithium niobate, *Phys. Rev. Appl.* **18**, 054078 (2022).
- [27] F. M. Mayor, W. Jiang, C. J. Sarabalis, T. P. McKenna, J. D. Witmer, and A. H. Safavi-Naeini, Gigahertz phononic integrated circuits on thin-film lithium niobate on sapphire, *Phys. Rev. Appl.* **15**, 014039 (2021).
- [28] W. Fu, Z. Shen, Y. Xu, C.-L. Zou, R. Cheng, X. Han, and H. X. Tang, Phononic integrated circuitry and spin-orbit interaction of phonons, *Nat. Commun.* **10**, 2743 (2019).
- [29] L. Shao *et al.*, Phononic band structure engineering for high-Q gigahertz surface acoustic wave resonators on lithium niobate, *Phys. Rev. Appl.* **12**, 014022 (2019).
- [30] Q. Liu, H. Li, and M. Li, Electromechanical Brillouin scattering in integrated optomechanical waveguides, *Optica* **6**, 778 (2019).
- [31] C. J. Sarabalis, R. Van Laer, R. N. Patel, Y. D. Dahmani, W. Jiang, F. M. Mayor, and A. H. Safavi-Naeini, Acousto-optic modulation of a wavelength-scale waveguide, *Optica* **8**, 477 (2021).
- [32] C. Chia, B. Machielse, A. Shams-Ansari, and M. Lončar, Development of hard masks for reactive ion beam angled etching of diamond, *Opt. Express* **30**, 14189 (2022).
- [33] K. Kuruma, B. Pingault, C. Chia, D. Renaud, P. Hoffmann, S. Iwamoto, C. Ronning, and M. Lončar, Coupling of a Single Tin-Vacancy Center to a Photonic Crystal Cavity in Diamond, <http://arxiv.org/abs/2105.01715>.
- [34] D. Lee, Q. Liu, L. Zheng, X. Ma, H. Li, M. Li, and K. Lai, Direct visualization of gigahertz acoustic wave propagation in suspended phononic circuits, *Phys. Rev. Appl.* **16**, 034047 (2021).
- [35] W. Jiang, C. J. Sarabalis, Y. D. Dahmani, R. N. Patel, F. M. Mayor, T. P. McKenna, R. Van Laer, and A. H. Safavi-Naeini, Efficient bidirectional piezo-optomechanical transduction between microwave and optical frequency, *Nat. Commun.* **11**, 1166 (2020).
- [36] W. Jiang, F. M. Mayor, S. Malik, R. Van Laer, T. P. McKenna, R. N. Patel, J. D. Witmer, and A. H. Safavi-Naeini, Optically heralded microwave photons, <http://arxiv.org/abs/2210.10739>.
- [37] X. Guo, N. Deegan, J. C. Karsch, Z. Li, T. Liu, R. Shreiner, A. Butcher, D. D. Awschalom, F. J. Heremans, and A. A. High, Tunable and transferable diamond membranes for integrated quantum technologies, *Nano Lett.* **21**, 10392 (2021).
- [38] S. L. N. Hermans, M. Pompili, H. K. C. Beukers, S. Baier, J. Borregaard, and R. Hanson, Qubit teleportation between non-neighbouring nodes in a quantum network, *Nature* **605**, 663 (2022).
- [39] M. J. Burek, D. Ramos, P. Patel, I. W. Frank, and M. Lončar, Nanomechanical resonant structures in single-crystal diamond, <http://arxiv.org/abs/1309.1834>.
- [40] M. J. Burek, Justin D. Cohen, Seán M. Meenehan, Nayera El-Sawah, Cleaven Chia, Thibaud Ruelle, Srujan Meesala, Jake Rochman, Haig A. Atikian, Matthew Markham, Daniel J. Twitchen, Mikhail D. Lukin, Oskar Painter, and Marko Lončar, Diamond optomechanical crystals, *Optica* **3**, 1404 (2016).