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Abstract

The high susceptibility of ultrathin two-dimensional (2D) material resonators to force and temperature makes them ideal systems for sensing applications and exploring thermomechanical coupling. Although the dynamics of these systems at high stress has been thoroughly investigated, their behavior near the buckling transition has received less attention. Here, we demonstrate that the force sensitivity and frequency tunability of 2D material resonators are significantly enhanced near the buckling bifurcation. This bifurcation is triggered by compressive displacement that we induce via thermal expansion of the devices, while measuring their dynamics via an optomechanical technique. We understand the frequency tuning of the devices through a mechanical buckling model, which allows to extract the central deflection and boundary compressive displacement of the membrane. Surprisingly, we obtain a remarkable enhancement of up to 14× the vibration amplitude attributed to a very low stiffness of the membrane at the buckling transition, as well as a high frequency tunability by temperature of more than 4.02% K⁻¹. The presented results provide insights into the effects of buckling on the dynamics of free-standing 2D materials and thereby open up opportunities for the realization of 2D resonant sensors with buckling-enhanced sensitivity.

1. Introduction

A flat mechanical plate subjected to a sufficiently high in-plane compressive stress becomes unstable, as its out-of-plane stiffness gradually reduces to zero [1]. When this happens, the plate experiences a buckling bifurcation. Even the slightest imperfection in the device, like a very small initial deformation, can determine whether the plate buckles up or downward. This high sensitivity to initial conditions offers exciting prospects, both for studying material properties [2–4] and for realizing new sensing applications [5]. Therefore there has been a growing interest for buckling in nano-electromechanical systems (NEMS) and resonators such as phononic waveguides [6], carbon nanotubes [7] and SiN_x drumheads [8], showing

reversible control of signal transmission, high sensitive switching, as well as remarkable nonlinear effects and high tunability of resonance frequencies. These properties of buckled resonators make them very suitable for applications as actuators, sensors, and energy harvesters [9, 10].

Nanomechanical resonators made of free-standing 2D materials are stiff within the plane, due to their high Young's modulus, but extremely flexible out-of-plane due to their atomic thickness [11–13]. As a result, free-standing 2D materials buckle at relatively low compressive stress values and thereby present an ideal platform for studying the buckling bifurcation in nanoscale systems. In fact, the buckling bifurcation provides a sensitive method to determine the bending rigidity of 2D materials [2, 14]. However,

Table 1. Characteristics of the fabricated devices including radius R , thickness h , Young's modulus E , Poisson ratio ν , mass density ρ , initial resonance frequency $f_0(T_0)$, temperature at turning point T_t , resonance frequency at turning point f_t , central deflection without boundary displacement loading z_{free} , initial displacement U_0 , and pre-strain ϵ_0 . D1 and D2 are from the same nanoflake (see figure 1(a)).

	R (μm)	h (nm)	E (GPa)	$f_0(T_0)$ (MHz)	T_t (K)
D1	4	33.9	69.9	5.89	302.0
D2	4	33.9	70.3	5.52	303.0
D3	3	34.5	93.1	11.18	307.5
	f_t (MHz)	z_{free} (nm)	U_0 (nm)	$\epsilon_0 \times 10^{-5}$	
D1	5.53	20.1	0.08	1.84	
D2	3.97	6.2	0.08	1.99	
D3	6.89	4.3	0.04	1.32	

most of the work on 2D NEMS resonators has focused on flat 2D mechanical resonators under tensile stress, because these can be more reproducibly fabricated [15, 16]. Moreover, the experimental detection of the buckling bifurcation in 2D NEMS remains difficult, as it requires a methodology to induce symmetric in-plane compression in suspended 2D materials while measuring their mechanical motion with high spatial resolution.

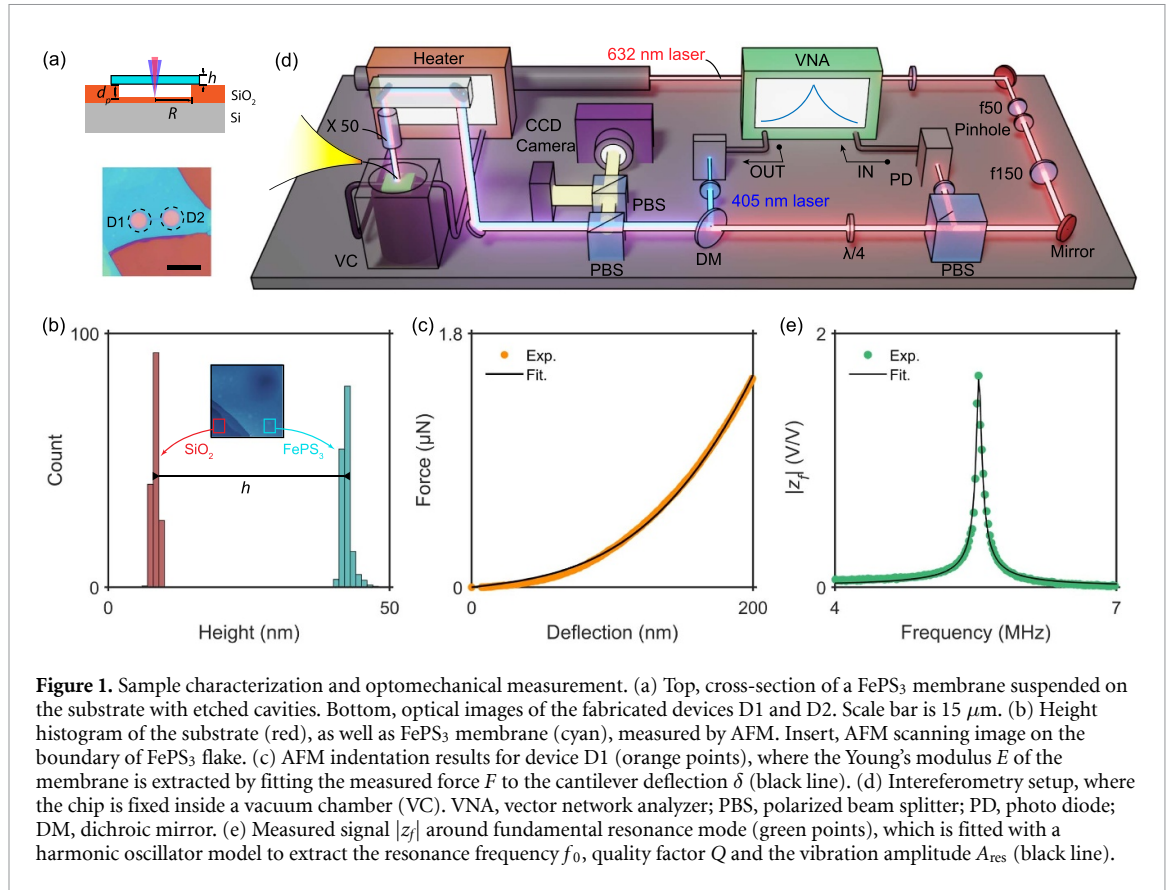
In this work, we study the effect of the buckling bifurcation on the dynamics of optothermally driven nanomechanical resonators made of FePS₃ membranes. By varying temperature, the membranes expand, causing a compressive displacement that triggers the membranes to deflect out-of-plane. Interestingly, this buckling bifurcation does not only cause a large change in the temperature-dependent resonance frequency, but also gives rise to a significant enhancement of vibration amplitude of the resonators when driven on-resonance. To account for these observations and relate them to the device parameters, we fit a mechanical buckling model to the experiments that quantifies central membrane deflection and boundary compressive displacement of the membrane. Based on the model we attribute the force response to a significantly reduced out-of-plane stiffness at buckling transition. The large frequency tuning and high responsivity to forces of 2D resonators near the buckling bifurcation might be utilized to enhance sensitivity in future designs of 2D NEMS devices like microphones and pressure sensors.

2. Fabrication and methodology

We fabricated 2D nanomechanical resonators by transferring exfoliated 2D flakes over etched circular cavities with a depth of $d_p = 285$ nm and varying radius R in a Si/SiO₂ substrate (Methods). In total, we made three FePS₃ devices D1–D3. Figure 1(a) shows a schematic cross-section and a top view (optical microscope) of the fabricated devices D1 and D2 with $R = 4$ μm . Using tapping mode atomic force microscopy (AFM), we measure the height difference

between the membrane and the Si/SiO₂ substrate. As figure 1(b) shows, we find a membrane thickness h of 33.9 nm for devices D1 and D2. To determine the Young's modulus E of the resonators, we indent the membrane centre by an AFM cantilever while measuring its deflection [17]. We fit the applied force F versus indentation δ , as depicted in figure 1(c) (orange points), to a model for point-force loading of a circular plate given by $F = (\frac{16\pi D}{R^2}\delta) + n_0\pi\delta + Ehq^3(\frac{\delta^3}{R^2})$, where $D = Eh^3/(12(1-\nu^2))$ is the bending rigidity of the membrane, ν is Poisson ratio, $n_0 = Eh\epsilon_0/(1-\nu)$ is the pre-tension in the membrane, and ϵ_0 is the built-in strain. From the fit (black line, figure 1(c)) we extract $E = 69.9$ GPa for device D1. The AFM measurements on devices D2 and D3 can be found in SI section 3. The extracted Young's moduli of all devices are listed in table 1 and are similar to values reported in the literature [18].

To probe the thermodynamic properties of the fabricated devices, we use a laser interferometer (see methods) [19, 20]. As shown in figure 1(d), we place the samples in a vacuum chamber with a pressure below 10^{-5} mbar during the measurements. A power-modulated diode laser ($\lambda = 405$ nm) photothermally actuates the resonator, while the reflection of a He-Ne laser ($\lambda = 632$ nm) from the cavity with the suspended membrane captures its motion. The reflection is measured by a photodetector (PD) and processed by a Vector Network Analyzer (VNA) and then converted to the response amplitude $|z_f|$ of the resonator in the frequency domain. Figure 1(e) shows the measured frequency response around the fundamental resonance (green points) and a fit to a harmonic oscillator model (black line), given by $|z_f| = \frac{A_{\text{res}}f_0^2}{Q\sqrt{(f_0^2 - f^2)^2 + (f_0f/Q)^2}}$, where f_0 is resonance frequency, A_{res} is the vibration amplitude at resonance and Q is quality factor. Here, we extract $f_0 = 5.57$ MHz, $Q = 195.93$ and $A_{\text{res}} = 1.64$ VV⁻¹ for device D1. We will now outline how the characteristics of the resonance frequency (f_0 and A_{res}) can be used to provide information about the temperature dependent properties of 2D material resonators, in particular near the buckling bifurcation.



3. Results and discussion

Figure 2(a) shows the measured $|z_f|$ as a function of actuation frequency and temperature (in the range from 300 to 316 K) for device D1. Interestingly, the resonance frequencies, including fundamental mode (indicated by the blue arrows) and second mode, first decrease and then increase as temperature increases, with a turning point at temperature $T_t = 302$ K (see figure 2(b)). Similarly, the measured vibration amplitude A_{res} for device D1 also reaches to its maximum at T_t (see figure 2(c)). These behaviors are also experimentally observed in devices D2 and D3 (see SI section 3). We attribute the turning of f_0 versus T to the mechanical buckling of the nanomechanical resonators under critical compressive loading,

which has been reported before in carbon nanotube resonators [7] and arch MEMS devices [21]. In fact, the bulk thermal expansion coefficients (TEC), α_m , of the measured FePS₃ membranes in this work is much larger than the TEC α_{Si} of the Si/SiO₂ substrate. Hence, heating induces compressive displacement in the resonators and buckling is a natural consequence.

Due to the buckling, we cannot use the standard equation for the resonance frequency of a pre-tensioned plate or membrane for further analysis. Therefore, we use a mechanical buckling model for clamped circular plate, as illustrated in figure 2(d). Using a Galerkin method from literature [22, 23], we obtain an expression of f_0 under thermally induced compressive displacement:

$$f_0(T) = \frac{10.33h}{\pi d^2} \sqrt{\frac{E}{3\rho(1-\nu^2)} \left(1 + \beta(1-\nu^2) \frac{3z^2 - z_{free}^2}{h^2} + \frac{3}{8}(1+\nu) \frac{Ud}{h^2} \right)}, \quad (1)$$

where U is the in-plane edge displacement of the plate, ρ is the mass density, z is the central deflection of the plate, z_{free} is the central deflection of free plate without loading (when $U = 0$), and β is a fitting constant and equal to 0.52 when $\nu = 0.304$

(see SI section 1). Both U and z depend on temperature T . The details of derivation of equation (1) can be found in SI section 1. In contrast to the standard equation for the resonance frequency of a pre-bending plate [24], we now find that not only

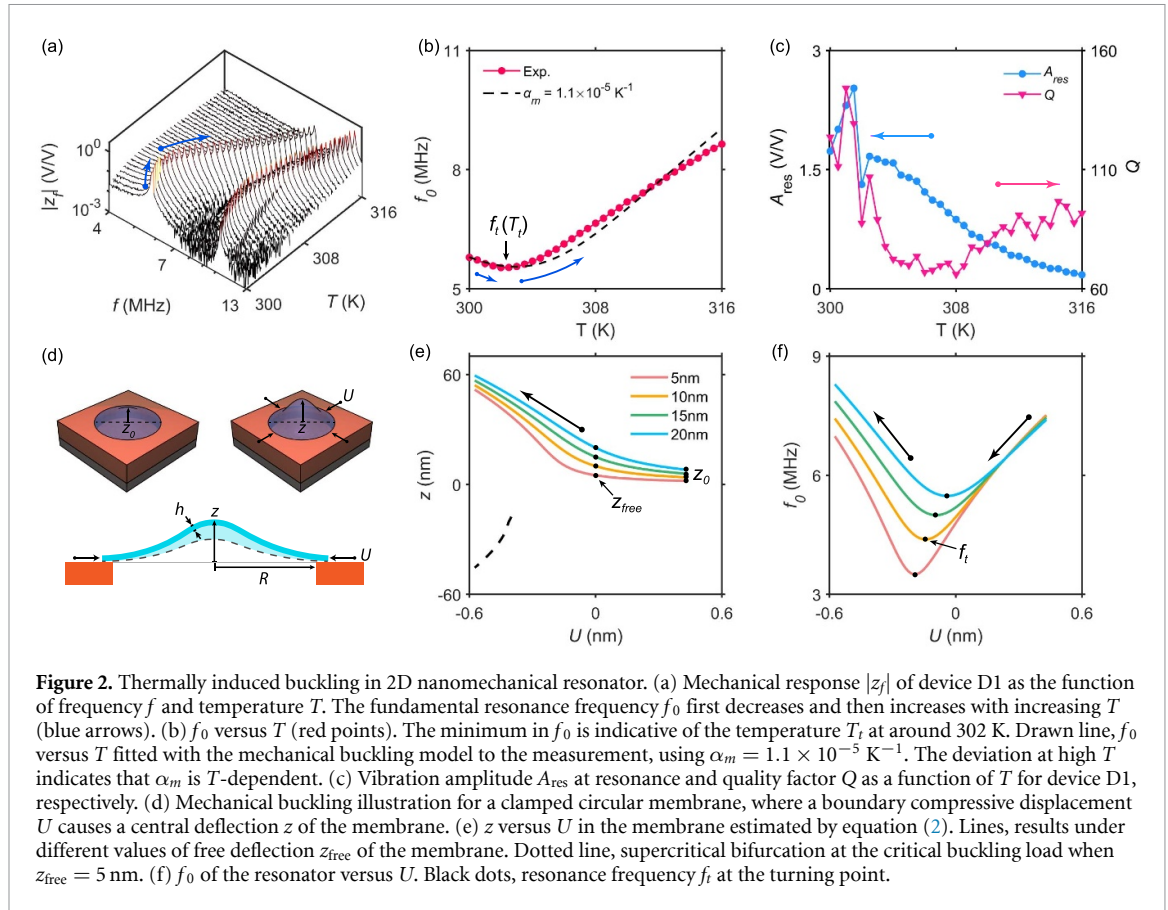


Figure 2. Thermally induced buckling in 2D nanomechanical resonator. (a) Mechanical response $|z_f|$ of device D1 as the function of frequency f and temperature T . The fundamental resonance frequency f_0 first decreases and then increases with increasing T (blue arrows). (b) f_0 versus T (red points). The minimum in f_0 is indicative of the temperature T_i at around 302 K. Drawn line, f_0 versus T fitted with the mechanical buckling model to the measurement, using $\alpha_m = 1.1 \times 10^{-5} \text{ K}^{-1}$. The deviation at high T indicates that α_m is T -dependent. (c) Vibration amplitude A_{res} at resonance and quality factor Q as a function of T for device D1, respectively. (d) Mechanical buckling illustration for a clamped circular membrane, where a boundary compressive displacement U causes a central deflection z of the membrane. (e) z versus U in the membrane estimated by equation (2). Lines, results under different values of free deflection z_{free} of the membrane. Dotted line, supercritical bifurcation at the critical buckling load when $z_{\text{free}} = 5 \text{ nm}$. (f) f_0 of the resonator versus U . Black dots, resonance frequency f_t at the turning point.

the bending rigidity determine $f_0(T)$, but also the thermally-induced boundary displacement U and the center deflection z of the membrane.

To find the relation between U and z , we consider a uniformly-clamped plate as depicted in figure 2(d). By studying the static state of the plate using Gakerkin method (see more details in SI section 1), we obtain an analytic solution:

$$\frac{32}{3} \left(1 - \frac{z_{\text{free}}}{z}\right) - 10.7\beta(1 - \nu^2) \left(\frac{z_{\text{free}}^2 - z^2}{h^2}\right) + 4(1 + \nu) \frac{Ud}{h^2} = 0. \quad (2)$$

Therefore, the change of central deflection z of the plate versus U as buckling happens can be extracted from equation (2). We further use COMSOL simulation method to obtain z and f_0 as the function of U , showing good agreements with the analytical solution obtained from equations (1) and (2) (see figure S2). By substituting the parameters $R = 4 \mu\text{m}$, $E = 69.9 \text{ GPa}$, $h = 33.9 \text{ nm}$, $\rho = 3.375 \text{ gcm}^{-3}$ and $\nu = 0.304$ into equation (2), we can evaluate z as a function of U for different z_{free} . As plotted in figure 2(e), z gradually increases with increasing U . The dotted black line in figure 2(e) represents a supercritical bifurcation at the critical buckling load when $z_{\text{free}} = 5 \text{ nm}$. This physically indicates an unstable equilibrium that the plate will either buckle up or

down when it is slightly perturbed. For nonzero z_{free} in this work, the 2D membrane always buckles in the direction of its pre-deflection.

In order to investigate the effect of buckling on the resonance frequency f_0 , we substitute the relation between z and U into equation (1). This results in a relation between f_0 and z_{free} , as plotted in figure 2(f). When decreasing the displacement U by compression, f_0 reduces to a minimal value (the turning point) and then starts to increase. At this turning point, the minimum resonance frequency f_t of the resonator is reached (marked as dots in figure 2(f)). Both the experimental curves in figure 2(a) and the theoretical curves in figure 2(f) clearly show this frequency minimum, which we take as qualitative evidence for the occurrence of buckling in the 2D resonators.

Let us now quantify U and z as a function of T for device D1, using a model that follows the flow chart depicted in figure 3(a). First, we need to determine the value of z_{free} in the mechanical buckling model. For this, we use the specific feature in the measured f_0 versus T data, which is $\frac{df_0}{dT}|_{T=T_i} = 0$ at the turning point (figure 2(b)). Assuming the Young's modulus of the membrane remains constant within the probed temperature range [25], z_{free} can be determined by f_t (see derivation in SI section 2). Here, using the parameters in table 1 and the measured value of $f_t(T_i) = 5.53 \text{ MHz}$, we extract $z_{\text{free}} = 20.1 \text{ nm}$ for device D1.

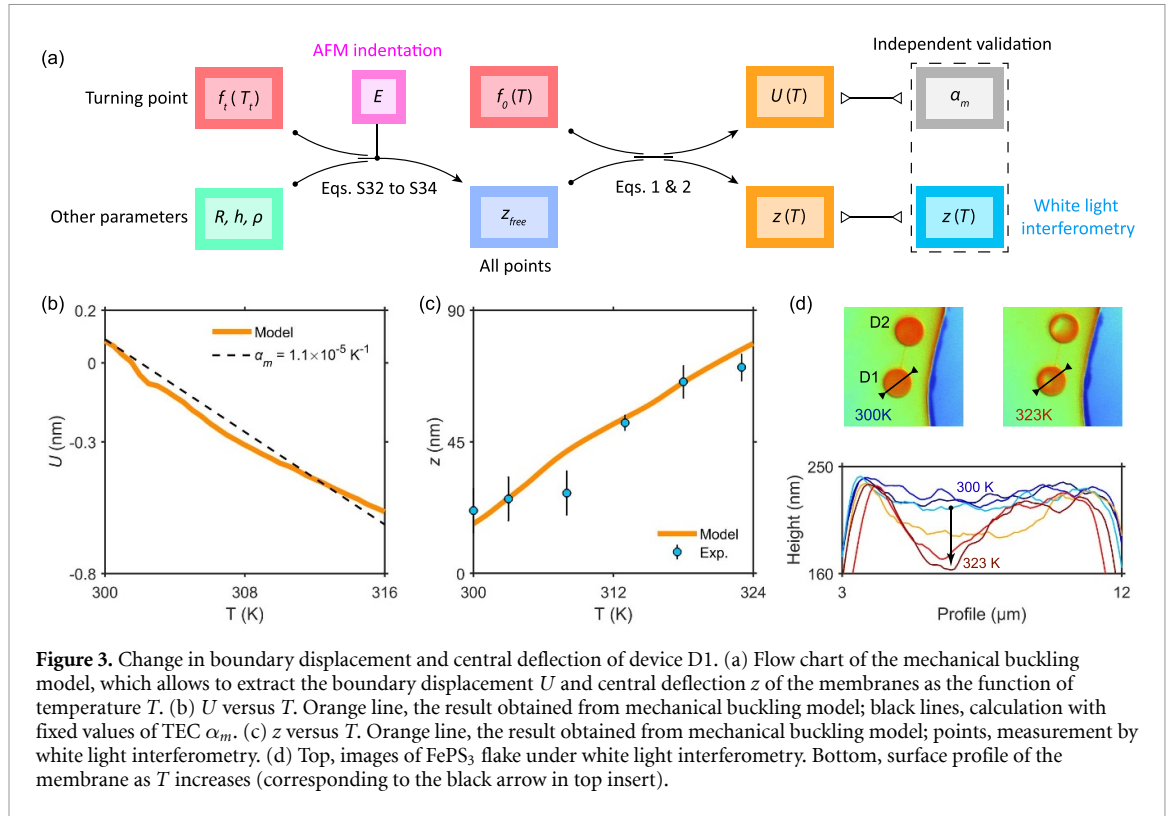


Figure 3. Change in boundary displacement and central deflection of device D1. (a) Flow chart of the mechanical buckling model, which allows to extract the boundary displacement U and central deflection z of the membranes as the function of temperature T . (b) U versus T . Orange line, the result obtained from mechanical buckling model; black lines, calculation with fixed values of TEC α_m . (c) z versus T . Orange line, the result obtained from mechanical buckling model; points, measurement by white light interferometry. (d) Top, images of FePS₃ flake under white light interferometry. Bottom, surface profile of the membrane as T increases (corresponding to the black arrow in top insert).

By substituting the obtained z_{free} into equations (1) and (2), we further extract U and z as a function of T from the measured f_0 at each temperature for device D1. In figure 3(b), we observe that the compressive displacement U becomes more than 10 times larger than its initial tensile value $U_0 = 0.08$ nm (table 1) by heating the membrane by only 16 K. To validate the extracted $U(T)$, we determine the TEC α_m of the membrane. Using the TEC of the substrate α_{Si} , we can use the relation $\frac{1}{R} \frac{dU}{dT} = -(\alpha_m - \alpha_{Si})$ to determine α_m [18]. We thus fit this relation to the obtained ϵ as shown in figure 3(c) (orange line) and find α_m is approximately $1.1 \times 10^{-5} \text{ K}^{-1}$, which is in good agreement with values reported in the literature for FePS₃ [18, 26]. The fitting deviation for $f_0(T)$ in figure 2(b) is thus attributed to the temperature dependence of α_m of FePS₃, or the irregular deflection of the membrane as buckling happens.

To experimentally validate the extracted $z(T)$ from the buckling model in figure 3(c), we use a white light interferometer to image the surface profile of the suspended FePS₃ membranes as a function of temperature. As shown in figure 3(d), we observe from the height profiles (black arrows, top panel) that the membrane deformation increases as T goes up (bottom panel). As a measure for $z(T)$, we take the difference between the maximum and minimum height for two height profiles and take the average value. As plotted in figure 3(c), the extracted $z(T)$ (points) for device D1 quantitatively matches the estimated $z(T)$ (orange line), which confirms that device D1 exhibits

mechanical buckling. In addition, the total strain in the FePS₃ membrane also changes from the initial tensile strain to a strong compressive strain. From the obtained $U_0 = 0.08$ nm and $z_{free} = 20.1$ nm, we extract the initial strain $\epsilon_0 = 1.84 \times 10^{-5}$ for device D1 using equation (S26) and the relation $N_r = \frac{Eh\epsilon}{1-\nu}$. All obtained ϵ_0 for devices D1 to D3 are listed in table 1.

We now focus on the vibration amplitude of the fundamental mode of the membrane. As shown in figure 2(c), we observe a remarkable enhancement of up to $14 \times$ the vibration amplitude A_{res} at the turning point $T_t = 302$ K. This is attributed to the reduction of out-of-plane stiffness, $k_{eff} = m_{eff}(2\pi f_0)^2$, of the membrane near the buckling transition. Furthermore, we also find the thermally induced buckling in devices D2 and D3 during optomechanical measurements (see SI section 3). We quantify the frequency turning of these devices with the mechanical buckling model, and extract their z_0 , ϵ_0 and ϵ_t as listed in table 1. Similar to what was observed for device D1 (figure 2(c)), A_{res} for devices D2 and D3 also show more than 14 times enhancements near the buckling transition (figure S6). However, although the quality factor $Q(T)$ reaches to its maximum at turning point for device D1, we observe completely different results of $Q(T)$ for devices D2 and D3. Since Q is related to the TEC and thermal properties of 2D materials [27], it is of interest to investigate the T -tuning Q of buckled 2D resonators in future work.

The implications of the observed phenomena extend beyond FePS₃ resonators. Even for 2D

materials with a negative TEC such as graphene, buckling might occur if it is cooled down and the initial tensile stress is low enough. A key assumption in equations (1) and (2) is a uniform compressive force at the boundary of the membrane and a constant Young's modulus over the measured temperature range. In reality, inhomogeneities due to uneven adhesion between membrane and substrate could lead to multiple smaller corrugations and wrinkles superimposed in the membrane when buckling occurs. This potential limitation, which we did not observe for the devices studied in this work, deserves future study as the buckled mode shape as well as the Young's modulus depend on it [28, 29]. Possibly, the experimental quantification of the Young's modulus for each device with AFM, as we did in figure 1(c), compensates for some of the effects of corrugations and wrinkles on the buckling bifurcation.

Despite the fact that the temperature-dependence of resonance frequency has been investigated in earlier works on 2D membranes [30–32], mechanical buckling has not been reported yet. It seems that one study on MoS₂ resonators might have almost reached the buckling point ($\frac{df_0}{dT} \rightarrow 0$) at around 373 K [30]. In this work it was relatively straightforward to reach the buckling bifurcation due to the large TECs of the selected 2D materials. It is of interest to speculate on the ultimate limits of buckling induced resonance frequency decrease. As indicated in figure 2(d), theoretically it might be possible to have the resonance frequency approaching zero for a deflection $z_{\text{free}} = 0$ nm. However, in practice it will be difficult to reach that point. Nevertheless, by making the membranes flatter and with low pre-stress, the zero resonance frequency might be approached, which allows for an extremely high tunability and therefore a high force, stress and temperature sensitivity of f_0 near the minimum f_i . For such flat and low stress membranes, we expect the bending rigidity of 2D materials to dominate the performance and resonance frequency versus temperature curve near the buckling bifurcation point.

Also from an application perspective, the thermally induced buckling in 2D nanomechanical resonators deserves further exploration. First, the frequency tuning with temperature is considerable. As shown in figure 4, we obtain a tunability, $\Delta f_0/(f_0 \Delta T)$, more than $4.02\% \text{ K}^{-1}$ for device D1, which is at least 2.3 times higher than reported in earlier studies [30, 31, 33]. The slope of frequency tuning for device D1 is $\Delta f_0/(\Delta T) = 194.3 \text{ kHz K}^{-1}$, which, when considering an accuracy of 1 kHz in determining f_0 , results in a temperature resolution of 5.1 mK. This value is comparable to state-of-the-art temperature sensors [34] and thus highlights the application buckled 2D resonators as bolometer [35] and NEMS resonant infrared detector [36]. Furthermore, precise control over the buckling bifurcation can be obtained by tailoring the initial deflection of the membrane

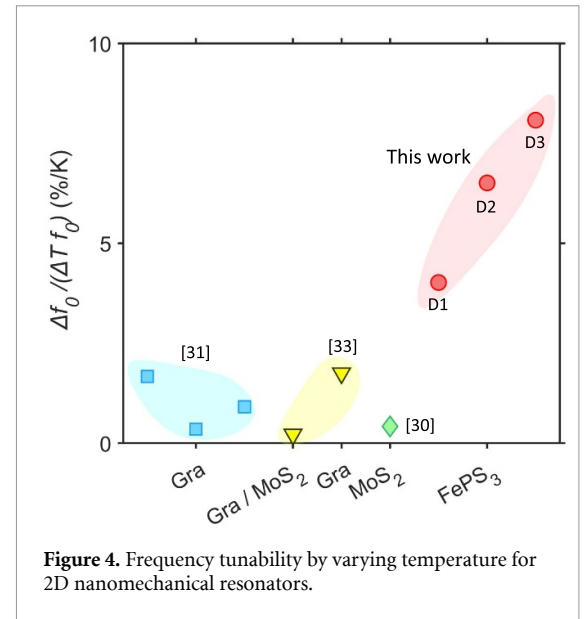


Figure 4. Frequency tunability by varying temperature for 2D nanomechanical resonators.

by applying, among others, electrostatic gating on the resonators [12], a gas pressure difference [37], or straining the resonators by MEMS actuators [38].

4. Conclusion

In summary, we reported the experimental observation of thermally-induced buckling in 2D nanomechanical resonators made of suspended FePS₃ membranes. Using an optomechanical method, we probed their dynamic responses as a function of temperature. A mechanical buckling model was developed to explain the observed large turning of the resonance frequency with temperature, which allows to determine the boundary compressive displacement and center deflection of the fabricated devices. Using white light interferometer, we independently validated the extracted deflection of the membrane versus temperature from buckling model. We found an enhancement of up to $14\times$ vibration amplitude near buckling bifurcation, which we attributed to the decrease in out-of-plane stiffness of the membrane. The gained insight not only advances the fundamental understanding of buckling bifurcation membranes made of 2D materials, but also enables pathways for buckling-enhanced designs and applications such as temperature detectors, thermoelectric and NEMS devices.

5. Methods

Sample Fabrication. A Si wafer with 285 nm dry SiO₂ is spin coated with positive e-beam resist and exposed by electron-beam lithography. Afterwards, the SiO₂ layer without protection is completely etched using CHF₃ and Ar plasma in a reactive ion etcher. The edges of cavities are examined to be well-defined by scanning electron microscopy and AFM. After resist removal, FePS₃ nanoflakes are exfoliated by Scotch tape, and then separately transferred onto the

substrate at room temperature through a deterministic dry stamping technique. More details about the fabrication of etched substrate with circular cavities, as well as the Scotch tape transfer method can be found in [13]. Detailed descriptions of the FePS₃ crystal growth and characterization is reported in earlier work [39]. We choose FePS₃ flakes due to its large value of TEC, which allows to experimentally observe the buckling phenomenon of 2D resonators within a small range of temperature increase.

Laser Interferometry Setup. We present temperature-dependent optomechanical measurements in a laser interferometry setup [18]. The fabricated devices is fixed on a sample holder inside the vacuum chamber. A PID heater and a temperature sensor are connected with the sample holder, which allows to precisely monitor and control the temperature sweeping. A piezo-electric actuator below the sample holder is used to optimize the X-Y position of the sample to maintain both the blue and red laser in the center of the 2D resonators. We use a red and blue laser power of 0.9 and 0.13 mW respectively. Note we verified that the resonators vibrate in linear regime and the temperature raise due to self-heating is negligible [40]. The real picture of experimental setup on the optical table can be found in figure S8.

Data availability statement

All data that support the findings of this study are included within the article (and any supplementary files).

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Author contribution

H L, P G S and G J V conceived the experiments. H L and G B performed the optomechanical measurements with heating control system. H L fabricated and

inspected the samples. C B C synthesized and characterized the FePS₃ crystals. H L, G J V, P G S and H S J v d Z analyzed and modeled the experimental data. H S J v d Z and P G S supervised the project. The paper was jointly written by all authors with a main contribution from H L. All authors discussed the results and commented on the paper.

Conflict of interest

The authors declare no competing financial interest.

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References

- [1] Hu N and Burgueño R 2015 Buckling-induced smart applications: recent advances and trends *Smart Mater. Struct.* **24** 063001
- [2] Lindahl N, Midtvedt D, Svensson J, Nerushev O A, Lindvall N, Isacson A and Campbell E E 2012 Determination of the bending rigidity of graphene via electrostatic actuation of buckled membranes *Nano Lett.* **12** 3526–31
- [3] Le Doussal P and Radzihovsky L 2021 Thermal buckling transition of crystalline membranes in a field *Phys. Rev. Lett.* **127** 015702
- [4] Chil C, Durinck J and Coupeau C 2022 Buckling of graphene under compressive strain: DFT calculations and second generation REBO potential *Extreme Mech. Lett.* **56** 101845
- [5] El Mansouri B, Middelburg L M, Poelma R H, Zhang G Q, van Zeijl H W, Wei J, Jiang H, Vogel J G and van Driel W D 2019 High-resolution MEMS inertial sensor combining large-displacement buckling behaviour with integrated capacitive readout *Microsyst. Nanoeng.* **5** 1–14
- [6] Kim S, Bunyan J, Ferrari P F, Kanj A, Vakakis A F, Van Der Zande A M and Tawfik S 2021 Buckling-mediated phase transitions in nano-electromechanical phononic waveguides *Nano Lett.* **21** 6416–24
- [7] Rechnitz S, Tabachnik T, Shlafman S, Shlafman M and Yaish Y E 2022 DC signature of snap-through bistability in carbon nanotube mechanical resonators *Nano Lett.* **22** 7304–10
- [8] Kanj A, Ferrari P F, van der Zande A M, Vakakis A F and Tawfik S 2022 Ultra-tuning of nonlinear drumhead MEMS resonators by electro-thermoelastic buckling (arXiv:2210.06982)
- [9] Xia J, Farrell P E and Castro S G 2020 Nonlinear bifurcation analysis of stiffener profiles via deflation techniques *Thin-Walled Struct.* **149** 106662
- [10] Harne R L and Wang K 2013 A review of the recent research on vibration energy harvesting via bistable systems *Smart Mater. Struct.* **22** 023001
- [11] Xu B et al 2022 Nanomechanical resonators: toward atomic scale *ACS Nano* **16** 15545–85
- [12] Steeneken P G, Dolleman R J, Davidovikj D, Alijani F and Van der Zant H S 2021 Dynamics of 2D material membranes *2D Mater.* **8** 042001
- [13] Liu H, Basuvalingam S B, Lodha S, Bol A A, van der Zant H S, Steeneken P G and Verbiest G J 2023

- Nanomechanical resonators fabricated by atomic layer deposition on suspended 2D materials *2D Mater.* **10** 045023
- [14] Iguñiz N, Frisenda R, Bratschitsch R and Castellanos-Gomez A 2019 Revisiting the buckling metrology method to determine the Young's modulus of 2D materials *Adv. Mater.* **31** 1807150
- [15] Kim S 2020 Impact of the van der Waals interface on the mechanics of 2D nanoelectromechanical systems *PhD Thesis* University of Illinois at Urbana-Champaign
- [16] Ferrari P F, Kim S and Van Der Zande A M 2021 Dissipation from interlayer friction in graphene nanoelectromechanical resonators *Nano Lett.* **21** 8058–65
- [17] Castellanos-Gomez A, Poot M, Steele G A, Van Der Zant H S, Agrañt N and Rubio-Bollinger G 2012 Elastic properties of freely suspended MoS₂ nanosheets *Adv. Mater.* **24** 772–5
- [18] Šiškins M, Lee M, Mañas-Valero S, Coronado E, Blanter Y M, van der Zant H S and Steeneken P G 2020 Magnetic and electronic phase transitions probed by nanomechanical resonators *Nat. Commun.* **11** 2698
- [19] Šiškins M, Sokolovskaya E, Lee M, Mañas-Valero S, Davidovikj D, Van Der Zant H S and Steeneken P G 2021 Tunable strong coupling of mechanical resonance between spatially separated FePS₃ nanodrums *Nano Lett.* **22** 36–42
- [20] Liu H, Lee M, Šiškins M, van der Zant H, Steeneken P and Verbiest G 2022 Tension tuning of sound and heat transport in graphene (arXiv:2204.06877)
- [21] Hajjaj A, Jaber N, Ilyas S, Alfosail F and Younis M I 2020 Linear and nonlinear dynamics of micro and nano-resonators: review of recent advances *Int. J. Non-Linear Mech.* **119** 103328
- [22] Yamaki N, Otomo K and Chiba M 1981 Non-linear vibrations of a clamped circular plate with initial deflection and initial edge displacement, part I: theory *J. Sound Vib.* **79** 23–42
- [23] Kim C and Dickinson S 1986 The flexural vibration of slightly curved slender beams subject to axial end displacement *J. Sound Vib.* **104** 170–5
- [24] Castellanos-Gomez A, van Leeuwen R, Buscema M, van der Zant H S, Steele G A and Venstra W J 2013 Single-layer MoS₂ mechanical resonators *Adv. Mater.* **25** 6719–23
- [25] Sha Z-D, Pei Q-X, Ding Z, Jiang J-W and Zhang Y-W 2015 Mechanical properties and fracture behavior of single-layer phosphorene at finite temperatures *J. Phys. D: Appl. Phys.* **48** 395303
- [26] Takano Y, Arai N, Arai A, Takahashi Y, Takase K and Sekizawa K 2004 Magnetic properties and specific heat of MPS₃ (M = Mn, Fe, Zn) *J. Magn. Magn. Mater.* **272** E593–5
- [27] Prabhakar S and Vengallatore S 2008 Theory of thermoelastic damping in micromechanical resonators with two-dimensional heat conduction *J. Microelectromech. Syst.* **17** 494–502
- [28] Bonilla L and Ruiz-Garcia M 2016 Critical radius and temperature for buckling in graphene *Phys. Rev. B* **93** 115407
- [29] Nicholl R J, Conley H J, Lavrik N V, Vlassiokou I, Puzyrev Y S, Sreenivas V P, Pantelides S T and Bolotin K I 2015 The effect of intrinsic crumpling on the mechanics of free-standing graphene *Nat. Commun.* **6** 1–7
- [30] Wang Z, Yang R and Feng P X-L 2021 Thermal hysteresis controlled reconfigurable MoS₂ nanomechanical resonators *Nanoscale* **13** 18089–95
- [31] Ye F, Lee J and Feng P X-L 2018 Electrothermally tunable graphene resonators operating at very high temperature up to 1200 K *Nano Lett.* **18** 1678–85
- [32] Davidovikj D et al 2020 Ultrathin complex oxide nanomechanical resonators *Commun. Phys.* **3** 163
- [33] Inoue T, Mochizuki Y, Takei K, Arie T and Akita S 2018 Tuning of the temperature dependence of the resonance frequency shift in atomically thin mechanical resonators with van der Waals heterojunctions *2D Mater.* **5** 045022
- [34] Quantum Design 2023 Lake shore ultra-low temperature rox™ (available at: <https://qd-uki.co.uk/lake-shore/temperature-sensors/ultra-low-temperature-rox/>) (Accessed 16 March 2023)
- [35] Blaikie A, Miller D and Alemán B J 2019 A fast and sensitive room-temperature graphene nanomechanical bolometer *Nat. Commun.* **10** 4726
- [36] Qian Z, Hui Y, Liu F, Kang S, Kar S and Rinaldi M 2016 Graphene–aluminum nitride NEMS resonant infrared detector *Microsyst. Nanoeng.* **2** 1–7
- [37] Sarafraz A, Givois A, Roslon I, Liu H, Brahmi H, Verbiest G, Steeneken P G and Alijani F 2022 Dynamics of pressurized ultra-thin membranes (arXiv:2212.05464)
- [38] Verbiest G J, Kirchhof J N, Sonntag J, Goldsche M, Khodkov T and Stampfer C 2018 Detecting ultrasound vibrations with graphene resonators *Nano Lett.* **18** 5132–7
- [39] Ramos M, Carrascoso F, Frisenda R, Gant P, Mañas-Valero S, Esteras D L, Baldoví J J, Coronado E, Castellanos-Gomez A and Calvo M R 2021 Ultra-broad spectral photo-response in FePS₃ air-stable devices *npj 2D Mater. Appl.* **5** 1–9
- [40] Dolleman R J, Lloyd D, Lee M, Bunch J S, Van Der Zant H S and Steeneken P G 2018 Transient thermal characterization of suspended monolayer MoS₂ *Phys. Rev. Mater.* **2** 114008