

Delft University of Technology

#### Assessing nozzle flow dynamics in fused filament fabrication through the parametric map α – λ

Schuller, Tomás; Fanzio, Paola; Galindo-Rosales, Francisco J.

DOI 10.1063/5.0193715

**Publication date** 2024 **Document Version** Final published version

Published in Physics of Fluids

**Citation (APA)** Schuller, T., Fanzio, P., & Galindo-Rosales, F. J. (2024). Assessing nozzle flow dynamics in fused filament fabrication through the parametric map  $\alpha = \lambda$ . *Physics of Fluids, 36*(3), Article 033114. https://doi.org/10.1063/5.0193715

#### Important note

To cite this publication, please use the final published version (if applicable). Please check the document version above.

Copyright Other than for strictly personal use, it is not permitted to download, forward or distribute the text or part of it, without the consent of the author(s) and/or copyright holder(s), unless the work is under an open content license such as Creative Commons.

Takedown policy

Please contact us and provide details if you believe this document breaches copyrights. We will remove access to the work immediately and investigate your claim.

### Green Open Access added to TU Delft Institutional Repository

#### 'You share, we take care!' - Taverne project

https://www.openaccess.nl/en/you-share-we-take-care

Otherwise as indicated in the copyright section: the publisher is the copyright holder of this work and the author uses the Dutch legislation to make this work public.

#### RESEARCH ARTICLE | MARCH 11 2024

# Assessing nozzle flow dynamics in fused filament fabrication through the parametric map $\alpha-\lambda$

Special Collection: Physics of 3D Printing

Tomás Schuller 💿 ; Paola Fanzio 💿 ; Francisco J. Galindo-Rosales 📼 💿

Check for updates

*Physics of Fluids* 36, 033114 (2024) https://doi.org/10.1063/5.0193715



### **APL Energy**



## Latest Articles Online!





**Read Now** 

Export Citatio

View Online

# Assessing nozzle flow dynamics in fused filament fabrication through the parametric map $\alpha - \lambda$

Cite as: Phys. Fluids **36**, 033114 (2024); doi: 10.1063/5.0193715 Submitted: 23 December 2023 · Accepted: 19 February 2024 · Published Online: 11 March 2024

Tomás Schuller,<sup>1,2,3</sup> 🕞 Paola Fanzio,<sup>4</sup> 🕞 and Francisco J. Galindo-Rosales<sup>3,5,a)</sup> 🝺

#### **AFFILIATIONS**

<sup>1</sup>Institute of Science and Innovation in Mechanical and Industrial Engineering (INEGI), Rua Dr. Roberto Frias, 400, Porto 4200-465, Portugal

<sup>2</sup>Transport Phenomena Research Center (CEFT), Mechanical Engineering Department, Faculty of Engineering of the University of Porto, Rua Dr. Roberto Frias s/n, Porto 4200-465, Portugal

<sup>3</sup>ALiCE-Associate Laboratory in Chemical Engineering, Faculty of Engineering of the University of Porto, Rua Dr. Roberto Frias s/n, Porto 4200-465, Portugal

<sup>4</sup>Department of Precision and Microsystems Engineering (PME), Faculty of Mechanical Engineering (ME), TU Delft (Delft University of Technology), Mekelweg 2, Delft 2628 CD, The Netherlands

<sup>5</sup>Transport Phenomena Research Center (CEFT), Chemical Engineering Department, Faculty of Engineering of the University of Porto, Rua Dr. Roberto Frias s/n, Porto 4200-465, Portugal

**Note:** This paper is part of the special topic, Physics of 3D Printing. <sup>a)</sup>Author to whom correspondence should be addressed: galindo@fe.up.pt

#### ABSTRACT

Polymer rheology profoundly influences the intricate dynamics of material extrusion in fused filament fabrication (FFF). This numerical study, which uses the Giesekus model fed with a full rheometric experimental dataset, meticulously examines the molten flow patterns inside the printing nozzle in FFF. Our findings reveal new insight into the interplay between elastic stresses and complex flow patterns, highlighting their substantial role in forming upstream vortices. The parametric map  $\alpha - \lambda$  from the Giesekus model allowed us to sort the materials and connect the polymer rheology with the FFF nozzle flow dynamics. The identification of elastic instabilities, the characterization of flow types, and the correlation between fluid rheology and pressure drop variations mark significant advancements in understanding FFF processes. These insights pave the way for tailored nozzle designs, promising enhanced efficiency and reliability in FFF-based additive manufacturing.

Published under an exclusive license by AIP Publishing. https://doi.org/10.1063/5.0193715

#### I. INTRODUCTION

Material extrusion, an additive manufacturing (AM) method, entails precisely dispensing material through a nozzle, following established standards.<sup>1</sup> Fused filament fabrication (FFF), introduced by S. Scott Crump in 1989,<sup>2</sup> currently stands as the predominant technology for material extrusion.<sup>3</sup> FFF allows for the rapid, cost-effective creation of intricate three-dimensional (3D) objects suitable for practical applications.<sup>4</sup> Moreover, post-processing techniques like sanding, chemical treatment, polishing, and metal plating, among others, can be employed to enhance surface quality.<sup>5–7</sup>

The FFF process consists of introducing thermoplastic materials, usually in filament shape, from spools into a temperature-regulated liquefier, where they transform into liquid state. Subsequently, the molten material is extruded through a nozzle and guided by the print head onto a build plate in specific patterns to create a 3D object. Common quality issues in FFF systems encompass over-extrusion and under-extrusion, leading to the formation of blobs or holes. Another extrusion challenge, known as annular backflow, happens when the molten polymer reverses its flow along the ring-shaped region between the filament and the liquefier wall, escaping the heated area and cooling below the glass temperature, where fluid-solid transition occurs  $(T_g)$ .<sup>8</sup> These issues undoubtedly arise from the interplay of extrusion process parameters with the rheological properties of the molten filament;<sup>9</sup> however, the state-of-the-art lacks fundamental research to fully understand the underlying mechanisms that allow for technical solutions to these issues.

The printing nozzle is at the heart of the FFF process, being a critical component responsible for precise material deposition. $^{10-12}$  The

nozzle is a metal part connecting the liquefier to the die through a contraction. It is well documented in the literature<sup>13–19</sup> that the flow of viscoelastic fluids through an axisymmetric contraction geometry can lead to elastic instabilities responsible for generating not only upstream vortices but also excess pressure drop. Furthermore, smaller characteristic length scales in the geometry intensify elastic effects. Previous efforts sought to replicate the polymer melt extrusion process within an FFF printer nozzle using microfluidic chips of a planar geometry with shear-thinning polymer solutions. This led to the construction of a Deborah-Reynolds flow map, revealing the production of growing upstream vortices under typical printing flow conditions in an FFF nozzle.<sup>20</sup> Subsequently, the formation of vortices upstream of the tapered region in the nozzle, driven by elastic instabilities, was observed. This study was complemented in Ref. 21, where numerical analysis confirmed the presence of these vortices when molten Polycarbonate flowed through an axisymmetric nozzle geometry. It also allowed for the disentanglement of the relative significance of extension-induced and shear-induced elastic stresses in this extrusion process. It was concluded that within the upstream vortex, extensional elastic stresses predominated, but their importance diminished with higher extrusion velocities; moreover, they played a determinant role in the size of the upstream vortex structures. However, shear-induced normal stress differences may account for the excess pressure drop and a change in equilibrium height  $(H^*)$  in the backflow region, where the polymer melt flows upward between the solid filament and the liquefier wall. Recently, an experimental study with polylactic acid (PLA)<sup>22</sup> allowed the experimental determination of the nozzle pressure drop, which, in combination with traditional top-of-nozzle pressure measurements, permitted determining the pressure drop occurring in the liquefier and the calculation of equilibrium height in the backflow region based on experimental data exclusively. Results showed a nonlinear increase in the pressure measured by the feeders, which was associated with shear-induced elastic instabilities occurring in the backflow region at the same extrusion velocity at which the maximum equilibrium height  $(H^*)$  occurred.

Most of the research papers available in the literature dealing with FFF are focused either on a single polymeric material, such as our previous works,<sup>21,22</sup> or on exclusively the viscous effect on flow dynamics,<sup>23–25</sup> disregarding the viscoelastic intrinsic nature of the polymer melts affecting the stability of the flow through the nozzle at real printing speed.<sup>20</sup> In this work, we aim to go beyond the state-ofthe-art by analyzing numerically how the non-linear rheological properties of different materials commonly used in FFF, such as PET-G, PET-CF, PLA, PC, ABS, and PA6/66, can be reduced to limited numbers of parameters, i.e., Giesekus model parameters, and how this can help in sorting the materials and understanding the FFF nozzle flow dynamics; special attention will be given to the shear and extensional stress developed in the fluid, and how these are connected elastic instabilities, extra pressure drop and, ultimately, backflow issues.

#### **II. MATERIALS AND METHODS**

### A. Selection, characterization, and modeling of the polymers

Polymer choice is pivotal in FFF 3D printing, directly influencing the produced part characteristics and performance. Common thermoplastics like ABS, PET-G, and PLA offer ease of use, while engineering-grade polymers such as Nylon and polycarbonate enhance strength and temperature resistance. Polymers and composites with additives like carbon fiber or metal particles offer unique properties like conductivity or flame resistance. Selecting the most suitable polymer depends on specific application needs, considering factors like mechanical load, environment, and functionality. Filament diameter, quality, and printer compatibility are also important considerations.

The polymers that have been selected for this study are:

- 1. PET-G: It is a glycol-modified thermoplastic polyester that offers durability, chemical resistance, and formability. It surpasses PLA in strength, impact resistance, and temperature tolerance, making it a versatile choice.<sup>26</sup> UltiMaker's transparent PET-G was the material of choice in this study.
- 2. PLA: Derived from renewable sources, PLA is an environmentally friendly thermoplastic. It is cost-efficient and widely used in 3D printing, food, and medical industries.<sup>7,27</sup> In this analysis, as in previous work,<sup>22</sup> UltiMaker transparent PLA was used.
- 3. PC: Polycarbonate is a strong thermoplastic known for impact resistance, heat tolerance, and fire retardancy, making it suitable for challenging environments.<sup>28</sup> For this study, as in Ref. 21, UltiMaker transparent PC was used.
- 4. PA6/66: A copolymer of PA6 and PA66, PA6/66 offers high rigidity, heat resistance, and chemical resistance. It is ideal for industrial applications, including automotive and aerospace.<sup>29,30</sup> DSM Novamid<sup>®</sup> ID 1030 (PA6/66) black was utilized in this investigation.
- ABS: ABS is an impact-resistant engineering thermoplastic commonly used in structural applications and various products.<sup>7,28</sup> In this study, the choice of material fell on UltiMaker white ABS.
- 6. PET-CF: PET-CF, a carbon fiber-reinforced PET variant, combines printability with enhanced stiffness, chemical, and temperature resistance, making it suitable for industrial 3D printing.<sup>31</sup> For this research, LUVOCOM<sup>®</sup> 3F PET-CF 9780 Black was used.

Traditionally, researchers have characterized and modeled the polymer melts based on rheometric data from small amplitude oscillatory shear experiments (SAOS), which provide information about the linear viscoelastic behavior of the materials. This rheological information has been proven to be useful in predicting the flow of monodisperse and bidisperse linear polymer melts; however, incorporating the nonlinear rheology is necessary to predict accurately the flow of polydisperse systems, such as those industrial melts, in extrusion flows.<sup>32</sup> Moreover, it is impossible to adequately describe the highly complex dependency on strain and strain rate experienced by a fluid element of viscoelastic material in a strong extensional flow using a shear rheological characterization exclusively.<sup>33</sup> Thus, a complete rheological characterization consisting of a combination of steady shear flow curves and steady extensional flow experiments followed the protocols is detailed below and is also present in our previous works.<sup>21,</sup>

Viscosity curves under steady shear conditions were obtained at the working temperature (Table I) for each polymer using an ARES G2 rotational rheometer. Parallel plates with a 12 mm diameter and a 1 mm gap were used. For shear rheological tests, specimens were shaped into disks (12 mm diameter, 1.5 mm thickness) through hot compression molding. The specimens were pre-conditioned in a wellventilated oven and then compression-molded, followed by cooling with a water circulation system.

TABLE I.	Polymer	melt working	temperatures.
----------	---------	--------------	---------------

Material	PET-G	PLA	PC	PA6/66	ABS	PET-CF
Temp. (°C)	240	205 <sup>22</sup>	260 <sup>21</sup>	243	240	265

For the elongational viscosity measurements, a rotational rheometer (ARES G2) equiped with the TA Instruments extensional viscosity fixture  $(EVF)^{34-36}$  was employed, imposing various strain rates (0.1, 0.3, 1, and 3 s<sup>-1</sup>) to fresh samples. Specimens (8–10 mm width, 1 mm thickness, 18 mm length) were die-cut from compression-molded plates, pre-dried, and cooled with a water circulation system before testing.

Åmong the plethora of constitutive models available in the literature for polymer melts, the Giesekus model was chosen [Eq. (1)], as in our previous works:<sup>21,22</sup>

$$\boldsymbol{\tau} + \lambda \boldsymbol{\bar{\tau}} + \alpha \frac{\lambda}{\eta_0} (\boldsymbol{\tau} \cdot \boldsymbol{\tau}) = \eta_0 (\nabla \boldsymbol{u} + \nabla \boldsymbol{u}^T), \tag{1}$$

where  $\eta_0$  is the zero-shear viscosity and  $\lambda$  is the relaxation time, both determined from the relaxation spectrum in steady-state; the dimensionless Giesekus-model mobility factor (a) governs the extensional viscosity and the ratio of the second normal stress difference to the first. This constitutive model, already incorporated into the constitutiveEquations library of rheoTool,37 can predict shearthinning, shear first and second normal-stress differences.<sup>38</sup> According to Ref. 39, both the Giesekus and Rolie-Poly models<sup>40</sup> achieve similar results; however, the Giesekus model is more attractive to carry out simulations because it needs fewer parameters. Moreover, we have already validated the potential of the Giesekus model to predict the growth of the vortex size produced by viscoelastic fluids flowing through planar contractions microfluidic channels (Fig. 5 in Ref. 21) additionally, the Giesekus model was also able to predict the extrudate-swell measurements for polycarbonate (Fig. 10 in Ref. 21) Furthermore, we have recently reported that the Giesekus model can reasonably predict the pressure inside the nozzle for PLA (Fig. 8 in Ref. 22) experimentally measured with a custom nozzle design. Based on this, we are confident that the Giesekus model captures the physics of the polymer melt flow through the nozzle in real FFF printing conditions.

As the printing process imposes a complex flow, combining extensional and shear flows, the Giesekus model has to be able to fit both kinds of non-linear rheometric datasets to provide meaningful predictions. Thus, the rheometric datasets from shear and extensional rheological characterizations determined the value of parameters of the Giesekus model and the number of modes. It is important to note that in its current version, *rheoTool* does not perform the automatic fitting of the constitutive model parameters from the user-input experimental data. It is currently a hot research topic developing new artificial intelligence tools for fitting constitutive models' parameters to non-linear data sets, such as those coming from LAOS experiments.<sup>41</sup> Thus, no routine is available for providing the fitting parameters of a constitutive model based on nonlinear rheometric data combining shear and extensional information.

Figure 1 shows the iterative process for determining the values of the Giesekus model, which combines the manual modification of the parameters values and the automatic production of the numerical prediction to the experimental datasets. *rheoTestFoam* was used to compare numerical responses with the rheometric datasets under the same experimental conditions. The initial approach to fitting the models was fully manual, involving the user in all the steps, leading to a repetitive and tedious process. To improve the process, a collection of Python scripts was developed to run and plot the data automatically (Fig. 1), allowing for a more visual iterative process drastically reducing the model creation time.<sup>42</sup> However, the final evaluation of the numerical prediction was qualitative.

Table II details the estimated values for model parameters for each polymer, weight-averaged by  $\eta$ . Figure 2 presents the parametric map  $\alpha - \lambda$ , as a sort of Ashby diagram, a valuable tool for materials selection and design optimization.<sup>43</sup> The goal is to group similar objects into clusters having similar values of the  $\lambda$  and  $\alpha$  parameters, enhancing our understanding of their rheological relationships. Figure 3 shows a comparison between the experimental rheological characterization and the numerical predictions for each working polymer. The subplots of Fig. 3 were gathered based on the groups formed in Fig. 2, confirming that similar locations in the  $\alpha - \lambda$  parameters-map resulted in similar rheological behaviors.

Regarding the experimental extensional datasets, the reader must be aware of the fact that their quality is lower than the one from the shear viscosity curves due to difficulties associated with imposing purely extensional deformations in the EVF system, such as sagging due to gravitational effects. Having an excellent rheological dataset is paramount for fitting the parameters of the constitutive model in order to ensure the quality of the numerical predictions. The filament stretching approach<sup>44</sup> has been proven to provide excellent results not



**FIG. 1.** Work flow for determining the values of the Giesekus model parameters based on both shear and extensional rheometric dataset.

TABLE II. Polymer melt parameters (all materials).

Material	PET-G	PLA	РС	PA6/66	ABS	PET-CF	
Model	Giesekus						
Num. modes	3	3	4	2	2	2	
Avg. η	600	2220	563	1300	43900	1038	
Avg. λ	0.355	0.209	0.713	0.518	13.27	27.21	
Avg. α	0.0331	0.0133	0.233	0.239	0.107	0.018	

only for Newtonian fluids and polymer solutions,<sup>45</sup> but also for suspensions;<sup>46</sup> Bach *et al.*<sup>47</sup> developed a prototype of filament stretching rheometer suitable for polymer melts at high temperatures, avoiding problems with temperature gradients, and end-plate slip and ensuring reliable measurement of deformation; unfortunately, this device is not currently commercialized.

Considering this, in the trial-error procedure for determining the model parameters for each polymer, the best possible approximation to the shear dataset was the first criterion for considering them reliable. Then, the trends defined by the extensional viscosity data were also tried to follow. Regarding the number of modes, we tried to keep them as low as possible, but it was necessary to increase them to improve the accuracy of the prediction. Deviations of the numerical predictions with the Giesekus model from the experimental measurements in Refs. 21 and 22 are not associated with the quality of the approximation to the rheometric data, but either with the simplifications assumed in the numerical modeling of the physical problem, such as isothermal flow, and backflow issues.

Figure 3 also illustrates the transient evolution of extensional viscosity  $[\eta_E^+(t, \dot{\epsilon})]^{48}$  at various extension rates. For the materials in group 1, it can be observed that all the curves overlap; additionally, the extensional viscosity reaches a steady state pointing toward a value



**FIG. 2.** Parametric map  $\alpha - \lambda$ , which allows for grouping the materials by property proximity. In regard to crystallinity: amorphous—square, semi-crystalline—circle, and composite—triangle.

respecting the Trouton ratio, i.e.,  $Tr = \frac{\eta_E^*}{\eta_0}^{49,50}$  which can be considered as a sign of the measurement quality and that the polymer chains are excited within the linear viscoelastic region.<sup>51,52</sup> Materials included in group 2 and 3 exhibited a marked strain-hardening, exhibiting Trouton ratios larger than 3.<sup>53</sup>

#### **B.** Nozzle flow simulations

The nozzle geometry consists of an axisymmetric contraction as described in Ref. 21. The tube length was adjusted to guarantee flow development at the start of the contraction region before the tapered section. Gravity was aligned with the nozzle's symmetry axis, and the cylindrical coordinate system's origin coincided with the beginning of the upstream length. Two boundary conditions were applied at the internal wall of the nozzle: a non-slip condition and zero pressure gradient. The non-slip condition means that the velocity of the polymer melt is the same as that of the solid wall, which in this case is zero, as the liquefier and the nozzle are stationary. Zero pressure gradient means no net change in pressure along the flow direction within the boundary layer; in other words, the pressure remains relatively constant as the fluid moves along the surface. In the context of the boundary layer, a zero pressure gradient condition implies that the pressure forces acting on the fluid in the direction parallel to the surface are relatively balanced, and there is no strong driving force due to pressure differences. The zero pressure gradient boundary layer is of interest in various engineering applications, and its study helps understand the behavior of fluid flow near surfaces. Additionally, at the inlet face, a uniform velocity profile  $(V_{in} = \overline{V_{in}} e_z)$  was enforced, with  $\overline{V_{in}}$  representing the average velocity linked to the extrusion velocity  $\overline{V_{ext}}$ ,

$$\overline{V_{in}} = \overline{V_{ext}} \frac{D_c^2}{D_u^2}.$$
(2)

In this research, we examined nine different extrusion velocities spanning four orders of magnitude:  $\overline{V_{ext}} = \{0.01, 0.1, 1, 2, 5, 10, 30, 70, 110\}$  mm/s. The Reynolds and Weissenberg numbers corresponding to each velocity and material are detailed in Tables III and IV. Additionally, we applied a zero gradient for pressure at the inlet. At the die exit, where the extruded material encounters atmospheric conditions, we set the pressure to zero, while the boundary condition for velocity was treated as outflow with a zero gradient.

The axisymmetric geometry allowed for efficient twodimensional (2D) numerical simulations instead of 3D, significantly reducing computational time. Consequently, the numerical 2D setup consisted of a narrow-angle wedge, one cell thick, running along the centerline. Wedge-type patches were used for both velocity and pressure, as previously validated in Ref. 21. Similar to our prior studies,<sup>21,22</sup> a structured two-dimensional mesh was created using the *blockMesh* utility, comprising three zones: (1) the straight upstream section, (2) the tapered area, and (3) the die region. A stream-wise stretch ratio was applied to enhance resolution at the die and abrupt contraction zone. A grid analysis ensured spatial convergence for the presented results in this work.

Isothermal and steady flow through the extrusion nozzle were assumed for all materials and simulations. Consequently, the energy equation was decoupled from the mass and momentum conservation equations. Treating the molten polymer as an incompressible fluid, the



FIG. 3. Steady shear and extensional viscosity curves for all materials. Experimental datasets (symbols) are compared against their numerical predictions (solid lines) obtained for the Giesekus model with the parameters given in Table II: (a) PET-G, (b) PLA, (c) PC, (d) PA6/66, (e) ABS, and (f) PET-CF. mass conservation equation was simplified as depicted in the following equation:

$$\nabla \cdot \boldsymbol{u} = \boldsymbol{0}. \tag{3}$$

Equation (4) gives the momentum conservation equation

$$\rho \boldsymbol{u} \cdot \nabla \boldsymbol{u} = -\nabla P - \nabla \cdot \boldsymbol{\tau}. \tag{4}$$

In this context, we considered a steady-state flow  $(\frac{\partial u}{\partial t} = 0)$ , while excluding the negligible effects of gravity. Here, we used the notation *P* for pressure,  $\rho$  for density, and the extra stress tensor  $\tau$ , which encompasses contributions arising from the fluid deformation as defined in the Giesekus model found in Eq. (1).

These equations were solved using the rheoTool library<sup>37,54</sup> integrated with OpenFOAM<sup>®</sup>.<sup>55</sup> A high-resolution scheme (CUBISTA) and the log-conformation formulation of the constitutive equation ensured numerical stability.<sup>56</sup>

#### **III. RESULTS AND DISCUSSION**

The kinematics of the flow through the nozzle geometry is complex, i.e., at the wall, the polymer melt will undergo pure shear flow  $(\dot{\gamma} = \frac{\partial u_z}{\partial r})$  and, at the centerline, the rate of deformation is purely extensional ( $\dot{\epsilon} = \frac{\partial u_z}{\partial z}$ ). The complexity of the contraction flow is well represented by the flow-type parameter,<sup>57</sup> defined as

$$\xi = \frac{\|\boldsymbol{D}\| - \|\boldsymbol{\Omega}\|}{\|\boldsymbol{D}\| + \|\boldsymbol{\Omega}\|}.$$
(5)

In this context,  $\|\boldsymbol{D}\| = \sqrt{\frac{\boldsymbol{D} \cdot \boldsymbol{D}^T}{2}}$  represents the magnitude of the rate-ofdeformation tensor  $\boldsymbol{D} = \frac{1}{2} (\nabla \boldsymbol{u} + \boldsymbol{u}^T)$ , and  $\|\boldsymbol{\Omega}\| = \sqrt{\frac{\boldsymbol{\Omega} \cdot \boldsymbol{\Omega}^T}{2}}$  signifies the

deformation tensor  $D = \frac{1}{2}(\nabla u + u^{T})$ , and  $||\Omega|| = \sqrt{\frac{24.32}{2}}$  signifies the magnitude of the vorticity tensor  $\Omega = \frac{1}{2}(\nabla u - u^{T})$ , where u denotes the velocity field. Irrespective of the fluid's rheological characteristics and the nozzle's geometry, reducing the diameter induces a complex flow pattern. This pattern encompasses regions characterized by purely simple shear ( $\xi = 0$ ), areas of purely elongational flow ( $\xi = 1$ ), sections approaching solid-body rotation ( $\xi = -1$ ), and regions displaying a combination of these behaviors.<sup>21,58-60</sup> The contraction within the nozzle generates a diverse range of flow types, spanning from simple shear to extensional flow, encompassing the entire nozzle's cross section. That kinematics complexity results in a complex distribution of normal stress differences ( $\Delta \tau = \tau_{zz} - \tau_{rr}$ ), that is, at the wall, the normal stress difference corresponds to the shear-induced ones ( $\Delta \tau = N_1$ ); at the centerline, the normal stress difference is related to the extension of the molecules ( $\Delta \tau = \sigma_E$ ); whereas at any location in between they are coupled.<sup>61</sup>

Figure 4 shows a composition of the contour plots corresponding to the gradient of flow type (left half) and the normal stress differences (right half) for all the materials considered in this study. Different patterns in the flow type can be observed depending on the material extruded; as expected, the flow type is mainly dominated by the shear flow (green), although important portions of the fluid domain, axisymmetric and with a dart shape, are pure extensional flow (red). As mentioned above, this leads to a rate of deformation distribution, which, depending on the rheological properties of the fluid, results in a convoluted distribution of stress differences, depending on the material's rheological properties. It can be observed in Fig. 3 that PLA and PET-G (group 1) exhibit shear thinning, and a soft-curved and asymptotic increase in the extensional viscosity, which resulted in a squared normal stress difference distribution centered at the axis of symmetry (Fig. 4). PC and PA6/66 (group 2) also exhibited shear thinning under shear flow but strain hardening under extensional flow (Fig. 3); this rheological behavior resulted in an indent at the centerline in the previous squared normal stress difference, compared to that shown by PLA and PET-G (Fig. 4). Finally, ABS and PET-CF (group 3) presented shear thinning, but a steep increase in the extensional viscosity with the accumulated deformation (Fig. 3), which resulted in an even more pronounced indentation in the normal stress difference contour plot at the centerline (Fig. 4).

In the elongational characterization of the polymer melts, the extensional viscosity is plotted against the accumulated deformation ( $\epsilon$ ). The accumulated deformation results from integrating the extension rate ( $\dot{\epsilon}$ ) over the time of the experiment

$$\epsilon = \int_0^t \dot{\epsilon} dt,\tag{6}$$

as in the rheometric experiment the extension rate is kept constant, then  $\epsilon = \dot{\epsilon}t$ . This relationship is essential in understanding how the material accumulates deformation in an elongational flow field, providing insight into the total extension experienced by the material over a given period. It is particularly relevant in polymer processing, fluid dynamics, and other fields where the deformation of materials is a critical aspect of the study. In the centerline of the nozzle geometry, the fluid undergoes a shear-free extensional flow, in which the extension rate depends on the position in the tapered region.<sup>21</sup> The average extension rate ( $\overline{\epsilon}$ ) increases with the volumetric flow rate (Q), according to the following equation:

$$\overline{\overline{\epsilon}} \approx \frac{4Q}{\pi L} \left( \frac{1}{D_c^2} - \frac{1}{D_u^2} \right). \tag{7}$$

Thus, on average, increasing the flow rate would increase the accumulated deformation for a constant residence time ( $\overline{\epsilon} = \overline{\epsilon} t_{res}$ ). The residence time ( $t_{res}$ ) of the polymer melt flowing through the nozzle can be calculated by dividing the volume of the nozzle (V) by the flow rate. The volume of the nozzle is the same for all the cases and all the materials. Thus, the residence time is inversely proportional to the volumetric flow rate ( $t_{res} = V/Q$ ). This means the residence time decreases as the volumetric flow rate increases, and vice versa. Therefore, the average accumulated deformation in the nozzle ( $\overline{\epsilon}$ ) does not depend on the flow rate but the geometric dimensions of the nozzle

$$\overline{\epsilon} \approx \frac{4V}{\pi L} \left( \frac{1}{D_c^2} - \frac{1}{D_u^2} \right). \tag{8}$$

It has been demonstrated that the averaged accumulated deformation remains independent of the flow rate for a specified nozzle shape.

Based on the arguments presented above, this result can be directly correlated with the extensional rheometric information as follow: a material with a steeper extensional viscosity curve will provide a larger resistance to flow under extensional flow for a given accumulated deformation, that remains unaltered for the same nozzle shape.

Due to the viscoelastic nature of the polymers, upon a critical flow rate, upstream vortex structures were observed for all of them



(Fig. 4). The tip of the normal stress difference distribution marked the tip of the upstream vortex structure, confirming that the presence of upstream vortices in viscoelastic contraction flows is due to elastic instabilities. Further increasing the flow rate leads to an unsteady

motion of the vortex and oscillating values in the pressure drop, as previously reported.  $^{\rm 17,22}$ 

Figure 5 shows the typical *S*-shaped curve for the upstream vortex size  $[X_r \text{ (mm)}]$  with a growing flow rate  $[Q \text{ (mm}^3/s)]$  for all materials,

**Physics of Fluids** 



FIG. 5. Numerical upstream vortex lengths for the different materials. Group 1—triangles; group 2—circles; and group 3—squares.

which tends asymptotically to the Moffatt vortex size at low flow rates and to a saturation size at high flow rates.<sup>14</sup> The combination of considerably high relaxation time and viscosity resulted in a faster growth rate of the upstream vortex size, as could be observed for group 3 of polymers, whereas relatively low viscosities and relaxation time exhibited a lower rate of growth in upstream vortex structures (e.g., PET-G). The sequence observed in Fig. 5 can be inferred from the product  $\eta \cdot \lambda$ (Table II), which is an estimation of the zero-shear first normal stress coefficient ( $\Psi_{10}$ ,<sup>48</sup> A); thus, the larger the first normal stress coefficient is, the more prone is the polymer to develop upstream vortices.<sup>16</sup>

In FFF, the solid thermoplastic filament is melted in the liquefier and extruded through a nozzle. The rollers push down the solid filament, which works as a piston to impose a pressure-driven flow to the polymer melt. It has been previously reported<sup>22</sup> that the total pressure drop measured in the feeders can be decoupled as a sum of the pressure drop in the liquefier and the pressure drop in the nozzle, being the latter very close to the one predicted by the numerical model proposed here. In a cylindrical coordinate system, the conservation momentum equation for the steady-state Poiseuille flow of viscoelastic material through the nozzle gets reduced to the following ones, corresponding to *r* and *z*-directions, respectively,<sup>38</sup>

$$\rho\left(u_r\frac{\partial u_r}{\partial r} + u_z\frac{\partial u_r}{\partial z}\right) \approx -\frac{\partial P}{\partial r} - \frac{1}{r}\frac{\partial N_2}{\partial r} - \frac{\partial \tau_{zr}}{\partial z},\tag{9}$$

$$\rho\left(u_r\frac{\partial u_z}{\partial r} + u_z\frac{\partial u_z}{\partial z}\right) \approx -\frac{\partial P}{\partial r} - \frac{1}{r}\frac{\partial}{\partial r}(r\tau_{rz}) - \frac{\partial\tau_{rr}}{\partial z}, \quad (10)$$

where  $u_r$  and  $u_z$  must satisfy the mass conservation equation

$$\frac{\partial u_r}{\partial r} + \frac{\partial u_z}{\partial z} = 0. \tag{11}$$

The shear viscosity ( $\eta \propto \tau_{rz}$ ) and the first normal stress difference ( $\Delta \tau = \tau_{zz} - \tau_{rr} \approx \tau_{zz}$ ) are responsible for the pressure gradient in the direction of the flow [Eq. (10)], being  $\Delta \tau$  dependent on the kind of deformation exerted to the polymeric molecules, i.e., extensional at the

centerline, pure shear at the wall, or a combination anywhere in between. Therefore, the larger the shear viscosity and the larger the area occupied by large values of first normal stress differences (Fig. 4), the more significant the pressure drop will be.

Figure 6 shows the dependence of the pressure drop with the imposed flow rate, and it confirms the previous analysis, showing that ABS, PLA, and PET-CF exhibit more significant pressure drops, followed by PET-G, PC, and PA6/66. It is important to note that Fig. 6 accounts for the pressure drop within the tapered region and the pressure drop in the straight parts of the nozzle. The shear thinning behavior present in all the polymeric materials provokes a decrease in pressure drop due to viscous contribution; upon a critical flow rate, the elastic instabilities are triggered, and the excess pressure drop is activated.<sup>13,62</sup> Further increasing the flow rate leads to an unsteady motion of the vortex and, subsequently, oscillating values in the pressure drop,<sup>22</sup> which can be associated with elastic turbulence.<sup>63,64</sup> A low value in the  $\alpha$  parameter implies a less shear thinning, and the fluid tends to a Boger-fluid-like behavior; thus, the material would be more prone to trigger elastic instabilities and turbulence.<sup>65</sup>

By combining the data presented in Fig. 6 with the viscosity curves depicted in Fig. 3, one can observe that the larger the viscosity of the polymer, the larger the pressure drop. A stronger shear thinning behavior (higher values in the  $\alpha$  parameter) results in a bend of the  $\Delta P - Q$  curve, whereas low values of  $\alpha$  lead to elastic turbulence, with oscillating and larger pressure drops. This, together with the shapes of normal stress difference plots, allows for the understanding that a more squared/plug-shaped region in the center of the tapered region, along with the approximation of the vortex to the center of the channel, more pronounced in the PLA case (Fig. 4), leads to a higher magnitude of elastic turbulence/instabilities in the re-entrant corner, a critical region of the flow.

By plotting the vortex size against the pressure drop for all materials (Fig. 7), it is possible to attest that polymers with relatively low relaxation time ( $\lambda < 1$  s) are more sensitive, and the pressure drop increases drastically for a small increase in vortex size in its initial stages. This increase then becomes more gradual as the recirculation grows.

The shaded regions in Figs. 5–7 represent the printing conditions when elastic turbulence is dominating. In that region, the pressure drop values and the vortices for this nozzle begin to oscillate and the shaded regions indicate the space between the minimum and maximum values recorded in the simulations, as in Ref. 22.

Although die-swell was not considered a matter of investigation in this work, it can be an important parameter in FFF, particularly on the fiber orientation and the resulting mechanical properties.<sup>66</sup> Dieswell is not affected by the presence of the upstream vortices,<sup>67</sup> and it has been reported in the literature<sup>68</sup> that the swelling ratio decreases as the value of the  $\alpha$  parameter increases. Therefore, according to Table II, the larger die-swell would be expected for polymers belonging to group 2, followed by ABS, PET-G, PET-CF, and, finally, PLA.

#### **IV. CONCLUSIONS**

This study has conducted a thorough numerical examination of upstream vortex formation in a standard fused filament fabrication (FFF) nozzle during stable flow conditions. The investigation utilized the Giesekus constitutive model, incorporating data from steady simple shear experiments and transient extensional viscosity experiments conducted at different extension rates.

ARTICLE



**FIG. 6.** Pressure drop against flow rate for all the polymers: (a) group 1—plug shape in  $\tau_{zz}$ - $\tau_{rr}$  plots; (b) group 2—short arrow shape in  $\tau_{zz}$ - $\tau_{rr}$  plots; and (c) group 3—long arrow shape in  $\tau_{zz}$ - $\tau_{rr}$  plots.

Significant contributions have been made to the body of knowledge derived from previous work.<sup>20,21</sup> It has been demonstrated that even under steady flow conditions at extrusion velocities representative of practical scenarios, growing upstream vortices are influenced by elastic instabilities. These instabilities manifest as physical disturbances in pressure, leading to the phenomenon known as "elastic turbulence."

Complex flow patterns induced within the nozzle, ranging from simple shear to extensional flow, have been critically examined. These flow phenomena affect the behavior of molten polymer from the nozzle walls to the axis (as depicted in Fig. 4). This intricate behavior persists through the tapered region and further upstream into the liquefier, while the flow inside the die is primarily characterized by simple shear.

Two key observations have arisen from the analysis of flow types and variations in normal stress first, the vortex tip marks the culmination of elastic stresses induced by extensional flow, and second, the shape of the stress contour plot has a direct impact on the proximity of the upstream vortex to the nozzle centerline. These observations are further supported by the consistent appearance of rheological groups identified during the characterization. In the examination of the plots displaying normal stress surfaces, the intricate interplay between these stresses surrounding the contraction has been discerned. This relationship sheds light on the rheological properties of the fluid and contributes significantly to variations in pressure drop and the emergence of instabilities. This fluid characteristic appears to correlate with elevated excess pressure drop, potentially causing operational challenges during printing.

Furthermore, the sensitivity of various materials to the creation of recirculation vortices has been uncovered. A thorough comprehension of total pressure drop and upstream vortex formation is paramount for optimizing the FFF process. These factors directly influence extrusion rates, backflow tendencies, and overall print quality, as previously discussed.<sup>22</sup> Elevated pressure drops can give rise to complications such as filament deformation, irregular flow patterns, or even nozzle clogging. Additionally, this insight empowers us to anticipate potential challenges and develop strategies to mitigate them, thereby enhancing the efficiency and reliability of FFF-based 3D printing.



FIG. 7. Pressure vs vortex size, for all materials. Group 1-triangles; group 2-circles; group 3-squares.

James and Roos recently demonstrated in their work<sup>67</sup> that it is feasible for a viscoelastic fluid to traverse a converging channel without inducing upstream vortices, resulting in an equivalent pressure drop across the contraction as that of a Newtonian fluid with the same viscosity. Under these circumstances, elasticity does not impact pressure drop within the nozzle, but influences die swell at the exit. Achieving this involves modifying the nozzle's shape to facilitate the radial distribution of normal stress and pressure, prompting streamlines to migrate to the centerline, consequently reducing the shear rate and shear stress at the wall. Consequently, the energy expended on shear within the channel decreases, with the saved energy being redirected toward polymer-related viscous dissipation. This conclusion,67 together with the result obtained in Fig. 7 inspired us and allowed us to envisage the possibility of having an optimal nozzle shape for each polymer rheology so that upstream vortices would be suppressed and, consequently, the pressure drop in the nozzle would be minimum, being dependent exclusively on the viscosity of the material.

This work showed that the tandem "nozzle shape—polymer rheology" affects the quality and performance of FFF, especially at high

TABLE III. Re <sub>0</sub> fo	r all materials and	extrusion velocities.
-------------------------------	---------------------	-----------------------

speeds. To prevent problems such as filament distortion, backflow and clogging, future research and development could focus on implementing Optimized Shape Design<sup>69</sup> to specific polymer rheologies. These improvements can help advance Fused Filament Fabrication technology and make 3D printing more efficient and reliable.

#### ACKNOWLEDGMENTS

The authors thank Johan Versteegh for the fruitful discussion and selfless support. F.J.G.-R. and T.S. acknowledge the financial support from Ultimaker B.V., and also LA/P/0045/2020 (ALiCE), UIDP/00532/2020 (CEFT) and the program Stimulus of Scientific Employment, Individual Support-2020.03203.CEECIND, funded by FEDER funds through COMPETE2020—Programa Operacional Competitividade e Internacionalização (POCI); and by national funds (PIDDAC) through FCT/MCTES.

#### AUTHOR DECLARATIONS

#### **Conflict of Interest**

The authors have no conflicts to disclose.

#### **Author Contributions**

Tomás Schuller: Conceptualization (supporting); Data curation (lead); Formal analysis (lead); Methodology (lead); Software (lead); Validation (lead); Visualization (lead); Writing – original draft (lead). Paola Fanzio: Conceptualization (equal); Funding acquisition (equal); Methodology (equal); Resources (equal); Supervision (equal); Validation (equal); Visualization (equal); Writing – review & editing (equal). Francisco J. Galindo-Rosales: Conceptualization (lead); Funding acquisition (lead); Methodology (equal); Project administration (lead); Resources (lead); Supervision (lead); Validation (equal); Visualization (equal); Writing – review & editing (lead).

#### DATA AVAILABILITY

The data that support the findings of this study are available from the corresponding author upon reasonable request.

#### APPENDIX: DIMENSIONAL ANALYSIS

White<sup>70</sup> used dimensional analysis for steady second-order fluid flows, revealing three key dimensionless groups. The first,

$\overline{V_{ext}}$ (mm/s)	ABS	PLA	PC	PA6-66	PET-CF	PET-G
0.01	$8.61  imes 10^{-11}$	$1.93  imes 10^{-9}$	$7.60 \times 10^{-9}$	$3.11 \times 10^{-9}$	$4.56 \times 10^{-9}$	$6.93 \times 10^{-9}$
0.1	$8.61\times 10^{-10}$	$1.93  imes 10^{-8}$	$7.60 \times 10^{-8}$	$3.11  imes 10^{-8}$	$4.56 \times 10^{-8}$	$6.93 \times 10^{-8}$
1	$8.61  imes 10^{-9}$	$1.93  imes 10^{-7}$	$7.60 \times 10^{-7}$	$3.11  imes 10^{-7}$	$4.56  imes 10^{-7}$	$6.93 \times 10^{-2}$
2	$1.72  imes 10^{-8}$	$3.86  imes 10^{-7}$	$1.52  imes 10^{-6}$	$6.22  imes 10^{-7}$	$9.12  imes 10^{-7}$	$1.39  imes 10^{-6}$
5	$4.31  imes 10^{-8}$	$9.64  imes 10^{-7}$	$3.80 \times 10^{-6}$	$1.56  imes 10^{-6}$	$2.28  imes 10^{-6}$	$3.47 \times 10^{-6}$
10	$8.61\times 10^{-8}$	$1.93  imes 10^{-6}$	$7.60 \times 10^{-6}$	$3.11  imes 10^{-6}$	$4.56 \times 10^{-6}$	$6.93 \times 10^{-6}$
30	$2.58 imes10^{-7}$	$5.78  imes 10^{-6}$	$2.28  imes 10^{-5}$	$9.33  imes 10^{-6}$	$1.37  imes 10^{-5}$	$2.08  imes 10^{-5}$
70	$6.03  imes 10^{-7}$	$1.35  imes 10^{-5}$	$5.32  imes 10^{-5}$	$2.18 imes10^{-5}$	$3.19  imes 10^{-5}$	$4.85  imes 10^{-5}$
110	$9.47 imes10^{-7}$	$2.12  imes 10^{-5}$	$8.36  imes 10^{-5}$	$3.42  imes 10^{-5}$	$5.01 \times 10^{-5}$	$7.63  imes 10^{-5}$

25 March 2024 07:48:07

TABLE IV. Wio for all materials and extrusion velocities.

$\overline{V_{ext}}$ (mm/s)	ABS	PLA	PC	PA6-66	PET-CF	PET-G
0.01	0.6635	0.01045	0.03565	0.0259	1.3605	0.01775
0.1	6.635	0.1045	0.3565	0.259	13.605	0.1775
1	66.35	1.045	3.565	2.59	136.05	1.775
2	132.7	2.09	7.13	5.18	272.1	3.55
5	331.75	5.225	17.825	12.95	680.25	8.875
10	663.5	10.45	35.65	25.9	1360.5	17.75
30	1990.5	31.35	106.95	77.7	4081.5	53.25
70	4644.5	73.15	249.55	181.3	9523.5	124.25
110	7298.5	114.95	392.15	284.9	14965.5	195.25

similar to classical fluid mechanics' Reynolds number  $(Re = \rho UD/\mu)$ , represents the ratio of inertial to viscous forces, here as  $Re_0 = \rho \overline{V_{ext}} D_c/\mu_0$ , being  $\mu_0$  the average viscosity parameter from Table II; the second group balances elastic and viscous forces; while the third relates to higher-order properties, particularly the "viscoelastic ratio" number, the ratio of  $N_2$  to  $N_1$ , which is typically negligible in polymer melts. The group  $\lambda U/L$  was termed the "Weissenberg number," now known as Wi; the Weissenberg number used is  $Wi_0 = \lambda_0 \overline{V_{ext}} / (D_c/2)$ , where  $\lambda_0$  is the average relaxation time from Table II. Finally, the elasticity number, El, characterizes the elastic and inertial forces balance, defined as El = Wi/Re; in this document,  $El_0 = Wi_0/Re_0$ , with  $Wi_0$  and  $Re_0$  as previously defined.

Tables III and IV show the values of  $Re_0$  and  $Wi_0$  for each material and each extrusion velocity considered in this study. It can be observed the low values of  $Re_0$ , below  $O(10^{-5})$  and  $Wi_0 > 1$  even for low extrusion velocities, depending on the rheological properties of the material. The small characteristic length scale and the large viscosities of every polymer melt ensure large values for  $El_0$  at all the extrusion velocities.

#### REFERENCES

- <sup>1</sup>ISO, Additive Manufacturing—General Principles—Fundamentals and Vocabulary, Standard (International Organization for Standardization, Geneva, 2021).
- <sup>2</sup>S. S. Crump, "Modeling apparatus for three-dimensional objects," US patent US5340433A (2011).
- <sup>3</sup>J. C. Najmon, S. Raeisi, and A. Tovar, "Review of additive manufacturing technologies and applications in the aerospace industry," in *Additive Manufacturing for the Aerospace Industry*, edited by F. Froes and R. Boyer (Elsevier, 2019), pp. 7–31.
- <sup>4</sup>H. Klippstein, A. Diaz De Cerio Sanchez, H. Hassanin, Y. Zweiri, and L. Seneviratne, "Fused deposition modeling for unmanned aerial vehicles (UAVs): A review," Adv. Eng. Mater. 20(2), 1700552 (2018).
- <sup>5</sup>A. Lalehpour and A. Barari, "Post processing for fused deposition modeling parts with acetone vapour bath," IFAC-PapersOnLine 49(31), 42–48 (2016).
  <sup>6</sup>A. P. Valerga, M. Batista, S. R. Fernandez-Vidal, and A. J. Gamez, "Impact of
- <sup>6</sup>A. P. Valerga, M. Batista, S. R. Fernandez-Vidal, and A. J. Gamez, "Impact of chemical post-processing in fused deposition modelling (FDM) on polylactic acid (PLA) surface quality and structure," Polymers 11(3), 566 (2019).
- <sup>7</sup>R. B. Kristiawan, F. Imaduddin, D. Ariawan, Ubaidillah, and Z. Arifin, "A review on the fused deposition modeling (FDM) 3D printing: Filament processing, materials, and printing parameters," Open Eng. **11**(1), 639–649 (2021).
- <sup>8</sup>E. L. Gilmer, D. Miller, C. A. Chatham, C. Zawaski, J. J. Fallon, A. Pekkanen, T. E. Long, C. Williams, and M. Bortner, "Model analysis of feedstock behavior in fused filament fabrication: Enabling rapid materials screening," Polymer 152, 51–61 (2018).

- <sup>9</sup>A. Das, E. L. Gilmer, S. Biria, and M. J. Bortner, "Importance of polymer rheology on material extrusion additive manufacturing: Correlating process physics to print properties," ACS Appl. Polym. Mater. 3(3), 1218–1249 (2021).
- <sup>10</sup>T. A. Osswald, J. Puentes, and J. Kattinger, "Fused filament fabrication melting model," Addit. Manuf. 22, 51–59 (2018).
- <sup>11</sup>X. Gao, S. Qi, X. Kuang, Y. Su, J. Li, and D. Wang, "Fused filament fabrication of polymer materials: A review of interlayer bond," Addit. Manuf. 37, 101658 (2021).
- <sup>12</sup>A. Yadav, P. Rohru, A. Babbar, R. Kumar, N. Ranjan, J. S. Chohan, R. Kumar, and M. Gupta, "Fused filament fabrication: A state-of-the-art review of the technology, materials, properties and defects," Int. J. Interact. Des. Manuf. 17, 2867 (2023).
- <sup>13</sup>G. H. McKinley, W. P. Raiford, R. A. Brown, and R. C. Armstrong, "Nonlinear dynamics of viscoelastic flow in axisymmetric abrupt contractions," J. Fluid Mech. 223(1), 411 (1991).
- <sup>14</sup>M. S. Oliveira, P. J. Oliveira, F. T. Pinho, and M. A. Alves, "Effect of contraction ratio upon viscoelastic flow in contractions: The axisymmetric case," J. Non-Newtonian Fluid Mech. 147(1), 92–108 (2007).
- <sup>15</sup>F. P. Baaijens, "Numerical analysis of start-up planar and axisymmetric contraction flows using multi-mode differential constitutive models," J. Non-Newtonian Fluid Mech. 48(1–2), 147–180 (1993).
- <sup>16</sup>J. P. Rothstein and G. H. McKinley, "Extensional flow of a polystyrene Boger fluid through a 4:1:4 axisymmetric contraction-expansion," J. Non-Newtonian Fluid Mech. 86(1), 61–88 (1999).
- <sup>17</sup>J. Rothstein and G. McKinley, "The axisymmetric contraction-expansion: The role of extensional rheology on vortex growth dynamics and the enhanced pressure drop," J. Non-Newtonian Fluid Mech. **98**(1), 33–63 (2001).
- <sup>18</sup>F. Pimenta, K. Toda-Peters, A. Q. Shen, M. A. Alves, and S. J. Haward, "Viscous flow through microfabricated axisymmetric contraction/expansion geometries," *Exp. Fluids* **61**(9), 204 (2020).
- <sup>19</sup>R. J. Poole, "Inelastic and flow-type parameter models for non-Newtonian fluids," J. Non-Newtonian Fluid Mech. **320**, 105106 (2023).
- <sup>20</sup>R. Mendes, P. Fanzio, L. Campo-Deaño, and F. Galindo-Rosales, "Microfluidics as a platform for the analysis of 3D printing problems," Materials 12, 2839 (2019).
- <sup>21</sup>T. Schuller, P. Fanzio, and F. Galindo-Rosales, "Analysis of the importance of shear-induced elastic stresses in material extrusion," Addit. Manuf. 57, 102952 (2022).
- <sup>22</sup>S. de Vries, T. Schuller, P. Fanzio, and F. Galindo-Rosales, "Pressure drop nonlinearities in material extrusion additive manufacturing: A novel approach for pressure monitoring and numerical modeling," Addit. Manuf. **80**, 103966 (2024).
- <sup>23</sup>A. Bellini, S. Guçeri, and M. Bertoldi, "Liquefier dynamics in fused deposition," J. Manuf. Sci. Eng. **126**(2), 237–246 (2004).
- <sup>24</sup>M. P. Serdeczny, R. Comminal, M. T. Mollah, D. B. Pederson, and J. Spangenberg, "Numerical modeling of the polymer flow through the hot-end in filament-based material extrusion additive manufacturing," Addit. Manuf. 36, 101454 (2020).
- <sup>25</sup>A. A. Mishra, A. Momin, M. Strano, and K. Rane, "Implementation of viscosity and density models for improved numerical analysis of melt flow dynamics in the nozzle during extrusion-based additive manufacturing," Prog. Addit. Manuf. 7(1), 41–54 (2022).
- <sup>26</sup>P. Latko-Durałek, K. Dydek, and A. Boczkowska, "Thermal, rheological and mechanical properties of PETG/rPETG Blends," J. Polym. Environ. 27(11), 2600–2606 (2019).
- 27 T. Swetham, K. M. M. Reddy, A. Huggi, and M. N. Kumar, "A critical review on of 3D printing materials and details of materials used in FDM," Int. J. Sci. Res. Sci. Eng. Technol. 3, 353–361 (2017), available at https://ijsrset.com/ IJSRSET173299.
- <sup>28</sup>R. Krache and I. Debbah, "Some mechanical and thermal properties of PC/ABS blends," Mater. Sci. Appl. 2(5), 404–410 (2011).
- <sup>29</sup>C. Bierögel, "Materials symbols," in Polymer Solids and Polymer Melts, Polymer Solids and Polymer Melts-Mechanical and Thermomechanical Properties of Polymers (Springer, 2014), pp. 16–24.
- 30C. Bierögel and W. Grellmann, "Quasi-static tensile test-tensile properties of thermoplastics-data," in *Polymer Solids and Polymer Melts, Polymer Solids and*

Polymer Melts-Mechanical and Thermomechanical Properties of Polymers (Springer, 2014), pp. 88-99.

- <sup>31</sup>K. Sharma, "Effect of FFF process parameters on density and mechanical properties of PET-G and carbon fiber reinforced PET-G composites," Master's thesis (University of Manitoba, Canada, 2021).
- <sup>32</sup>B. Robertson, R. L. Thompson, T. C. B. McLeish, and I. Robinson, "Theoretical prediction and experimental measurement of isothermal extrudate swell of monodisperse and bidisperse polystyrenes," J. Rheol. 61(5), 931–945 (2017).
- <sup>33</sup>F. J. Galindo-Rosales, M. A. Alves, and M. S. N. Oliveira, "Microdevices for extensional rheometry of low viscosity elastic liquids: A review," Microfluid. Nanofluid. 14(1), 1–19 (2013).
- <sup>34</sup>R. Garritano and J. Berting, "Polymer melt and elastomer extension fixture," US patent US7096728B2 (29 August 2006).
- <sup>35</sup>A. Franck, see https://tinyurl.com/55e8puhh for "Extensional viscosity of polyolefin's and polystyrene;" accessed 29 November 2021.
- 36 A. Franck, see https://tinyurl.com/2p8h4sxn for "The ARES-EVF: Option for measuring extensional viscosity of polymer melts;" accessed 29 November 2021.
- 37F. Pimenta and M. Alves, see https://github.com/fppimenta/rheoTool for "rheoTool" (2016).
- <sup>38</sup>F. Morrison, Understanding Rheology, edited by R. F. Boyer (Oxford University Press, 2001).
- <sup>39</sup>M. Stępień, G. Y. Choong, D. S. D. Focatiis, and L. Figiel, "Modeling non-linear rheology of PLLA: Comparison of Giesekus and Rolie-Poly constitutive models," Int. J. Biobased Plast. 2(1), 13–28 (2020).
- <sup>40</sup>A. E. Likhtman and R. S. Graham, "Simple constitutive equation for linear polymer melts derived from molecular theory: Rolie-Poly equation," J. Non-Newtonian Fluid Mech. **114**(1), 1–12 (2003).
- <sup>41</sup>T. John, M. Mowbray, A. Alalwyat, M. Vousvoukis, P. Martin, A. Kowalski, and C. Fonte, "Machine learning for viscoelastic constitutive model identification and parameterisation using large amplitude oscillatory shear," arXiv:2312.13793 (2023)
- parameterisation using large amplitude oscillatory shear," arXiv:2312.13793 (2023). <sup>42</sup>T. Schuller, see https://github.com/T-Schuller/foamScripts for "foamScripts" (2023).
- <sup>43</sup>M. F. Ashby, "Materials selection—The basics," in *Materials Selection in Mechanical Design*, 4th ed., edited by M. F. Ashby (Butterworth-Heinemann, Oxford, 2011), Chap. 5, pp. 97–124.
- <sup>44</sup>V. Tirtaatmadja and T. Sridhar, "A filament stretching device for measurement of extensional viscosity," J. Rheol. 37(6), 1081–1102 (1993).
- <sup>45</sup>S. L. Anna, G. H. McKinley, D. A. Nguyen, T. Sridhar, S. J. Muller, J. Huang, and D. F. James, "An interlaboratory comparison of measurements from filament-stretching rheometers using common test fluids," J. Rheol. 45(1), 83– 114 (2001).
- <sup>46</sup>R. J. E. Andrade, A. R. Jacob, F. J. Galindo-Rosales, L. Campo-Deaño, Q. Huang, O. Hassager, and G. Petekidis, "Dilatancy in dense suspensions of model hard-sphere-like colloids under shear and extensional flow," J. Rheol. 64(5), 1179–1196 (2020).
- <sup>47</sup>A. Bach, H. K. Rasmussen, and O. Hassager, "Extensional viscosity for polymer melts measured in the filament stretching rheometer," J. Rheol. 47(2), 429–441 (2003).
- <sup>48</sup>Ad Hoc Committee on Official Nomenclature and Symbols, "Official symbols and nomenclature of The Society of Rheology," J. Rheol. 57(4), 1047–1055 (2013).

- <sup>49</sup>F. T. Trouton, "On the coefficient of viscous traction and its relation to that of viscosity," Proc. Roy. Soc. London, Ser. A 77(519), 426–440 (1906).
- 50J. Wisniak, "Frederick Thomas Trouton: The man, the rule, and the ratio," Chem. Educ. 6(1), 55–61 (2001).
- <sup>51</sup>J. M. Dealy and K. F. Wissbrun, *Extensional Flow Properties and Their Measurement* (Springer, Dordrecht, The Netherlands, 1999), pp. 231–268.
- <sup>52</sup>C. Gabriel and H. Münstedt, "Strain hardening of various polyolefins in uniaxial elongational flow," J. Rheol. 47(3), 619–630 (2003).
- <sup>53</sup>H. Münstedt, "Various features of melt strain hardening of polymeric materials in uniaxial extension and their relation to molecular structure: Review of experimental results and their interpretation," Rheol. Acta **62**(7), 333–363 (2023).
- <sup>54</sup>F. Pimenta and M. Alves, "Stabilization of an open-source finite-volume solver for viscoelastic fluid flows," J. Non-Newtonian Fluid Mech. 239, 85–104 (2017).
- <sup>55</sup>OpenCFD Ltd, see https://www.openfoam.com/ for "OpenFOAM<sup>®</sup>" (2019).
- <sup>56</sup>M. Alves, P. Oliveira, and F. Pinho, "Numerical methods for viscoelastic fluid flows," Annu. Rev. Fluid Mech. **53**(1), 509–541 (2021).
- <sup>57</sup>J. Ortega-Casanova, M. Jimenez-Canet, and F. Galindo-Rosales, "Numerical study of the heat and momentum transfer between a flat plate and an impinging jet of power law fluids," Int. J. Heat Mass Transfer 141, 102–111 (2019).
- <sup>58</sup>R. Thompson, P. R. Souza Mendes, and M. Naccache, "A new constitutive equation and its performance in contraction flows," J. Non-Newtonian Fluid Mech. 86(3), 375–388 (1999).
- <sup>59</sup>G. Mompean, R. Thompson, and P. Souza Mendes, "A general transformation procedure for differential viscoelastic models," J. Non-Newtonian Fluid Mech. 111(2), 151–174 (2003).
- 60 A. Fakhari, C. Fernandes, and F. J. Galindo-Rosales, "Mapping the volume transfer of graphene-based inks with the gravure printing process: Influence of rheology and printing parameters," Materials 15(7), 2580 (2022).
- <sup>61</sup>H.-C. Tseng, "The competing role of shear and extension-induced first normal stress differences within a mixed flow for a viscoelastic fluid," Korea-Aust. Rheol. J. **35**, 307 (2023).
- <sup>62</sup>M. A. Alves and R. J. Poole, "Divergent flow in contractions," J. Non-Newtonian Fluid Mech. 144(2-3), 140-148 (2007).
- <sup>63</sup>A. Groisman and V. Steinberg, "Elastic turbulence in a polymer solution flow," Nature 405(6782), 53–55 (2000).
- <sup>64</sup>R. G. Larson, "Turbulence without inertia," Nature 405(6782), 27–28 (2000).
- <sup>65</sup>S. Peng, J.-y. Li, Y.-l. Xiong, X.-y. Xu, and P. Yu, "Numerical simulation of twodimensional unsteady Giesekus flow over a circular cylinder," J. Non-Newtonian Fluid Mech. 294, 104571 (2021).
- <sup>66</sup>B. P. Heller, D. E. Smith, and D. A. Jack, "Effects of extrudate swell and nozzle geometry on fiber orientation in fused filament fabrication nozzle flow," Addit. Manuf. 12, 252–264 (2016).
- <sup>67</sup>D. F. James and C. A. Roos, "Pressure drop of a Boger fluid in a converging channel," J. Non-Newtonian Fluid Mech. 293, 104557 (2021).
- <sup>68</sup>M. Tomé, M. Araujo, J. Evans, and S. McKee, "Numerical solution of the Giesekus model for incompressible free surface flows without solvent viscosity," J. Non-Newtonian Fluid Mech. **263**, 104–119 (2019).
- <sup>69</sup>T. Borrvall and J. Petersson, "Topology optimization of fluids in Stokes flow," Numer. Methods Fluids 41(1), 77-107 (2003).
- <sup>70</sup>J. L. White, "Dynamics of viscoelastic fluids, melt fracture, and the rheology of fiber spinning," J. Appl. Polym. Sci. 8(5), 2339–2357 (1964).