

A two-step modelling approach for plasma reactors-experimental validation for CO₂ dissociation in surface wave microwave plasma

Moreno, Sergio H.; Stankiewicz, Andrzej I.; Stefanidis, Georgios D.

DOI

[10.1039/c9re00022d](https://doi.org/10.1039/c9re00022d)

Publication date

2019

Document Version

Accepted author manuscript

Published in

Reaction Chemistry and Engineering

Citation (APA)

Moreno, S. H., Stankiewicz, A. I., & Stefanidis, G. D. (2019). A two-step modelling approach for plasma reactors-experimental validation for CO₂ dissociation in surface wave microwave plasma. *Reaction Chemistry and Engineering*, 4(7), 1253-1269. <https://doi.org/10.1039/c9re00022d>

Important note

To cite this publication, please use the final published version (if applicable). Please check the document version above.

Copyright

Other than for strictly personal use, it is not permitted to download, forward or distribute the text or part of it, without the consent of the author(s) and/or copyright holder(s), unless the work is under an open content license such as Creative Commons.

Takedown policy

Please contact us and provide details if you believe this document breaches copyrights. We will remove access to the work immediately and investigate your claim.

**A two-step modelling approach for plasma reactors –
experimental validation for CO₂ dissociation in surface wave
microwave plasma.**

Sergio H. Moreno^a, Andrzej I. Stankiewicz^a, Georgios D. Stefanidis^{b,}*

^a *Intensified Reaction & Separation Systems, Process & Energy Laboratory,
Delft University of Technology, Leeghwaterstraat 39, 2628 CB, Delft, The
Netherlands*

^b *Chemical Engineering Department, Katholieke Universiteit Leuven,
Celestijnenlaan 200f, 3001 Leuven (Heverlee), Belgium*

** Corresponding author: Georgios D. Stefanidis, e-mail:
georgios.stefanidis@kuleuven.be*

Abstract

Plasma reactors have the potential to enable CO₂ utilization technologies and so there is need to investigate their performance from a chemical or process engineering perspective. Multiphysics models are excellent tools to carry out this analysis; however, practical engineering models of plasma reactors are limited. Herein a two-step modelling approach for plasma reactors is presented. In the first step, a 2D plasma reactor model with a simple chemistry is used to characterize the discharge. The result of this step is used in the second step to develop a global (volume averaged) model of the reactor with the actual chemistry. The approach is applied in the case of CO₂ dissociation in a non-thermal surface wave microwave plasma reactor. Preliminary calculations reveal the need to include the vibrationally enhanced dissociation of CO₂ in the chemistry of the model. Reduced vibrational kinetics are employed for this purpose by introducing the fictitious species CO₂*. The model predictions are compared to experimental results to validate the model and obtain insight into the performance of the reactor. In comparison to the experimental results the conversions obtained with the model are underestimated between 11% and 25%. The dominant dissociation paths in the plasma reactor are also identified. Further calculations are performed to show the importance of an approximate description of the power deposition. Limitations of the approach are discussed as well, especially those with major contribution to the discrepancies between experimental and modelling results.

Keywords

CO₂ dissociation, plasma model, microwave plasma, plasma reactor

1. Introduction

The utilization of CO₂ emerges as a promising approach in the blend of solutions to cope with two major challenges confronted by human society nowadays, global warming and low-carbon circular economy. Among the CO₂ utilization alternatives, the concept of solar fuels stands out, as the surplus in green electricity is used to produce synthetic fuels from CO₂. Thus, the limitations of renewable sources with respect to their unsteady nature are removed by storing the surplus of green electricity as a fuel that can be used in high demand periods.

Microwave plasma has the potential to enable this technology due to its particular characteristics that allow for efficient splitting of the CO₂ molecule, reaching energy efficiencies up to 90% ¹. The mechanism behind the efficient dissociation of CO₂ is the vibrationally enhanced dissociation, in which the vibrational energy of highly excited states in the asymmetric vibrational mode can decrease the activation energy of the dissociation reaction. That way, the endothermic reaction is carried out efficiently, breaking the very stable CO₂ molecule. The importance of vibrational excitation for achieving an efficient dissociation in diatomic and triatomic molecules has already been known for decades ^{2,3}. In a nutshell, under adequate conditions, the low-lying asymmetric vibrational states get excited by electron collisions and they transfer their energy to higher vibrational states thus creating an overpopulation of highly energetic states that can easily dissociate. This is claimed to be the most efficient dissociation mechanism; a detailed description can be found elsewhere ^{1,4}.

After some years in the shadows, the CO₂ dissociation by means of non-thermal plasma has recently been brought back to the spotlight, mainly due to the crucial need to find solutions to the aforementioned challenges ⁵. From the modelling point of view, research groups in Antwerp, Bari and Lisbon have been working on the fundamental understanding of the physical and chemical processes taking place in the plasma. For this purpose, the Boltzmann equation for the electrons is solved together with detailed kinetic models that involve specific interactions between distinct energy states of the molecules ⁶⁻¹¹. From the experimental point of view, various techniques have recently been used to gain new insights into the effect of different plasma configurations, operating conditions and gas compositions on the behaviour of CO₂-containing plasmas ¹²⁻²¹. Despite these efforts, not all processes taking place inside the plasma, or involved in the dissociation, are fully understood and crucial data required for modelling, such as cross sections or rate constants, are not available.

Given the potential of the technology, it is beneficial to investigate its performance from a chemical or process engineering point of view. Thus, there is need for practical engineering plasma models that consider dimensionality and transport, and ultimately allow for integration of a plasma reactor to a process system. In this document, we describe a two-step modelling approach for plasma reactors, applied to the specific case of CO₂ dissociation in a non-thermal surface wave microwave plasma reactor. The work is continuation of our previous published research on the matter ^{12,13,22}. In the first step, the two-dimensional axisymmetric Argon plasma model, developed in ¹³, is used to characterize the discharge by identifying the power losses, the deposited power density patterns and the time and length scales as well as by performing a qualitative analysis of the plasma and process variables. These results are then used in the second step to develop the model of the CO₂ plasma reactor. During the process, the need to include the vibrationally enhanced dissociation in the chemistry of the model is identified. For this purpose, the methodology for the reduction of vibrational kinetics in non-equilibrium microwave plasma presented in ²² is used. The final model predictions are compared to our previously published experimental results ¹² to validate the model and get insight into the performance of our lab-scale reactor. The reader is referred to ^{12,13,22} for further details on the reduction methodology, the experimental setup and the Argon model.

2. First Step: Power deposition and discharge characterization

The energy required for the CO₂ dissociation comes from the microwave power, which is transferred to the electrons and from these to other species. It reaches the highest values inside the surface wave launcher (Surfatron), where most of the microwave power is deposited, and decreases downstream. An estimate of the power deposition per unit volume (deposited power density) can be obtained from our previously developed two-dimensional model of an Argon plasma ¹³.

The physics of this self-consistent model involve variables whose times and lengths scales differ widely in magnitude, making the non-linear system of equations numerically challenging to solve. Simple chemistries, such as Argon, are preferred in this first step as they allow for characterization the discharge without adding much more complexity to the system of equations. The opposite is true for complex chemistries, such as CO₂ dissociation, for which vibrationally excited states must be included in the non-thermal plasma model. The kinetics of vibrationally excited states lead to very high gradients and rates during the solution

of the system of equations as well as numerical instabilities early in the simulation that impede the solution of equations.

The Argon model was slightly modified to account for the heat removal from the reactor. In our experimental setup the cooling system consisted of cooling water at 5 °C flowing inside the Surfatron and compressed air at 20 °C blowing inside the cavity (between the Surfatron and the quartz tube). A detailed modelling of the cooling system is outside the scope of the present work. Thus, for the sake of simplicity the inner wall temperature of the quartz tube was fixed to a specific value.

Simulations at the experimental conditions of the pure CO₂ dissociation reported in ¹² were performed in the Argon model to investigate the power deposition in the reactor. In the experiments, the microwave power input was 150 W, the pressure 20 mbar, the inlet temperature 300 K and the inlet flowrate 100, 200 and 300 sccm. The simulations were carried out in a time dependent solver until 0.02 s, which is sufficient time for the process to reach steady state. The results of the simulation for an inlet flowrate of 300 sccm and a tube inner wall temperature of 300 K are shown in Figures 1-4. Qualitatively similar results were obtained for the other flowrates. The analysis of the results is only performed in the axial direction due to its relevance with the second step of the approach.

Figure 1 shows the steady state average values of the electron density, electron temperature and gas temperature as a function of z (axial coordinate). These profiles are obtained by integrating the variables in the radial and angular directions and dividing the result over the cross section of the quartz tube. The steady state for these variables is obtained at ~0.006 s, given their direct relation with the electron kinetics, which are characterized by very short timescales. The steady state for the average velocity and the pressure is reached later, at 0.016 s (profiles shown in Figure 2).

The steady state of the average deposited power density is shown in Figure 3. This profile remains constant after 0.006 s, when the plasma variables have also reached their steady states. However, the portion of the profile corresponding to the Surfatron body (between 38 and 118 mm) stabilizes earlier in the simulation, at ~0.001 s. In this zone, the plasma is ignited and most of the power is deposited.

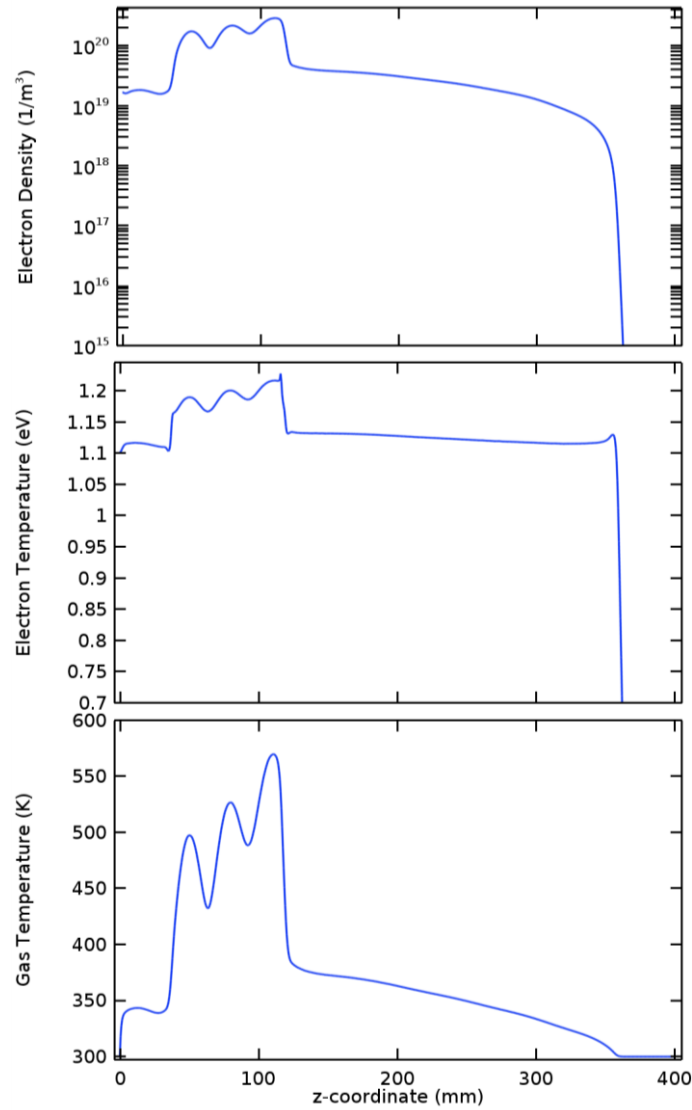


Fig. 1. Electron density (top), electron temperature (middle) and gas temperature (bottom) profiles at steady state (0.006 s). These profiles were obtained using the Argon model ¹³ for a flowrate of 300 sccm, inlet temperature of 300 K, inner wall temperature of 300 K, outlet pressure of 20 mbar and a microwave power input of 150 W. (1 eV \approx 11600 K)

In a surface wave discharge, the generated plasma serves as a propagating medium for the surfaces waves that are created and shaped inside the surface wave launcher (Surfatron). These electromagnetic waves travel axially in both directions inside the plasma while feeding it with their power ²³. This can be easily seen in Figure 3, where the power density decreases as the electromagnetic waves travel through the plasma and completely vanishes when the plasma does as well (see Figure 1). The power density oscillations, also observed in Figure 3, are related to the variations in the magnitude of the surface wave electric field and, particularly, its axial component. Inside the plasma the axial component of the electric field

dominates over the radial component, thus having a larger contribution to the power deposition. Outside of the plasma, the radial component dominates²⁴. It can also be seen that all variables exhibit fluctuations driven by the power deposition fluctuations inside the Surfatron body.

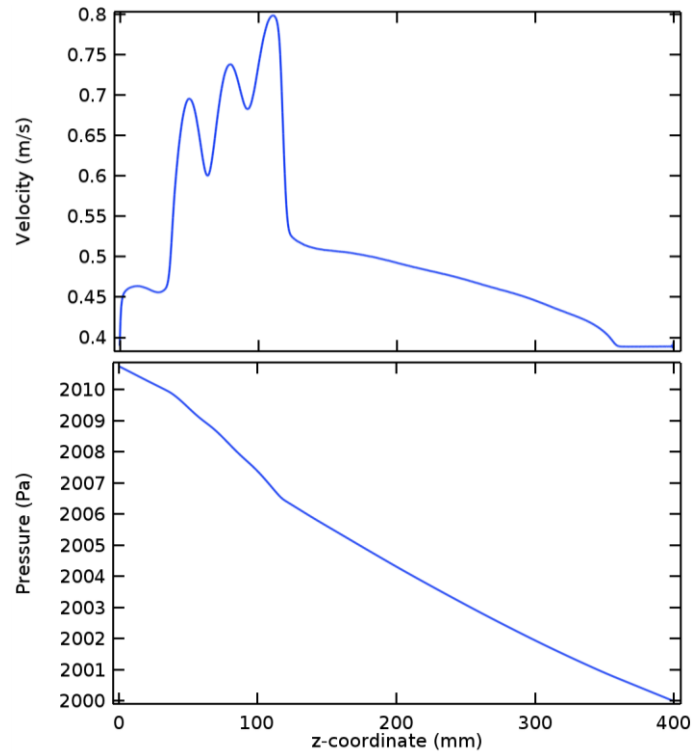


Fig. 2. Velocity (top) and pressure (bottom) profiles at steady state (0.016 s). Argon model at the same conditions given in Figure 1.

Electrons are the driving force in a plasma, they take energy from the microwaves before transferring it to the heavy species. The behaviour of the variables in Figures 1 and 2 can be explained in simple terms from the variations seen in Figure 3. The microwave power energizes the electrons, increasing their mean energy, which is proportional to the electron temperature. High ionization rates are obtained at high electron temperatures and therefore high electron densities are located at zones of high deposited power densities. Conversely, more power can be deposited in zones of high electron densities. The electrons subsequently transfer their energy to the Argon species via elastic and inelastic collisions, which ultimately leads to a local increase of the gas temperature where high electron densities are located. Similarly, the velocity increases at zones of high temperatures due to the local expansion of the gas. For this ideal gas, the variation between the temperature and the velocity is roughly linear given the very low pressure drop. At higher local velocities the pressure drop increases,

but for the entire reactor it remains low and almost linear with the tube length, as expected for this laminar flow.

The total power deposited in the plasma is 121.8 W, which corresponds to the area below the curve of Figure 3 multiplied by the quartz tube cross section. This value is smaller than the 150 W of microwave power input to the Surfatron due to the leakage of microwaves. Figure 4 shows the time average power flow in the positive radial and z directions at the edge of the Surfatron body, where most of the microwave leak takes place. The addition of a waveguide at the Surfatron outlet has proven to be successful in limiting these power losses, thereby increasing the overall performance of the reactor for the case of CO₂ reduction with hydrogen

13.

Another important quantity is the 89.4 W of power that is deposited inside the Surfatron body, within a length of approximately 8 cm. This gives an average power density of 8.9×10^7 W/m³, which is enough to ignite and sustain the plasma. The remaining 32.4 W are deposited at considerably lower power densities, with an average power density of 9.5×10^6 W/m³ over 27 cm of plasma (approximately 35 cm of total Argon plasma length according to Figure 1).

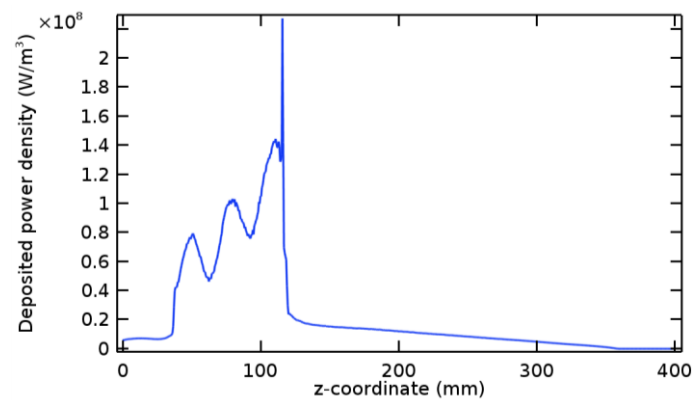


Fig. 3. Deposited power density profile at steady state (0.006 s). Argon model at the same conditions given in Figure 1. The power density peak seen at 116 mm is related to the intense electric field formed at this point due to the Surfatron design (see small protrusion at the bottom of Figure 4).

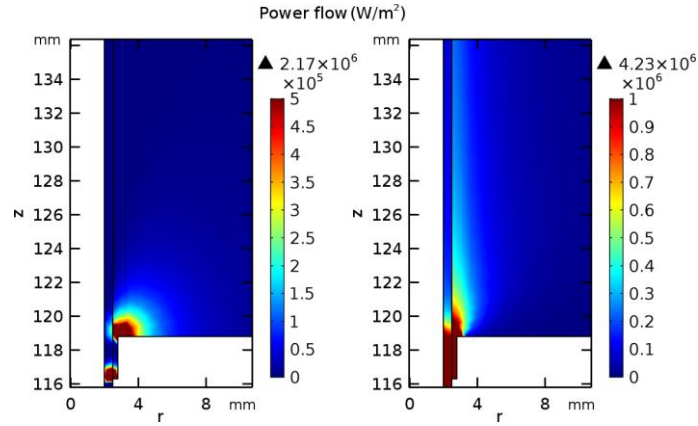


Fig. 4. Time average power flow (0 to 0.02 s) in the positive radial direction (left) and positive z direction (right). Argon model at the same conditions given in Figure 1.

Figure 5 shows the evolution of the power deposition in time, distinguishing the total deposited power from the power deposited into the Surfatron body. These two quantities reach their steady state values at approximately the same time as the plasma variables do (0.006 s) and their difference is established at the early stages of the discharge.

Additional simulations were performed for the lowest experimental inlet flowrate and a higher wall temperature (results summarized in Table 1). It is concluded that in our setup for an Argon plasma at the conditions of the CO₂ dissociation experiments, approximately 80% of the power input is deposited into the plasma and 20% is lost to the surroundings. Moreover, 60% of the power input is deposited effectively at high power densities, while 20% is gradually deposited at low power densities. The latter plays a role in sustaining the plasma, although its effectiveness in this regard is considerably inferior for a molecular plasma, due to the internal degrees of freedom of the molecules (mainly vibration at low electron temperatures). Molecular plasmas are highly collisional in comparison to atomic plasmas; consequently the electron temperature is lower and decays faster in space and time. Therefore, in the so-called afterglow, the small amount of energy gained by the electrons at low power densities is predominantly transferred to vibrational states (of CO₂, CO and O₂ molecules in a CO₂ plasma) and ultimately to heat, further increasing the temperature and the relaxation rates.

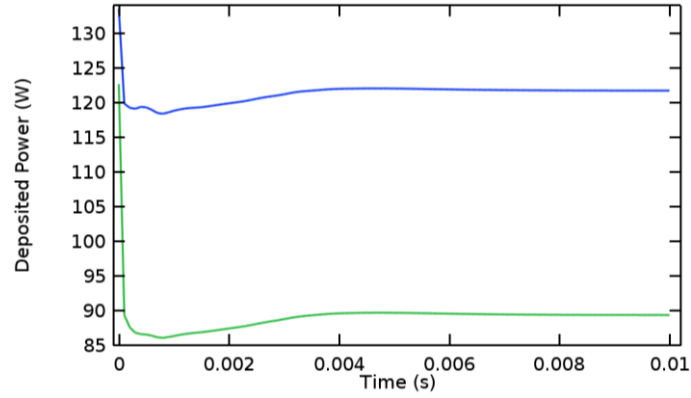


Fig. 5. Deposited microwave power over time. Blue: total deposited power, green: deposited power inside the Surfatron body (at high power densities). Argon model at the same conditions given in Figure 1.

Table 1. Deposited power and deposition efficiencies at selected inlet flowrates and wall temperatures T_w . The results were obtained with the Argon model for an inlet temperature of 300 K, outlet pressure of 20 mbar and a microwave power input of 150 W. SB: Surfatron body.

Flowrate (sccm)	T_w (K)	Total P_{dep} (W)	Deposition eff. (%)	$P_{dep, SB}$ (W)	SB-Deposition eff. (%)
100	300	123.1	82%	91.1	61%
100	600	126.0	84%	92.7	62%
300	300	121.8	81%	89.4	60%
300	600	125.9	84%	92.6	62%

The quartz tube temperature has a minor effect on the power deposition according to the results shown in Table 1. The real temperature of the inner wall is clearly not uniform along the reactor, but measurements indicated that it ranged from 50 to 90 °C downstream of the Surfatron¹². A rough estimation of the surface plasma/inner reactor wall temperature was also done by means of thermal imaging, showing temperatures as high as 600 K at the Surfatron outlet¹³. The variation of the deposited power is shown to be small within the range of these temperatures.

To illustrate the approach, a profile similar to that of Figure 3 is used as input to the global model for CO₂ dissociation. Using a profile based on the results of the Argon model is more descriptive than a power input value as it gives information on where and how the power is deposited into the plasma. This information is necessary for the modelling of the reactor, given its direct relation with the plasma variables. Furthermore, it is also closer to reality than assuming, for instance, a uniform power deposition in the plasma.

The simplified deposited power density profile used in the CO₂ model is designed to be easier to construct and adjust to the CO₂ plasma, while retaining the main characteristics of the profile shown in Figure 3 that is, a high and oscillating power density inside the Surfatron body and a lower and approximately linearly decaying power density outside of it. The deposited power density profile, $P_{d,den}(z)$, can be computed using the following equation, in which r_i is the inner radius, L_p is the length of the plasma and P_{dep} is the total deposited power computed from the power input and the deposition efficiency.

$$\iiint_V P_{d,den} dV = \pi r_i^2 \int_{L_p} P_{d,den}(z) dz = P_{dep} \quad (1)$$

3. Second step: Global model in a Lagrangian approach

In a so-called global model the variables are averaged over the reactor volume, removing the spatial dependence in the equations. Thus, the equations to solve are simplified to the much simpler rate equations, such as the following equation for the conservation of species:

$$\frac{dn_i}{dt} = R_{prod,i} - R_{loss,i} \quad (2)$$

where the rates of production and loss of a species i is given by the chemical reactions.

The electron temperature is computed by the following equations

$$e \frac{dn_\varepsilon}{dt} = R_\varepsilon + P_{d,den} + R_{ion}(\varepsilon_e + \varepsilon_i) \quad (3)$$

$$T_e = \frac{2}{3} \bar{\varepsilon} = \frac{2 n_\varepsilon}{3 n_e} \quad (4)$$

Where e is the elementary charge, n_ε the electron energy density, R_ε the electron energy loss over all electron impact reactions (see Table 4), $P_{d,den}$ the deposited power density, R_{ion} the rate of ion losses to the walls (see Table 8, reaction RS3), $(\varepsilon_e + \varepsilon_i)$ the mean energy lost per electron-ion pair lost to the wall (see Section 3.3), $\bar{\varepsilon}$ the mean electron energy and n_e the electron density, which is computed from the electroneutrality assumption.

These time-dependent equations can be used in a Lagrangian description to obtain a one-dimensional model of the plasma reactor. In this approach, it is assumed that the reactor behaves as a plug flow reactor and a perfectly mixed volume element is tracked in the time

domain as it flows throughout the reactor. There is no flow entering or leaving the volume element. The microwave power is deposited in the volume element depending on its position according to the profile computed from equation 1. The velocity of the element is computed from the flowrate and process conditions, and it is integrated to find its position. This also allows to transform the results of the global model from the time domain into the space domain, i.e. the axial coordinate. In Section 4 all results are conveniently given in the space domain, as functions of z and not time. Figure 6 illustrates the approach.

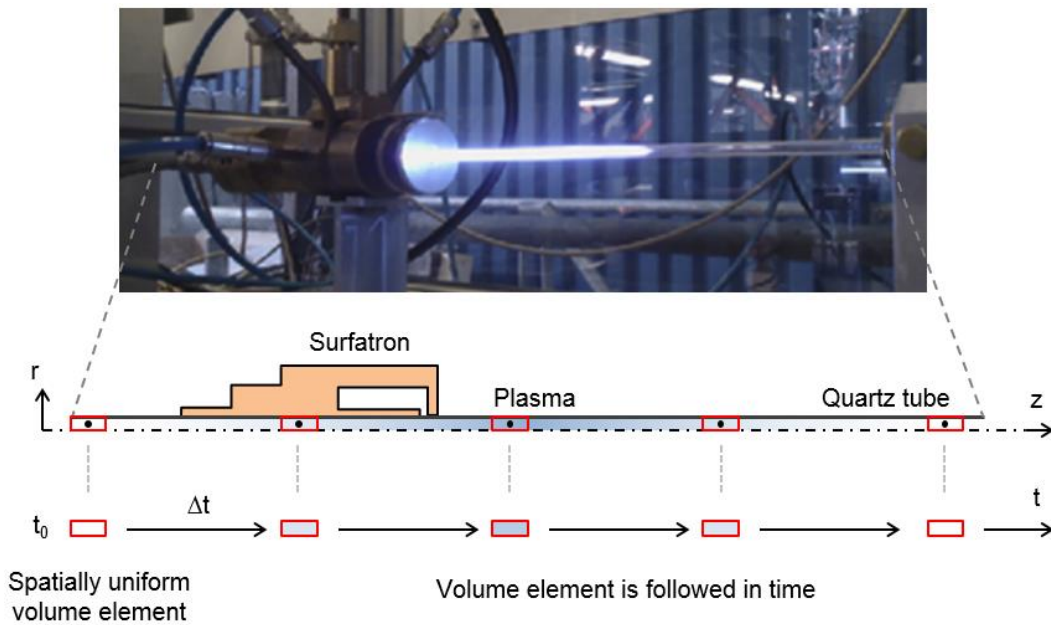


Fig. 6. Approach for modelling CO_2 dissociation in a microwave plasma reactor. Top: Experimental setup used in ¹², middle: Two-dimensional axisymmetric sketch of the reactor ¹³, bottom: Approach used in this work.

Radial and angular variations of the variables inside the reactor are neglected by using this approach. The volume element is axisymmetric, with a radius equal to the inner radius of the quartz tube used in the experimental setup, 2 mm. The length of the quartz tube is approximately 40 cm from the starting point of the surface wave launcher (Surfatron) to the sampling point for the mass spectroscopy analysis used for the quantification of the gas composition. Tubing of 3 mm inner radius and 2.5 m length connects the sampling point to the mass spectrometer.

This simple model can predict the plasma and process variables within reasonable agreement while using much less computational resources than a two-dimensional model. The COMSOL

Multiphysics' Plasma Module was used for the implementation of the global model. A detailed explanation of the equations solved in this module can be found elsewhere ²⁵, herein only brief explanations are provided when needed. The following subsections describe the most relevant aspects of the global model.

3.1. Species

The species included in the CO₂ model are listed in Table 2. These consist of neutral, excited and charged species. CO₂ and the products of its dissociation comprise the neutral species. Excited states refer to the internal degrees of freedom of CO₂ used in the calculation of the electron temperature and the fictitious species CO₂* ²², which groups all levels in the asymmetric vibrational mode of the CO₂ molecule. As mentioned before, highly excited states in this vibrational mode are involved in the vibrationally enhanced dissociation of CO₂.

Table 2. Species considered in the CO₂ model.

Type	Species
Neutral ground states	CO ₂ , CO, O, O ₂
Vibrationally excited states	CO ₂ v _i , CO ₂ *
Electronically excited states	CO ₂ e ₁ , CO ₂ e ₂
Charged species	CO ₂ ⁺ , O ⁻ , e

Vibrational and electronically excited states are only included for CO₂, considering that it is the initial and dominant species in the discharge and therefore it has the highest influence in the electron kinetics. Table 3 lists the excited states along with their energy levels and statistical weights. The vibrational state of a CO₂ molecule is given by three quantum numbers (*i j k*) describing the vibrational levels in the symmetric stretching, symmetric bending and asymmetric stretching modes, respectively. The symmetric bending levels are degenerate as the bending can take place in orthogonal planes, having, for a vibrational level *j* a degeneracy of *j* + 1. In addition, the symmetric levels ((*i* + 1) *j k*) and (*i* (*j* + 2) *k*) are coupled due the proximity of their energy levels, implying that they coexist and therefore are usually grouped into a single species. The statistical weights given in Table 3 refer to the total degeneracy of the species. In the case of CO₂v₈, the statistical weight was computed considering the coupled symmetric levels with a maximum energy slightly lower than the energy threshold of the excitation cross section. The electronically excited species are assumed to be non-degenerate. Lastly, two charged species besides electrons are considered, the positive ion CO₂⁺ and the negative ion O⁻. The production/consumption of these two

species is coupled to the electron density due to the electroneutrality assumption. Lower electron densities are obtained at a higher production of O^- and the opposite is true for CO_2^+ .

Table 3. Excited states included in the CO_2 model. The species and their energies are based on ¹⁰.

Species	Vibrational states	Threshold (eV)	Statistical Weight
CO_2v_1	(0 1 0)	0.083	2
CO_2v_{2a}	(0 2 0)	0.167	3
CO_2v_{2b}	(1 0 0)	0.167	1
CO_2v_3	(0 3 0) + (1 1 0)	0.252	6
CO_2v_4	(0 0 1)	0.291	1
CO_2v_{5a}	(2 0 0)	0.339	1
CO_2v_{5b}	(0 4 0) + (1 2 0) + (0 1 1)	0.339	10
CO_2v_6	(0 5 0) + (2 1 0) + (1 3 0) + (0 2 1) + (1 0 1)	0.422	12
CO_2v_{7a}	(3 0 0)	0.505	1
CO_2v_{7b}	(0 6 0) + (2 2 0) + (1 4 0)	0.505	15
CO_2v_8	(0 n 0) + (n 0 0)	2.500	256
CO_2e_1	-	7.0	1
CO_2e_2	-	10.5	1

3.2. Reactions

The set of reactions is based on our previous work and has been updated according to the species, which now include a negative ion and more excited states. The reactions are mainly elementary two-body reactions and few three-body reactions. They are further divided into electron impact reactions, vibrational energy transfer reactions, reactions between neutral species, reactions involving charged species and surface reactions. Tables 4-8 show these reactions.

The energy gained by the electrons from the electromagnetic fields is transferred to other species through electron impact reactions. Their rate constants are given as functions of the mean electron energy in the form of tabulated data. The cross sections used for the calculations are given in the references of Table 4. These cross sections were integrated with a Maxwellian Electron Energy Distribution Function (EEDF) for mean electron energies up to 10 eV. It is known that the EEDF is in general non-Maxwellian and the rate constants of electron impact processes can be overestimated due to this assumption, particularly for high energy processes. To illustrate this, the rate constant for the direct electron impact dissociation (RX15 in Table 4) can be overestimated up to an order of magnitude for low electron temperatures (~ 0.7 eV), when compared to the result obtained by solving the Two-Term Approximation of the Boltzmann equation. For higher electron temperatures (~ 2 eV),

the rate constant is overestimated by less than 40%. The same comparison for the vibrational excitation of the first asymmetric level (low energy process, RX6 in Table 4) gives an overestimation of around 20% for an electron temperature of 0.7 eV. For higher electron temperatures (>1.8 eV), the deviation is only 1%. Nevertheless, it is very important to remark that different values of the mean electron energy are obtained when the energy conservation equation for the electrons (equation 3) is solved with rates computed with a Maxwellian EEDF and a non-equilibrium EEDF. Therefore, the overestimations mentioned before do not represent the error induced in the rates of the electron impact processes by assuming a Maxwellian EEDF. Indeed, the error is expected to be smaller considering the higher mean electron energies required for a non-equilibrium EEDF to achieve an ionization rate comparable to that obtained with a Maxwellian EEDF. The electron temperature determining the Maxwellian EEDF is computed using equations 3 and 4.

Table 4. Electron impact reactions. Rate constants computed from the cross sections of the references, except for reactions RX16 and RX22 which are given directly (see notes).

No	Process	Reaction	Ref	Note
RX1	Elastic scattering	$e + \text{CO}_2 \rightarrow e + \text{CO}_2$	10	A
RX2	Dissociative attachment	$e + \text{CO}_2 \rightarrow \text{CO} + \text{O}^-$	10	
RX3a	Vibrational excitation	$e + \text{CO}_2 \rightarrow e + \text{CO}_2\nu_1$	10	
RX3b	Superelastic deexcitation	$e + \text{CO}_2\nu_1 \rightarrow e + \text{CO}_2$	10	
RX4a	Vibrational excitation	$e + \text{CO}_2 \rightarrow e + \text{CO}_2\nu_{2a}$	10	
RX4b	Vibrational excitation	$e + \text{CO}_2 \rightarrow e + \text{CO}_2\nu_{2b}$	10	
RX5	Vibrational excitation	$e + \text{CO}_2 \rightarrow e + \text{CO}_2\nu_3$	10	
RX6	Vibrational excitation	$e + \text{CO}_2 \rightarrow e + \text{CO}_2\nu_4$	10	
RX7a	Vibrational excitation	$e + \text{CO}_2 \rightarrow e + \text{CO}_2\nu_{5a}$	10	
RX7b	Vibrational excitation	$e + \text{CO}_2 \rightarrow e + \text{CO}_2\nu_{5b}$	10	
RX8	Vibrational excitation	$e + \text{CO}_2 \rightarrow e + \text{CO}_2\nu_6$	10	
RX9a	Vibrational excitation	$e + \text{CO}_2 \rightarrow e + \text{CO}_2\nu_{7a}$	10	
RX9b	Vibrational excitation	$e + \text{CO}_2 \rightarrow e + \text{CO}_2\nu_{7b}$	10	
RX10	Vibrational excitation	$e + \text{CO}_2 \rightarrow e + \text{CO}_2\nu_8$	10	
RX11	Electronic excitation	$e + \text{CO}_2 \rightarrow e + \text{CO}_2e_1$	10	
RX12	Electronic excitation	$e + \text{CO}_2 \rightarrow e + \text{CO}_2e_2$	10	
RX13	Total ionization	$e + \text{CO}_2 \rightarrow 2e + \text{CO}_2^+$	10	
RX14a	Vibrational excitation	$e + \text{CO}_2 \rightarrow e + \text{CO}_2^*$	22	
RX14b	Superelastic deexcitation	$e + \text{CO}_2^* \rightarrow e + \text{CO}_2$	22	
RX15	Electron impact dissociation	$e + \text{CO}_2 \rightarrow e + \text{CO} + \text{O}$	26	B
RX16	Dissociative recombination	$e + \text{CO}_2^+ \rightarrow \text{CO} + \text{O}$	27	C
RX17	Elastic scattering	$e + \text{CO} \rightarrow e + \text{CO}$	28	A
RX18	Elastic scattering	$e + \text{O}_2 \rightarrow e + \text{O}_2$	29	A
RX19	Dissociative attachment	$e + \text{O}_2 \rightarrow \text{O} + \text{O}^-$	29	D
RX20a	Electron impact dissociation	$e + \text{O}_2 \rightarrow e + \text{O} + \text{O}$	29	D,E
RX20b	Electron impact dissociation	$e + \text{O}_2 \rightarrow e + \text{O} + \text{O}$	29	D,F
RX21	Elastic scattering	$e + \text{O} \rightarrow e + \text{O}$	29	G
RX22	Three-body electron attachment	$e + \text{O} + \text{M} \rightarrow \text{O}^- + \text{M}$	30	H

Notes

- A: Computed from the cross section set of the reference.
 B: The total cross section referred as the sum of partial cross sections is used here.
 C: Rate constant given by $2.0 \times 10^{-11} T_e^{-0.5} T_g^{-1}$ (m³/s).
 D: www.lxcat.net, retrieved on November 1, 2017.
 E: Assuming a direct dissociation into ground state Oxygen atoms (³P) from electronic states A ³Σ_u⁺, A ³Δ_u and c ¹Σ_u⁻ with threshold energy of 6 (eV).
 F: Assuming a direct dissociation into ground state Oxygen atoms from the electronic state B ³Σ_u⁻ with threshold energy of 8.4 (eV).
 G: www.lxcat.net, retrieved on August 9, 2018.
 H: Rate constant given by 10⁻⁴³ (m⁶/s). M = CO₂, CO, O₂ or O.

The reactions in Table 4 are: 1) collision processes from a *complete* and *consistent* cross section set for CO₂ (RX1-13), 2) additional processes for CO₂ that make no contribution to equation 3 (RX14,15) and 3) elastic scattering and processes leading to electron losses for the other species. An elastic scattering cross section is computed by subtracting the cross sections of inelastic processes (attachment, excitation and ionization) from the effective momentum transfer cross section.

Table 5. Vibrational energy transfer reactions. Rate constants in (m³/s). M = CO₂, CO or O₂, unless otherwise stated. The rate constants of reactions RV1 and RV2 are computed from the non-thermal degree of the discharge T_V/T , where T_V is the vibrational temperature (see Modelling results and experimental validation).

No	Reaction	Rate constant	Ref
RV1	CO ₂ * + M → v ₁ CO ₂ * + (1-v ₁) CO ₂ + M	$f(T_V/T)$	22
RV2	CO ₂ * + CO ₂ → v ₁ CO ₂ * + (1-v ₁) CO ₂ + CO ₂	$f(T_V/T)$	22
RV3	CO ₂ v ₁ + M ↔ CO ₂ + M	$7.14 \times 10^{-14} \exp(-177T^{-1/3} + 451T^{-2/3})$	31
RV4	CO ₂ v ₄ + CO ₂ ↔ CO ₂ + CO ₂	$0.43 \times 10^{-6} \exp(-407T^{-1/3} + 824T^{-2/3}) +$ $0.86 \times 10^{-6} \exp(-404T^{-1/3} + 1096T^{-2/3}) +$ $1.43 \times 10^{-11} \exp(-252T^{-1/3} + 685T^{-2/3}) +$ $2 \times 2.13 \times 10^{-11} \exp(-242T^{-1/3} + 633T^{-2/3})$	31
RV5	CO ₂ v ₄ + M ↔ CO ₂ + M (M = CO, O ₂)	$0.43 \times 10^{-6} \exp(-407T^{-1/3} + 824T^{-2/3}) +$ $0.86 \times 10^{-6} \exp(-404T^{-1/3} + 1096T^{-2/3}) +$ $1.43 \times 10^{-11} \exp(-252T^{-1/3} + 685T^{-2/3})$	31

Vibrationally excited states created by electron impact reactions are mostly deexcited by collisional processes at moderate and high pressures. In the case of symmetric vibrational states (CO₂v_i, $i \neq 4$), the deexcitation takes place via Vibrational-Translational (VT) relaxation, i.e. the energy stored in the vibrational degree of freedom is transferred to the translational degree of freedom i.e., as heat. The probability of this energy transfer is highest for processes in which one vibrational quantum is transferred and the rate increases as the vibrational level increases. It is therefore assumed that the process takes place in a cascade fashion and the limiting rate is the VT relaxation of the first symmetric vibrational level. The

rate constant of the latter is assumed for the VT relaxation reactions of all symmetric vibrational levels (reaction RV3) and all collision partners M.

For purely asymmetric vibrational levels ($\text{CO}_2\nu_4$, CO_2^*), the deexcitation takes place via VT relaxation and intermode Vibrational-Vibrational relaxation (VV'), where vibrational energy is transferred to the symmetric vibrational modes. However, the vibrational relaxation of the symmetric modes is much faster than the same in the asymmetric mode; it is therefore assumed that any symmetric level formed in the VT or VV' relaxation is immediately relaxed. Purely asymmetric vibrational states are thus involved in their vibrational relaxation processes and the VV' relaxation acts as an additional VT relaxation process. Therefore, the rate constant for the reaction RV4 is the sum of the VT and VV' relaxation rate constants of the reference. Specifically, the first three terms in the expression correspond to the VT relaxation reactions $\text{CO}_2\nu_4 + \text{M} \leftrightarrow \text{CO}_2\nu_i + \text{M} \leftrightarrow \text{CO}_2 + \text{M}$ with $\text{M} = \text{CO}_2$ and the symmetric levels $\text{CO}_2\nu_1$, $\text{CO}_2\nu_{2a} + \text{CO}_2\nu_{2b}$ and $\text{CO}_2\nu_3$ as respective intermediate states. Reaction RV5 corresponds to the analogous VT relaxation reactions for $\text{M} = \text{CO}$ and O_2 . The last term in the expression for the rate constant of reaction RV4 corresponds to the VV' relaxation reactions $\text{CO}_2\nu_4 + \text{CO}_2 \leftrightarrow \text{CO}_2\nu_i + \text{CO}_2\nu_j \leftrightarrow \text{CO}_2 + \text{CO}_2$ with the symmetric levels $\text{CO}_2\nu_1$, $\text{CO}_2\nu_{2a} + \text{CO}_2\nu_{2b}$ or $\text{CO}_2\nu_{2a} + \text{CO}_2\nu_{2b}$, $\text{CO}_2\nu_3$ as intermediate states.

Table 6. Reactions between neutral species. Rate constants in (m^3/s) for two-body reactions and (m^6/s) for three-body reactions. $\text{M} = \text{CO}_2$, CO or O_2 . The rate constants of reactions RN3 and RN4 are computed from the non-thermal degree of the discharge T_V/T , where T_V is the vibrational temperature (see Modelling results and experimental validation).

No	Reaction	Rate constant	Ref
RN1	$\text{CO}_2 + \text{M} \rightarrow \text{CO} + \text{O} + \text{M}$	$4.39 \times 10^{-13} \exp(-65000/T)$	1
RN2	$\text{CO}_2 + \text{O} \rightarrow \text{CO} + \text{O}_2$	$7.77 \times 10^{-18} \exp(-16600/T)$	1
RN3	$\text{CO}_2^* + \text{M} \rightarrow \text{CO} + \text{O} + \text{M}$	$f(T_V/T)$	22
RN4	$\text{CO}_2^* + \text{O} \rightarrow \text{CO} + \text{O}_2$	$f(T_V/T)$	22
RN5	$\text{CO} + \text{O} + \text{M} \rightarrow \text{CO}_2 + \text{M}$	$8.2 \times 10^{-46} \exp(-1510/T)$	32
RN6	$\text{CO} + \text{O}_2 \rightarrow \text{CO}_2 + \text{O}$	$1.23 \times 10^{-18} \exp(-12800/T)$	1
RN7	$\text{O} + \text{O} + \text{M} \rightarrow \text{O}_2 + \text{M}$	$1.27 \times 10^{-44} (T/300)^{-1} \exp(-170/T)$	33

For reactions RV1,2 the rate constants are computed according to the methodology of the reference, i.e. from the state-specific normalized populations and rate constants of the vibrational levels lumped within the fictitious species CO_2^* . In addition, the symmetric levels are replaced by ground state CO_2 for the reasons previously explained. Rate constants for reverse reactions are computed by using the detailed balancing principle. No reverse reactions

are considered for reactions RV1,2 as the highly energetic fictitious species CO_2^* can only be produced by electron collisions.

Thermal dissociation of CO_2 takes place through reactions RN1 and RN2, whereas vibrationally enhanced dissociation takes place through the analogous reactions RN3 and RN4. The rate constants for the reactions RN3,4 are computed by following the approach of the given reference. This approach is also used to compute the enthalpy change in these reactions, as exemplified here for RN3. Figure 7 illustrates the enthalpy change in the dissociation reaction RN1 for specific levels of the asymmetric vibrational mode of CO_2 . For this reaction and this vibrational mode, the vibrational energy decreases the activation energy, which is also the enthalpy change of the reaction.

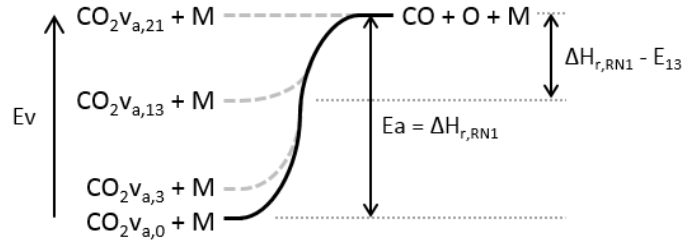


Fig. 7. Enthalpy change of the CO_2 dissociation reaction RN1 for selected asymmetric vibrational levels. The energy barrier of the reaction decreases as the vibrational energy increases up to the dissociation limit of 5.5 eV.

The enthalpy change of the lumped reaction RN3 is computed by adding the heat of the dissociation reactions for all asymmetric vibrational levels (grouped inside CO_2^*) and the result is made equal to the heat of reaction of the lumped reaction, as follows

$$\begin{array}{r}
 \begin{array}{l}
 \text{Reactions of asymmetric levels} \\
 \text{CO}_2 v_{a,21} + \text{M} \rightarrow \text{CO} + \text{O} + \text{M} \\
 \vdots \\
 \text{CO}_2 v_{a,1} + \text{M} \rightarrow \text{CO} + \text{O} + \text{M} \\
 \hline
 \text{CO}_2^* + \text{M} \rightarrow \text{CO} + \text{O} + \text{M}
 \end{array}
 &
 \begin{array}{l}
 \text{Heat of reaction} \\
 [\text{CO}_2^*] n_{21} [\text{M}] k_{RN1,21} (\Delta H_{r,RN1} - E_{21}) \\
 \vdots \\
 [\text{CO}_2^*] n_1 [\text{M}] k_{RN1,1} (\Delta H_{r,RN1} - E_1) \\
 \hline
 [\text{CO}_2^*] [\text{M}] k_{RN3} \Delta H_{r,RN3}
 \end{array}
 \end{array}$$

Therefore, the expression for the enthalpy change of reaction RN3 is

$$\Delta H_{r,RN3} = \frac{\sum n_i k_{RN1,i} (\Delta H_{r,RN1} - E_i)}{\sum n_i k_{RN1,i}} \quad (5)$$

The brackets denote concentration, n_i is the normalized population of the asymmetric vibrational level i , k is the rate constant, ΔH_r the enthalpy change and E_i the vibrational energy of the asymmetric vibrational level i . The enthalpy change of reaction RN4 is computed likewise, from its analogous reaction RN2 and considering that only half of the vibrational energy decreases the activation energy ¹. Any vibrational energy surplus in this case becomes heat of the products.

The remaining reactions between neutrals are recombination reactions producing O₂ and CO₂. Reactions involving charged species are limited to three detachment reactions, releasing electrons from the negative ions O⁻.

Table 7. Reactions involving charged species. Rate constants in (m³/s). M = CO₂, CO or O₂.

No	Reaction	Rate constant	Ref
RI1	O ⁻ + CO → CO ₂ + e	5.5×10^{-16}	34
RI2	O ⁻ + O → O ₂ + e	2.3×10^{-16}	35
RI3	O ⁻ + M → O + M + e	4.0×10^{-18}	36

Ions can also recover a neutral charge in a collision with a wall, as well as excited states can also return to their ground state through the same action. Given the low temperature of heavy species (neutrals, excited and ions), it is assumed that the probability of this grounding event is 1, i.e. every time an excited or charged species collides with a wall it returns to the neutral ground state. This probability is also referred to as the sticking coefficient and is given in Table 8 along with the surface reactions of the model. No surface reaction is considered for the negative ions O⁻ as they are confined in the plasma core due the action of the ambipolar field.

Table 8. Surface reactions for excited and charged species.

No	Reaction	Sticking coefficient	Correction factor	Diffusion length
RS1	CO ₂ v _i → CO ₂	1	1	$\Lambda_{eff,cyl}$
RS2	CO ₂ e _i → CO ₂	1	1	$\Lambda_{eff,cyl}$
RS3	CO ₂ ⁺ → CO ₂	1	h_l, h_r	N/A

The rate constants can be computed from the sticking coefficients by using the following expression ³⁷

$$k_s = \left(\frac{1}{1 - \gamma/2} \right) \frac{\gamma}{4} \sqrt{\frac{8RT}{\pi M_n}} \quad (6)$$

Where γ is the sticking coefficient, the term in parenthesis the Motz-Wise correction for high sticking coefficients and the square rooted term is the thermal velocity of the colliding species. The rate constant for the surface reaction of CO_2^+ is multiplied by a correction factor to take into consideration the effect of ambipolar diffusion (see next section). In the case of neutral species, the total loss rate to the walls is computed from ³⁸

$$\frac{1}{k_l} = \frac{1}{k_D} + \frac{1}{k_s} \quad (7)$$

where k_l is the loss rate, k_D is the diffusion rate of the species to the walls and k_s is the previously defined rate constant for the surface reaction. The loss rate is therefore the contribution of the transport of species to the walls and their reaction when colliding the walls. Naturally, either of these can be the rate limiting step in the process. The diffusion rate is calculated by equation 8 as function of the diffusion coefficient of the species k through the mixture, $D_{k,m}$, the effective diffusion length, Λ_{eff} , and the dimension over which diffusion takes place, V/S .

$$k_D = \frac{D_{k,m} V}{\Lambda_{eff}^2 S} \quad (8)$$

Surface recombination reactions for neutral species are neglected. The sticking coefficients of these reactions cannot be determined intuitively and are difficult to estimate; they are functions of the gas and wall temperatures and strongly depend on the material of the wall and its surface properties ³⁸. Experimentally obtained values are also scarce and not in agreement ^{39,40}. In addition, no significant carbon deposition was observed during the CO_2 dissociation experiments in our setup.

3.3. Transport effects

The effects of transport on energy and mass conservation are treated globally. Momentum conservation is not solved for, viscous effects are disregarded and the pressure is assumed

uniform and constant throughout the reactor (see Figure 2 for the negligible pressure loss of order 10^{-3} in the Argon model).

Diffusion effects are only considered for the surface reactions as the concentration of the reacting species at the wall is not equal to their average concentration. Regarding the excited states, the diffusion coefficients $D_{k,m}$ and the effective diffusion length Λ_{eff} are needed to compute their diffusion rates from equation 8. The calculation of the former is based on the kinetic gas theory and is included in COMSOL's Plasma Module ²⁵. The latter, for a cylindrical reactor of length L_r and inner radius r_i can be estimated as follows ⁴¹

$$\frac{1}{\Lambda_{eff,cyl}^2} = \left(\frac{\pi}{L_r}\right)^2 + \left(\frac{2.405}{r_i}\right)^2 \quad (9)$$

The positive ion diffuses to the walls at a higher rate due to the action of the ambipolar field. The correction factors h_l, h_r for the surface reaction of CO_2^+ are the wall to centre ratios of the species concentration in the z and r dimensions, respectively, and are computed, based on ⁴², from

$$h_l = \frac{n_{l/2}}{n_0} \approx \frac{0.86}{(3 + L_r/2\lambda_i + (0.86L_r u_B/\pi D_a)^2)^{1/2}} \quad (10)$$

$$h_r = \frac{n_r}{n_0} \approx \frac{0.8}{(4 + r_i/\lambda_i + (0.8r_i u_B/2.405J_1(2.405)D_a)^2)^{1/2}} \quad (11)$$

In the above expressions, J_1 is the Bessel function of the first order, λ_i is the ion-neutral mean free path, u_B the Bohm velocity and D_a the ambipolar diffusion coefficient, computed as follows

$$\lambda_i = \frac{1}{n_g \sigma_i} \quad (12)$$

$$u_B \approx \sqrt{\frac{eT_e}{M}} \quad (13)$$

$$D_a \approx D_{\text{CO}_2^+,m} \left(1 + \frac{T_e}{T}\right) \quad (14)$$

where n_g is the density of neutrals, σ_i the total ion-neutral collisional cross section and M the mass of the ion. An average and constant value of 10^{-18} m^2 is assumed for this cross section,

which is within the typical range of values for CO_2^+ transport in its parent gas⁴³. Moreover, it is also assumed that all heavy species are in thermal equilibrium (share the same temperature) and the electronegativity of the discharge is very low $\alpha = n_{O^-}/n_e \ll 1$ and hence the plasma behaves similar to an electropositive discharge.

Regarding heat transfer, it is assumed that heat conduction is the dominant heat transfer mechanism in the plasma⁴⁴. The heat transfer equation therefore corresponds to that of a cylinder with heat generation inside and a constant wall temperature. It can be easily shown that in this case a parabolic temperature profile is obtained and the heat losses and maximum temperature are

$$Q_{loss} = 8\lambda_{mix} \frac{T - T_w}{r_i^2} \quad (15)$$

$$T_{max} = 2T - T_w \quad (16)$$

where λ_{mix} is the thermal conductivity of the gas mixture, computed from the species' mole fractions and thermal conductivities²⁵, which in turn are computed from the Stiel-Thodos equation⁴⁵.

The heat losses are included in the following heat transfer equation to calculate the temperature of the gas in the plasma

$$\rho c_{p,mix} \frac{dT}{dt} = Q_{gen} - Q_{loss} \quad (17)$$

Where ρ is the gas density, $c_{p,mix}$ the specific heat at constant pressure of the gas mixture and Q_{gen} the heat source from reactions. The internal energy lost to the walls by the excited species is normalized per unit volume and added to the heat source from gas phase reactions. Likewise, the ionization energy of the positive ions is also added.

The acceleration induced by the ambipolar field leads to higher kinetic energies in the positive ions. This kinetic energy is $\varepsilon_i = V_s + 0.5T_e$, with the sheath voltage V_s computed as in³⁸

$$V_s = T_e \ln \sqrt{\frac{M}{2\pi m_e}} \quad (18)$$

where m_e is electron mass. Additionally, to preserve the electroneutrality in the plasma, an electron is also lost each time a positive ion is neutralized or “lost” to the walls. The kinetic energy lost per Maxwellian electron is $\varepsilon_e = 2T_e$. The sum of these kinetic energies ($\varepsilon_i + \varepsilon_e$) is also normalized per unit volume and is added to Q_{gen} . This approach ensures that the energy from the microwaves not used in chemical reactions ends up as heat in the plasma.

The contribution of the asymmetric vibrational states to the specific heat of the fictitious species CO_2^* is computed from their vibrational energy. The following equations are used for the calculation

$$\frac{C_{P,vib}}{R} = \frac{C_{V,vib}}{R} + 1 \quad (19)$$

$$C_{V,vib} = \left(\frac{\partial E_{vib}}{\partial T} \right)_V \quad (20)$$

$$E_{vib} = \frac{\sum n_i E_i}{\sum n_i} \quad (21)$$

Where $C_{P(V),vib}$ is the contribution of the asymmetric vibrational mode to the molar specific heat at constant pressure (volume) of CO_2^* , R the universal gas constant, E_{vib} the mean vibrational energy, and n_i and E_i are the population and vibrational energy of the level i , respectively. The reader is referred to ²² for the details regarding the calculation of the energies and populations of the vibrational levels grouped within CO_2^* . The calculation of the enthalpy change in deexcitation reactions of CO_2^* is performed using the computed specific heat for this species.

4. Modelling results and experimental validation

The simplified profile used as input for the CO_2 model is shown in Figure 8. This profile is based on Figure 3 and consists of three peaks of the same magnitude distributed uniformly inside the Surfatron body and a declining power density downstream. The plasma obtained in the CO_2 experiments is shorter than the Argon plasma at the same process conditions, with a total length of approximately 20 cm ^{12,13}. Assuming this value for the plasma length as well as deposition efficiencies of 62% inside the Surfatron body and 21% for the surface wave (refer to Table 1, the value corresponding to $T_W = 600$ K is assumed for the former), the piecewise linear profile is calculated using equation 1. It is also assumed that the power deposition starts

inside the Surfatron body and the profile remains constant within the range of studied flowrates as it was observed in the Argon model.

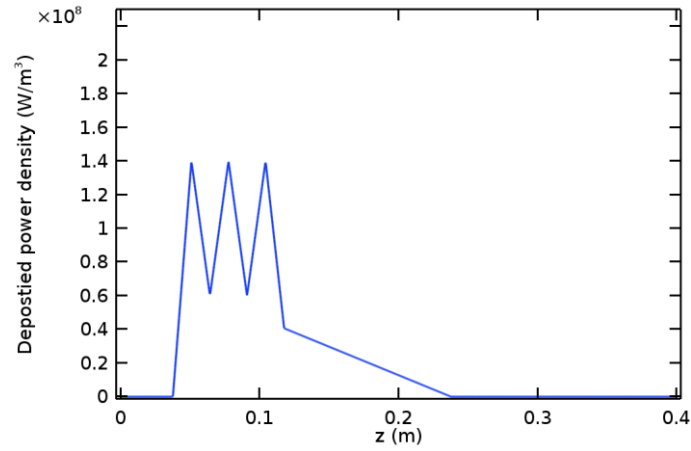


Fig. 8. Deposited power density profile for the CO₂ model. Refer to Figure 3 for the power density profile obtained with the Argon model.

The simulations in the CO₂ model are performed at the same process conditions of the experiments for three different values of the inlet flowrate, 100, 200 and 300 sccm. The pressure is fixed at 20 mbar, the initial (inlet) temperature and the wall temperature are both 300 K and the input power is 150 W. CO₂ is ~100% of the initial composition and the initial mass fractions of the excited species are computed by assuming a Boltzmann distribution. In addition, thermal equilibrium is initially assumed for the electrons and the initial ionization degree (electrons to neutrals ratio) is 10⁻¹⁰. A direct solver is used for the fully coupled system of equations and the solution time is optimized using Anderson acceleration with a dimension of iteration space of 10.

The CO₂ conversion in the plasma reactor as a function of the axial position can be computed with the following expression, where n_{CO_2} is the total density of the CO₂ species and v is the flow velocity.

$$X(z) = 1 - \frac{n_{CO_2}(z)v(z)}{n_{CO_2}(0)v(0)} \quad (22)$$

Several reactions in the model can contribute to the dissociation of the CO₂ molecule. These can be arranged into 5 different paths:

1. Dissociative attachment (RX2, Table 4).

2. Ionization + dissociative recombination (RX13 + RX16, Table 4).
3. Direct electron impact dissociation (RX15, Table 4).
4. Thermal dissociation (RN1,2, Table 6).
5. Vibrationally enhanced dissociation (RX14a, Table 4 + RN3,4, Table 6).

The dashed lines in Figure 9 show the CO₂ conversion computed when the vibrationally enhanced dissociation of CO₂ is not considered. In this case, the conversion at the reactor outlet ($x = 0.4$ m) is 11%, 16% and 31% for 300, 200 and 100 sccm, respectively. In these calculations the direct electron impact dissociation is the dominant path, forming approximately 92% of CO. Dissociative recombination after ionization and dissociative attachment also contribute, forming 5.5% and 2.5% of CO, respectively. Thermal dissociation is orders of magnitude smaller than the other paths due to the relatively low temperatures in the plasma.

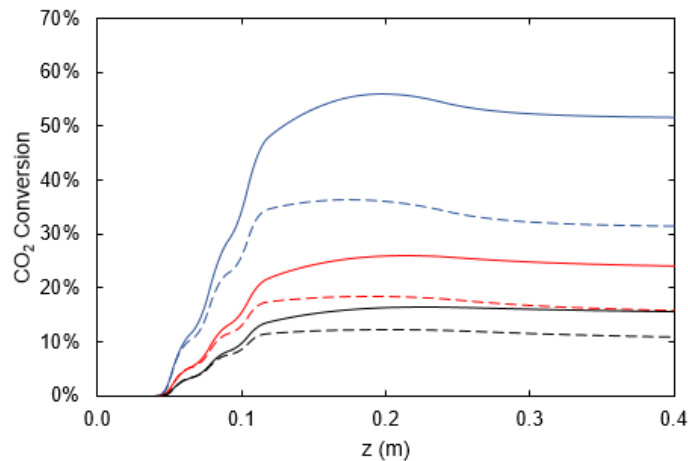


Fig. 9. CO₂ conversion as a function of the axial position in the reactor for 100 (blue), 200 (red) and 300 sccm (black). Results ignoring the vibrationally enhanced CO₂ dissociation are shown in dashed lines. The solid lines correspond to the full model, including the fictitious species CO₂* and its reactions. In all cases, the CO₂ recombination from $x = 0.4$ m until the measuring device located at $x = 2.9$ m is estimated to be less than 1%.

These conversion values are clearly far from the experimental values of 18%, 32% and 66% obtained for the same flowrates, indicating that the vibrationally enhanced dissociation could play a significant role in the dissociation of CO₂. It is worth mentioning that the CO₂ recombination from the reactor outlet to the measuring device is, in all cases, estimated to be

less than 1% and is therefore neglected. Hereinafter, conversion refers to the conversion at the outlet of the reactor unless otherwise stated.

It is possible to estimate the CO₂ dissociation via vibrational excitation by including the fictitious species CO₂* in the model. The stoichiometric coefficients, reaction rates, enthalpy of reactions and specific heat required to include this species in the model are computed from the non-thermal degree by following the methodology presented in ²² (see previous Sections 3.2 and 3.3). This reduction methodology is based on 1) lumping all asymmetric vibrational levels within the fictitious species CO₂*, 2) assuming a Treanor distribution of these levels, 3) using an algebraic approximation based on the Landau-Teller formula to compute the evolution of non-thermal degree in the discharge and 4) employing weighted algebraic expressions to compute the rate constants of reactions involving CO₂*. The application of this methodology results in a substantial simplification regarding the number of reactions and species required to describe the vibrationally enhanced dissociation of CO₂.

The non-thermal degree is an implicit comparison between VV and VT relaxation and is given by the ratio between the vibrational temperature T_V and the gas temperature T . The vibrational temperature is based on the population density of the first vibrational level of the asymmetric mode and is computed from $T_V = E_1/\ln(n_0/n_1)$. An efficient dissociation of CO₂ is possible at low temperatures and high non-thermal degrees, when the vibrational energy is predominantly exchanged between vibrational levels (VV relaxation) instead of being lost as heat (VT relaxation).

The CO₂ model without the fictitious species CO₂* is used to estimate the non-thermal degree at the characteristic time of the VT relaxation, i.e. the time at which VT relaxation kicks in and the evolution of T_V/T follows the trend described in ²². This characteristic time is approximately 1.6×10^{-4} s and it is computed at the initial conditions of the discharge from $\tau_{VT} = (k_{RV4}n_{CO_2})^{-1}$, where k_{RV4} is the rate constant of the VT relaxation reaction RV4 and n_{CO_2} is the population density of CO₂. The non-thermal degree is then computed at 1.6×10^{-4} s after the power deposition starts, giving the approximate values of 3.5, 3.1 and 2.6 for 300, 200 and 100 sccm, respectively.

The results of the full model, including CO_2^* , are shown in the solid lines of Figure 9. The conversion in the plasma reactor is now 16%, 24% and 52% for 300, 200 and 100 sccm, respectively. The absolute increase in the conversion by considering the vibrationally enhanced dissociation is 5%, 8% and 21%, which also correspond to a relative increase of 45%, 50% and 68%, respectively. These numbers confirm that this path plays a significant role and must be considered when modeling the CO_2 dissociation in non-thermal plasmas. In these calculations, the dominant paths for the dissociation are now the direct electron impact dissociation and the vibrationally enhanced dissociation. The dissociative recombination after ionization and dissociative attachment also have minor contributions, whereas thermal dissociation is still negligible.

Table 9 gives the percentage of CO molecules formed by each of the dissociation paths. The direct electron impact dissociation accounts for approximately 55% of the dissociation, while 40% is due to the vibrationally enhanced dissociation. Although not shown in the table, there is an absolute increase in the dissociation for each path as the flowrate decreases, due to an increase in the electron density. However, the dissociation rate for all paths increase differently as the electron temperature increases, modifying the rate constant of the electron impact reactions.

Table 9. Percentage of CO molecules formed per CO_2 dissociation path. Thermal dissociation is orders of magnitude smaller due to the low temperatures of the discharge and is therefore not shown.

Flowrate (sccm)	CO ₂ Dissociation path			
	1 DA	2 I + DR	3 DEID	5 VED
100	1.4%	3.0%	53.2%	42.4%
200	1.5%	2.8%	54.0%	41.7%
300	1.6%	2.8%	56.2%	39.4%

The conversions obtained with the full model are still lower than the experimental values, having relative errors of 11%, 25% and 21%. These deviations can be seen in Figure 10, where the experimental and modelling results are plotted as functions of the flowrate. Given the complexity of modelling plasma and the simplifications taken in the process, the results are considered in fair agreement. Indeed, various elements have influence on the lower conversions obtained in the model, particularly the power deposition. The power deposition efficiencies were characterized from a model of an atomic plasma and are assumed to remain the same for a molecular plasma. However, this is not necessarily true since molecules have

more degrees of freedom and have chemical bonds that can be broken (or formed); therefore, molecular plasmas are more reactive and have more energy channels through which the energy given by the electrons can flow or be stored. In other words, this means that the power deposition in the CO₂ plasma is expected to be higher than the value taken from the Argon model. The calculation of a correction factor for the power deposition in the CO₂ plasma can be problematic due to the complexity of the physics involved in the 2D self-consistent model, e.g. the electromagnetic wave equation inside and outside of the reactor. The formulation of the power deposition depends on the type discharge and the presence of electric arcs can simplify the treatment ⁴⁶.

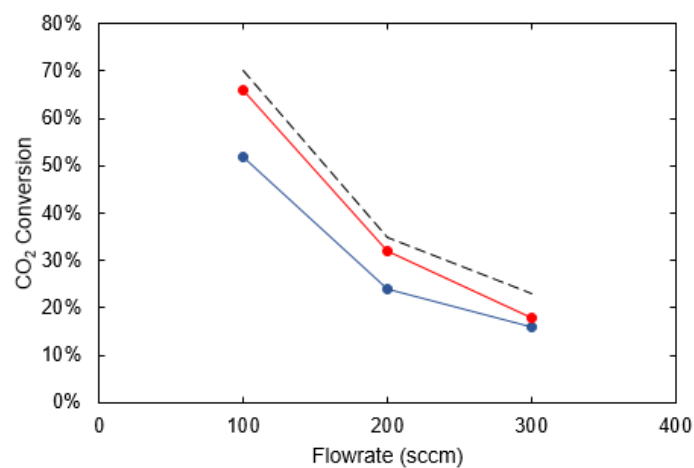


Fig. 10. CO₂ conversion as a function of the flowrate. Red: experimental results, blue: full model simulation results. The dashed line shows the limiting case for the maximum conversion assuming 100% of deposited power and 75% of deposited power inside the Surfatron body.

The dashed line of Figure 10 illustrates the influence of the deposition efficiencies in the conversion. For these calculations, it is assumed that all 150 W of power input are deposited in the plasma, with 75% of it being deposited inside the Surfatron body (approximate ratio of 62/83). The non-thermal degrees are kept constant, implying that these conversions are slightly underestimated. Nevertheless, these results serve as a limiting case, proving that this uncertainty alone can explain the lower conversions in the model. It is to be noted that the power deposition remains lower than 100% in the CO₂ plasma. As we proved experimentally, the addition of a waveguide reduces the power losses and increases the performance of the reactor for the case of CO₂ reduction with hydrogen¹³.

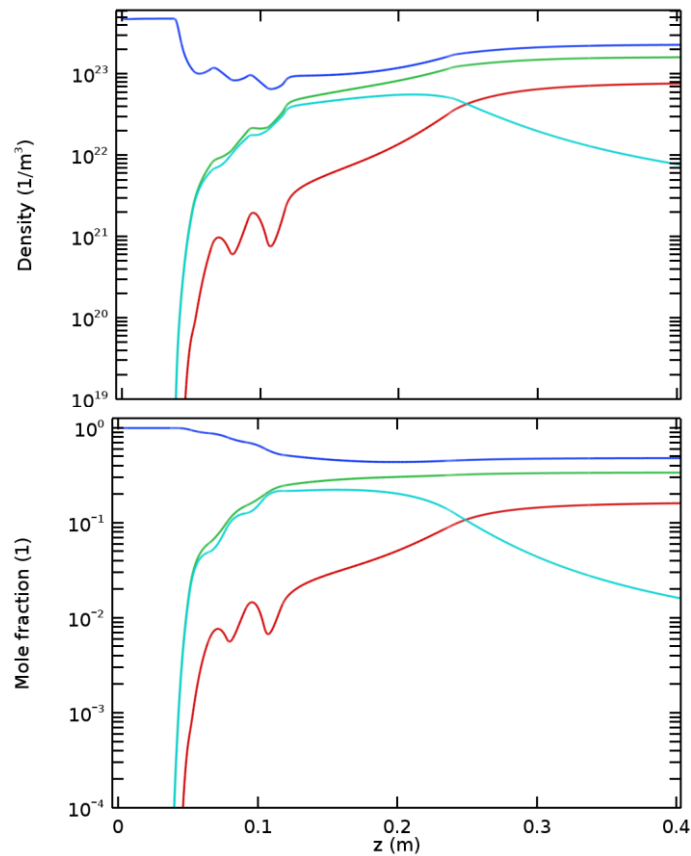


Fig. 11. Densities (top) and mole fractions (bottom) of neutral species as functions of the axial position in the reactor for a flowrate of 100 sccm. Blue: CO₂, green: CO, cyan: O, red: O₂.

The portion of power deposited inside the Surfatron body can also vary, having further influence on the conversion, as most of the CO₂ dissociation takes place there. Figure 11 shows the densities of the neutral species as a function of the axial position in the plasma reactor. The oscillations seen in the graph at the top are partially caused by expansions due to the increase in the gas temperature when power is deposited. This effect is not present in the mole fractions shown in the graph at the bottom, where the remaining fluctuations are then related to the reacting system. In the bottom graph, it is seen that most of the CO₂ dissociation takes place inside the Surfatron body, forming mainly CO and O. O₂ is subsequently formed by the recombination of two O atoms, or in the reaction of CO₂* and O.

The fluctuations still seen in O₂ are located at the peaks of the power deposition profile and are related to electron impact dissociation reactions of O₂. The maximum dissociation of CO₂, corresponding to a maximum conversion of 56%, is slowly reached downstream of the Surfatron; afterwards, recombination takes place and the final conversion of 54% is achieved.

O atoms also recombine into O₂ downstream of the Surfatron, notably past the end of the plasma. The final products are then CO₂, CO and O₂, as expected.

The energy efficiency of the reactor can be computed from the CO₂ conversion, considering that a minimum of 2.93 eV per CO₂ molecule are required for the reaction CO₂ → CO + 1/2 O₂ to take place. The energy input per particle in the plasma, commonly known as Specific Energy Input (SEI), is also used in the calculation, as follows

$$\eta = X \frac{2.93}{\text{SEI}} \quad (23)$$

$$\text{SEI} = \frac{P_{dep} M_{n,inlet}}{e N_A \dot{m}} \quad (24)$$

Where $M_{n,inlet}$ is the mean molar mass at the inlet (44.01 kg/kmol for CO₂), N_A is the Avogadro constant and \dot{m} is the mass flowrate. The energy efficiencies calculated with the model are in agreement with the experimental values; the results are presented in Table 10.

Table 10. Energy efficiency of the plasma reactor for the considered flowrates. The experimental values are taken from ¹², where a power deposition of 150 W is assumed.

Flowrate (sccm)	SEI, model (eV/molecule)	E. Efficiency, model (%)	E. Efficiency, exp. (%)
100	17.3	8.8	8.3
200	8.7	8.1	8.3
300	5.8	7.9	6.8

Assuming 100% of power deposition in the model, as before, the energy efficiencies for the same flowrates increase to approximately 10%, which is still a low value. The reason for this is that the experimental conditions and the reactor itself were not optimized for an efficient dissociation of CO₂, which is achieved at low values of SEI (<2 eV/molecule). At high values of the SEI, such as the ones in Table 10, relatively high electron densities and electron temperatures are obtained, shifting the EEDF away from the vibrational excitation reactions. An efficient dissociation of CO₂ should take place mostly through vibrational excitation, not direct electron impact dissociation with a higher energy requirement. As mentioned before, the latter is the main dissociation path in the Surfatron reactor, leading to low energy efficiencies.

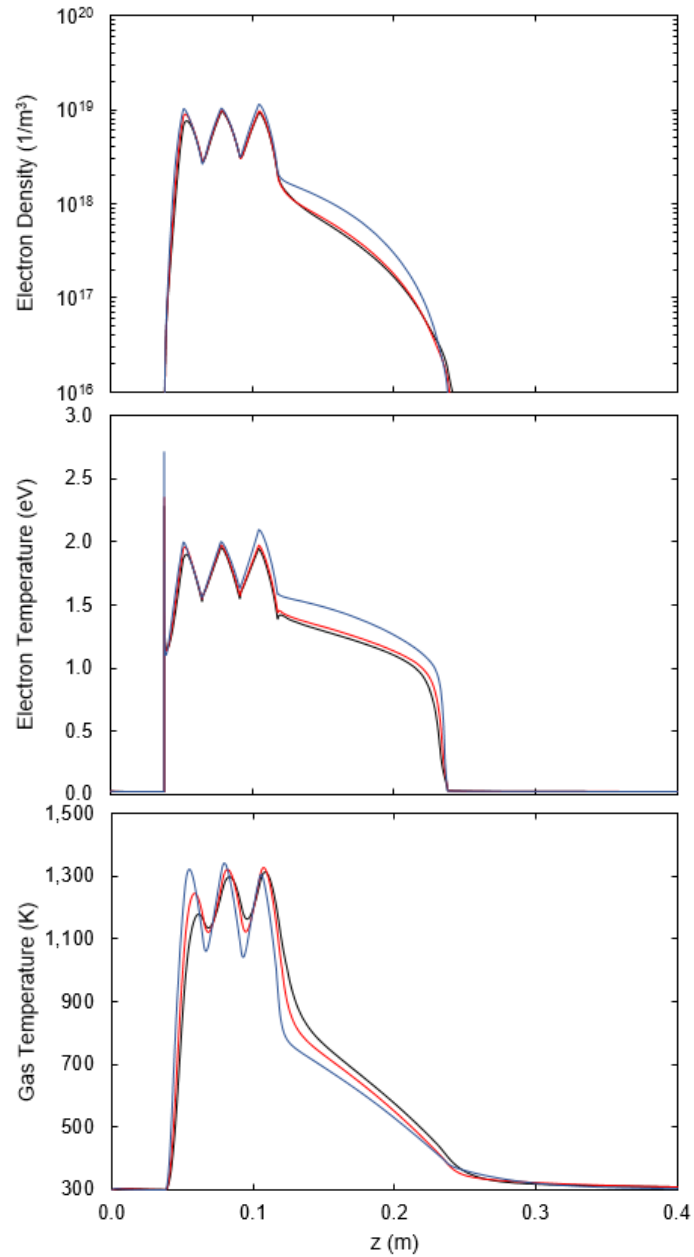


Fig. 12. Electron density (top), electron temperature (middle) and gas temperature (bottom) as a function of the axial position in the reactor for 100 (blue), 200 (red) and 300 sccm (black).

The effect of the SEI is clearly seen in the top and middle graphs of Figure 12, showing that both the electron density and electron temperature increase as the SEI increases (flowrate decreases). Nonetheless, the results for the different flowrates are quite similar and within the range of typical values for non-thermal CO_2 microwave plasmas: $T_e \approx 0.5 - 2$ eV and $n_e \approx 10^{18-20} 1/m^3$. The ionization degree in the plasma is then 10^{-5} inside the Surfatron body and 10^{-6} outside.

Experimental values of the electron density and electron temperature in this reactor were determined downstream of the Surfatron for gas mixtures of H₂ and CO₂ ¹². Electron densities in the order of 10²¹ and 10²⁰ 1/m³ were estimated for H₂:CO₂ ratios of 4 and 3, respectively. Likewise, electron temperatures of 1.3 and 0.7 eV were estimated for H₂:CO₂ ratios of 3 and 1, respectively. Lower electron densities and temperatures are expected for lower mixing ratios ¹¹. These reference values suggest that the computed electron densities are within the expected order of magnitude while the electron temperatures are slightly overestimated (see below discussion on lack of electron transport).

A qualitative match between Figure 1 and Figure 12 is also observed, confirming that these variables follow the power deposition profile. Therefore, given that the variables in Figures 1 and 12 determine the rate of the electron impact reactions, it can be inferred that not only the deposited power, but also the density at which it is deposited has an influence on the results.

The lack of electron transport in the CO₂ model is also evident by comparing the electron densities and electron temperatures of Figure 1 and Figure 12. In the Argon model, a smaller difference is seen between the values inside and outside of the Surfatron body. Furthermore, the slope at which they decrease in the low power density zone is flatter, being virtually horizontal for the electron temperature. Thus, the lack of electron transport in the CO₂ model results in a less uniform plasma with a reduced reactivity due to the rapid decay in the number of electrons.

The average gas temperature, shown at the bottom of Figure 12, does not vary much with the flowrate, except in the first and last peaks of the power deposition. The variations seen in the first peak are related to the electron density, while the CO₂ dissociation explains the variations in the last peak. The CO₂ dissociation is also related to the electron temperature and density variations seen for a flowrate of 100 sccm in Figure 12.

Despite the variations, the maximum average temperature for the flowrates is the same, reaching around 1300 K inside the Surfatron body. Hence, according to equation 16, the maximum gas temperature at the center of the plasma is 2300 K, which is within the range of our previously estimated values for the gas temperature, 2200-2400 K ¹².

It is also possible to verify the previous assumption regarding the electropositive behavior of the plasma. Figure 13 shows that the maximum electronegativity is around 0.2 as the power deposition begins. However, it promptly decays and for most of the plasma, it is in the order of magnitude of 10^{-3} , which agrees with the assumption of a very low electronegativity ($\alpha = n_{O^-}/n_e \ll 1$). This means that there are few negative ions, which are confined at the core of the plasma and their effect on the positive ions can be neglected.

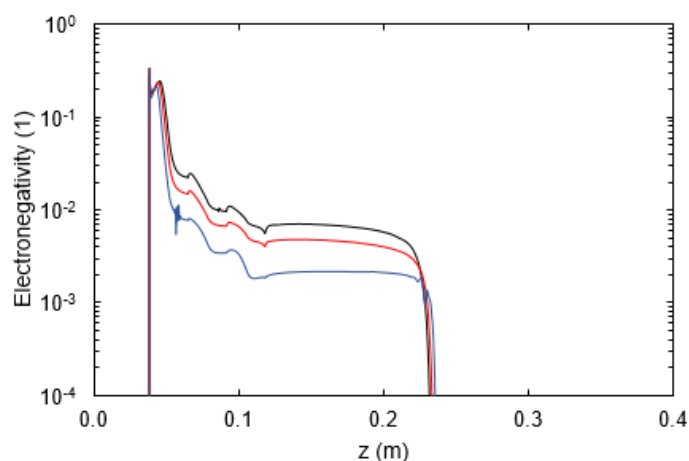


Fig. 13. Electronegativity as a function of the axial position in the reactor for 100 (blue), 200 (red) and 300 sccm (black).

Even though the positive ions are not held back in their movement towards the walls, the rate of surface recombination is two orders of magnitude smaller than the collisional counterpart (dissociative recombination, RX16 Table 4). Thus, most electrons are lost inside the plasma instead of being lost to the walls.

Contrarily, the rates of collisional and surface deexcitation of vibrationally excited species are comparable, with the surface process becoming more important as the vibrational level increases due to the limiting rate assumed for the collisional process. Moreover, the reverse collisional process intensifies the relevance of the surface deexcitation, making its contribution to vibrational deexcitation larger than the collisional counterpart.

The importance of surface reactions in this model is expected from the characteristic diffusion time, which, depending on the computed gas temperature, is estimated in the order of 0.1 - 1 ms. This characteristic time is shorter than the residence time in the plasma reactor, which for 20 cm of plasma is approximately 3.7, 5.7 and 11.6 ms for 300, 200 and 100 sccm,

respectively. Therefore, for such a small reactor and relatively low operating pressure, the species have sufficient time to diffuse and possibly collide with the walls.

For larger reactors, the surface reactions can be neglected considering that their rates scale as $1/r$ compared to the gas phase reactions. In addition, longer characteristic diffusion times are also obtained and fewer species would reach the walls during the short residence times in the reactor.

5. Conclusions

We have developed a two-step modelling approach for plasma reactors, consisting of a plasma characterization step using simple chemistry and a global modelling step using the actual chemistry of interest. Specifically, in the first step, we used a self-consistent two-dimensional axisymmetric Argon plasma model of a laboratory surface wave microwave plasma reactor to characterize the discharge, particularly the power deposition along the reactor. In the second step, the outcome of the first step was used to develop a zero-dimensional volume-averaged CO₂ plasma model, under a Lagrangian description, which represents a one-dimensional model of our experimental setup.

With the global model we showed that the vibrationally enhanced dissociation is a relevant process taking place in the reactor and must be included in the model. For this purpose, we have used the fictitious species CO₂* that groups all levels in the asymmetric vibrational mode of the CO₂ molecule. We also pointed out the significant role of the surface reactions in the deactivation of excited species at the investigated conditions in our plasma reactor. The relevance of the surface reactions should be evaluated according to the reactor design and operating conditions before deciding whether to include them in the modelling process.

The results of the simulations showed CO₂ conversions of 16%, 24% and 52%, for inlet flowrates of 300, 200 and 100 sccm, respectively. The relative increase in the conversion when the vibrationally enhanced dissociation is considered was 45%, 50% and 68%, respectively. With the model we also identified the direct electron impact dissociation and the vibrationally enhanced dissociation as the dominant paths for the CO₂ dissociation in our plasma reactor, accounting for approximately 55% and 40% of CO formation, respectively.

The experimental conversions for the corresponding flowrates of 300, 200 and 100 sccm are 18%, 32% and 66%, respectively. Thus, the agreement between the modelling and experimental values, mentioned in the previous paragraph, is good in view of the complexity involved in modelling non-thermal CO₂ plasma reactors. The experimental validation of the CO₂ plasma variables indicates that the electron densities are close to the expected order of magnitude and the gas temperature is in agreement with the experimentally estimated values. The electron temperatures are slightly overestimated, mainly due to the lack of electron transport in the global model.

The power deposition profile determined with the Argon model was identified as the major source of error, due to the uncertainty of its variation when the plasma is generated in a CO₂ flow, e.g. higher power depositions are expected in a molecular plasma. Despite this, the profile obtained from the Argon model was adopted as it is more descriptive than a power input value and closer to reality than an arbitrarily shaped profile. Using the Argon model, it was determined that 17% of the power input is lost to the surroundings and the remaining power is deposited into the plasma. Moreover, it was identified that 75% of the power deposition occurs inside the Surfatron body, whereas 25% is gradually deposited by the surface waves as they travel axially along the plasma.

Additional simulations showed that the uncertainties regarding the power deposition profile can explain the error obtained in the CO₂ conversion. It is therefore essential to have an approximate description of the power deposition profile, including the deposited power inside the Surfatron reactor, the power of the surface wave, the length of the plasma and the power deposition densities (shape of the profile). It was also shown with both models that the latter can be particularly important as the plasma variables have a fast response and closely follow the same variations.

Further limitations of the global model were also discussed, especially those that can contribute to the discrepancies in the results. Among these are the simplified treatment of the heat transfer inside the reactor body, the simplified treatment of the heat and mass transfer in the radial direction (due to averaging) and the lack of heat and mass transfer (plug flow assumption) in the axial direction (due to the Lagrangian approach).

Despite these limitations, we believe that the two-step modelling approach is valuable for process engineering applications involving design, optimization and verification of plasma reactors and their performance.

Conflicts of interest

There are no conflicts to declare.

References

- 1 A. Fridman, *Plasma chemistry*, Cambridge University Press, 2008.
- 2 V. D. Rusanov, A. a. Fridman and G. V. Sholin, *Uspekhi Fiz. Nauk*, 1981, **134**, 185.
- 3 M. Capitelli, M. Dilonardo and E. Molinari, *Chem. Phys.*, 1977, **20**, 417–429.
- 4 M. Capitelli, C. M. Ferreira, B. F. Gordiets and A. I. Osipov, *Plasma Kinetics in Atmospheric Gases*, Springer Berlin Heidelberg, Berlin, Heidelberg, 2000, vol. 31.
- 5 R. Snoeckx and A. Bogaerts, *Chem. Soc. Rev.*, 2017, **46**, 5805–5863.
- 6 T. Kozák and A. Bogaerts, *Plasma Sources Sci. Technol.*, 2014, **23**, 045004.
- 7 T. Kozák and A. Bogaerts, *Plasma Sources Sci. Technol.*, 2015, **24**, 015024.
- 8 L. D. Pietanza, G. Colonna, G. D'Ammando, A. Laricchiuta and M. Capitelli, *Plasma Sources Sci. Technol.*, 2015, **24**, 042002.
- 9 L. D. Pietanza, G. Colonna, G. D'Ammando, A. Laricchiuta and M. Capitelli, *Phys. Plasmas*, 2016, **23**, 013515.
- 10 M. Grofulović, L. L. Alves and V. Guerra, *J. Phys. D. Appl. Phys.*, 2016, **49**, 395207.
- 11 P. Diomede, M. C. M. van de Sanden and S. Longo, *J. Phys. Chem. C*, 2017, **121**, 19568–19576.
- 12 J. F. de la Fuente, S. H. Moreno, A. I. Stankiewicz and G. D. Stefanidis, *Int. J. Hydrogen Energy*, 2016, **41**, 21067–21077.
- 13 J. F. de la Fuente, S. H. Moreno, A. I. Stankiewicz and G. D. Stefanidis, *Int. J. Hydrogen Energy*, 2017, **42**, 12943–12955.
- 14 W. Bongers, H. Bouwmeester, B. Wolf, F. Peeters, S. Welzel, D. van den Bekerom, N. den Harder, A. Goede, M. Graswinckel, P. W. Groen, J. Kopecki, M. Leins, G. van Rooij, A. Schulz, M. Walker and R. van de Sanden, *Plasma Process. Polym.*, 2017, **14**, 1600126.
- 15 T. Silva, N. Britun, T. Godfroid and R. Snyders, *Plasma Sources Sci. Technol.*, 2014, **23**, 025009.
- 16 L. F. Spencer and a D. Gallimore, *Plasma Sources Sci. Technol.*, 2013, **22**, 015019.
- 17 B. L. M. Klarenaar, M. Grofulović, A. S. Morillo-Candas, D. C. M. van den Bekerom, M. A. Damen, M. C. M. van de Sanden, O. Guaitella and R. Engeln, *Plasma Sources Sci. Technol.*, 2018, **27**, 045009.
- 18 B. Hrycak, M. Jasiński and J. Mizeraczyk, *Acta Phys. Pol. A*, 2014, **125**, 1326–1329.
- 19 M. Jasiński, M. Dors and J. Mizeraczyk, *Int. J. Plasma Environ. Sci. Technol.*, 2008, **2**, 134–139.
- 20 L. M. Martini, S. Lovascio, G. Dilecce and P. Tosi, *Plasma Chem. Plasma Process.*,

- 2018, **38**, 707–718.
- 21 L. M. Martini, N. Gatti, G. Dilecce, M. Scotoni and P. Tosi, *Plasma Phys. Control. Fusion*, 2018, **60**, 014016.
- 22 J. F. de la Fuente, S. H. Moreno, A. I. Stankiewicz and G. D. Stefanidis, *React. Chem. Eng.*, 2016, **1**, 540–554.
- 23 M. Jimenez-Diaz, E. a D. Carbone, J. van Dijk and J. J. a M. van der Mullen, *J. Phys. D. Appl. Phys.*, 2012, **45**, 335204.
- 24 M. Selby and G. M. Hieftje, *Spectrochim. Acta Part B At. Spectrosc.*, 1987, **42**, 285–298.
- 25 COMSOL, *Plasma Module User's Guide*, COMSOL 5.3, 2017.
- 26 L. S. Polak and D. I. Slovetsky, *Int. J. Radiat. Phys. Chem.*, 1976, **8**, 257–282.
- 27 R. E. Beverly, *Opt. Quantum Electron.*, 1982, **14**, 501–513.
- 28 *Phelps database*, www.lxcat.net, retrieved on October 24, 2017.
- 29 L. L. Alves, *J. Phys. Conf. Ser.*, 2014, **565**, 012007.
- 30 H. Shields, A. L. S. Smith and B. Norris, *J. Phys. D. Appl. Phys.*, 1976, **9**, 1587–1603.
- 31 J. A. Blauer and G. R. Nickerson, *A survey of vibrational relaxation rate data for processes important to CO₂–N₂–H₂O infrared plume radiation*, Irvine, California, 1973.
- 32 A. Cenian, A. Chernukho, V. Borodin and G. Śliwiński, *Contrib. to Plasma Phys.*, 1994, **34**, 25–37.
- 33 S. Hadj-Ziane, B. Held, P. Pignolet, R. Peyrous and C. Coste, *J. Phys. D. Appl. Phys.*, 1992, **25**, 677–685.
- 34 T. G. Beuthe and J.-S. Chang, *Jpn. J. Appl. Phys.*, 1997, **36**, 4997–5002.
- 35 J. T. Gudmundsson and E. G. Thorsteinsson, *Plasma Sources Sci. Technol.*, 2007, **16**, 399–412.
- 36 H. Hokazono and H. Fujimoto, *J. Appl. Phys.*, 1987, **62**, 1585–1594.
- 37 R. J. Kee, M. E. Coltrin and P. Glarborg, *Chemically Reacting Flow*, John Wiley & Sons, Inc., Hoboken, NJ, USA, 2003.
- 38 M. A. Lieberman and A. J. Lichtenberg, *Principles of Plasma Discharges and Materials Processing*, John Wiley & Sons, Inc., Hoboken, NJ, USA, 2005.
- 39 A. F. Kolesnikov, I. S. Pershin, S. A. Vasil', evskii and M. I. Yakushin, *J. Spacecr. Rockets*, 2000, **37**, 573–579.
- 40 N. G. Bykova, S. A. Vasil'evskii, A. N. Gordeev, A. F. Kolesnikov, I. S. Fershin and M. I. Yakushin, *Fluid Dyn.*, 1997, **32**, 876–886.

- 41 P. J. Chantry, *J. Appl. Phys.*, 1987, **62**, 1141–1148.
- 42 C. Lee and M. A. Lieberman, *J. Vac. Sci. Technol. A Vacuum, Surfaces, Film.*, 1995, **13**, 368–380.
- 43 L. A. Viehland and E. A. Mason, *At. Data Nucl. Data Tables*, 1995, **60**, 37–95.
- 44 C. M. Ferreira, B. F. Gordiets and E. Tatarova, *Plasma Phys. Control. Fusion*, 2000, **42**, B165–B188.
- 45 L. I. Stiel and G. Thodos, *AIChE J.*, 1964, **10**, 26–30.
- 46 G. Trenchey, S. Kolev, W. Wang, M. Ramakers and A. Bogaerts, *J. Phys. Chem. C*, 2017, **121**, 24470–24479.