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# Experimental and Theoretical Analysis of Vacuum Circuit Breaker Prestrike Effect on a Transformer

Marjan Popov, *Senior Member, IEEE*, René Peter Paul Smeets, *Fellow IEEE*, Lou van der Sluis, *Senior Member, IEEE*, Hans de Herdt and Jan Declercq, *Member IEEE*

**Abstract**— The work presented in this paper deals with the investigation of circuit breaker prestrike effect that occurs during energizing a distribution transformer. An experimental test setup that consists of a supply transformer, a vacuum circuit breaker (VCB), a cable and a test transformer is built, and the prestrikes in the VCB are recorded. The test transformer is a prototype distribution transformer, with installed measuring points along transformer windings in each phase. Voltage oscillations are measured along the windings and transformer terminals. The transformer is modeled by lumped parameters extracted from telegrapher's equations in discrete form.

Voltage oscillations during switching-in operations are recorded and calculated with and without a cable installed between the VCB and the transformer. Computed voltages show good agreement with the measured voltages. Described method can be used by transformer manufacturers to estimate voltage wave forms during switching or lightning, to provide useful information for insulation coordination studies, and to investigate resonance effects in transformer windings.

**Index Terms**— Transformer, vacuum circuit breaker, switching tests, modeling.

## I. INTRODUCTION

IT is well known that during switching highly inductive loads like transformers and motors, under specific conditions multiple restrikes in the circuit breaker can occur. Multiple restrikes are fast voltage surges which proceed along the cable and reach the transformer or motor terminals. Because of different surge impedances at terminals, a wave reflection and absorption takes place. Voltage oscillations which proceed toward windings are continuously superposed by new voltage waves from new upcoming surges. Hence, voltage waveforms along the transformer winding within a particular time interval can have very different amplitude and rate of rise. Their oscillations contain a broad frequency range

which can be from a few kilohertz up to a few megahertz. These are unwanted phenomena which cause deterioration and failure of the equipment insulation. Almost one third of all motor failures occur because of fast switching surges [1]. Switching surges which enter the windings are non-linearly distributed [2]. Besides, sometimes high inter-turn overvoltages can take place which stress the thin insulation and accelerate its failure. So far, a lot of work has been done on transformer and motor switching [3-9]. However, voltage transients are measured on transformer terminals and prediction of the voltage distribution along the windings is difficult to be done. In [10] a computer model for motor windings is described which is applied during sequential pole closing [11]. It is also applied for determination of inter-turn voltages during energizing a motor with a VCB [12].

Most of the time, the geometry of the windings and dimensions are not known. Furthermore, a proper model based on transformer geometry and type of windings is difficult to develop. Consideration of the frequency-dependent losses is another problem.

So far, there was successful work done on transformer modeling. In [13, 14], a hybrid model based on transmission line theory was successfully applied to describe the wave propagation in large shell-type transformers. An accurate approach for modeling transformers and motors is done by applying the so called vector fitting [15]. This model is based on the measured frequency admittance matrix of the transformer, the elements of which are admittances measured from any provided measuring point in the transformer windings [16]. The advantage of the latter model is that it gives the possibility to use existing simulation software like EMTP.

In this work, the prestrike effect during energizing the transformer was investigated. Voltage waveforms on transformer terminals are measured and they are used as an input parameter to the transformer model. A lumped-parameter model based on discretized telegraphist's equations is applied [17]. It was found that this approach can be successfully applied for computation of voltages along the windings, even for matrices with large dimensions (100x100). Computations are done in frequency domain, and time domain solutions are provided by applying inverse continuous Fourier transform [18]. Measurements and computations are also done with and without applying a cable between the VCB and

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transformer. The computations are verified by laboratory measurements.

## II. TEST TRANSFORMER AND ITS REPRESENTATION

### A. Transformer description

The test transformer is a three-phase layer-type transformer. However, the computation and measurements of the voltages along the windings is done per phase whilst other two phases are not connected to the studied phase.



Figure 1. Test transformer.

TABLE I  
TRANSFORMER DATA

Transformer Power	630 kVA
Transformer ratio	15375 V / 400 V
No-load losses	770 W
No-load current	0.3 %
Number of layers (HV side)	10
Number of turns in a layer	~ 140
Inner radius of HV winding	135.3 mm
External radius of HV winding	163.3 mm
Inner radius of the LV winding	97 mm
Wire diameter	3.0 mm
Double wire insulation	0.1 mm
Distance between layers	0.4 mm
Coil's height	425 mm

The primary transformer winding consists of layers with approximately 140 turns. The transformer is equipped with special measuring points in each phase. In phase A, measuring points are installed at the 3<sup>rd</sup> and the 5<sup>th</sup> turn. In phase B, the measuring points are at the 290<sup>th</sup> and the 580<sup>th</sup> turn, and in phase C, the measuring points are at the 444<sup>th</sup> and the 888<sup>th</sup> turn. All measuring points can be directly reached as it can be seen from Figure 1. The most important parameters of the transformer are summarized in Table I.

### B. Transformer representation

Studied transformer is a layer-type prototype transformer particularly produced for this research. The transformer has measuring points installed in each phase. The tank and the oil are removed so that an easy access to the windings can be provided. The transformer with capacitances and inductances

is represented in Figure 2. The inductance matrix is formed by the self inductances of a group of turns and mutual inductances between the turns. The capacitance matrix is formed by capacitances between layers and capacitances from the top and the bottom of the layers to the transformer tank.

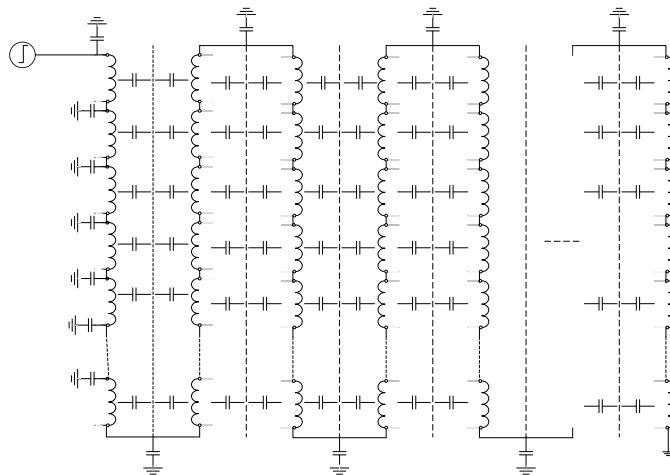


Figure 2. Transformer capacitances and inductances

The transformer represented in Figure 2 can be simplified by re-arranging the capacitances. To do this, we will consider an equipotential surface between the layers [2]. In this way, one can divide a group of winding in the following way. Half of the capacitance between coils is added to the edges of the coils [19-21]. Then, it is assumed that there is an equipotential line in the middle of the coil, so that the capacitance between coils can be added as a cross-over capacitance at each coil with a value equal to the half of the value of the total capacitance. The description is given in Figure 3.

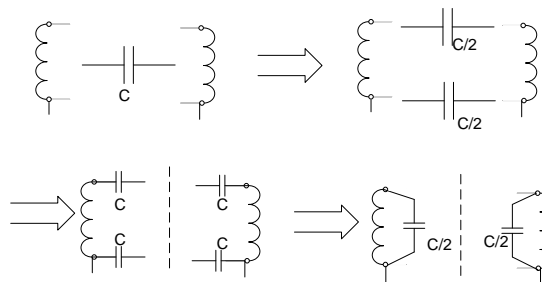


Figure 3. Simplification of a section of the transformer.

Figure 4 represents the simplification of the transformer model from Figure 2, and Figure 5 is the final model of the transformer. It has to be pointed out that the cross-over capacitances which belong to the first and last layer are a half of the cross-over capacitance of the other layers. Capacitances to ground in this case are small because the surface of the top and bottom of the coil is small. They are estimated as less than 1 pF.

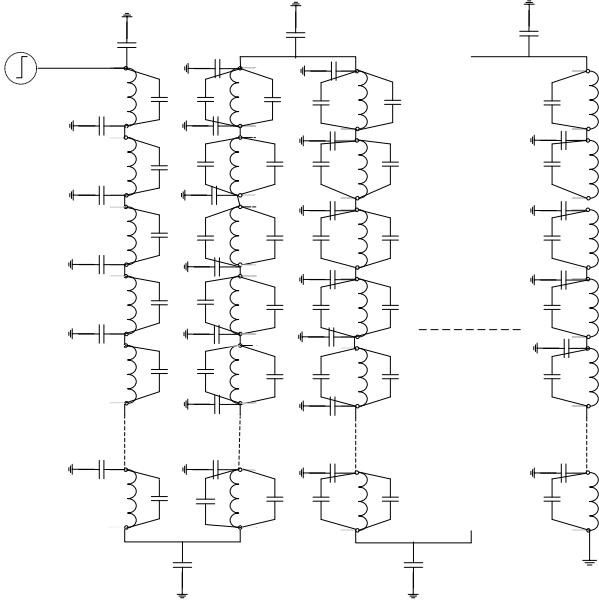


Figure 4. Simplification of the circuit from Figure 1.

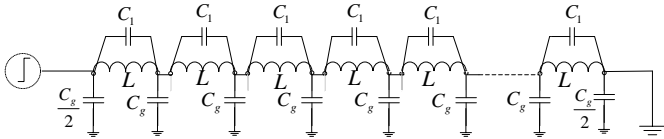


Figure 5. Final lumped-parameter model for transformer voltage distribution studies

### C. Inductance and capacitance matrix

Inductances are calculated by the well known Maxwell formulas on a turn-to-turn basis [22]. The  $\mathbf{L}$  matrix is formed in a way that diagonal elements of the matrix correspond to a group of turns. The off-diagonal elements are mutual inductances between different groups of turns. For simplicity in this case, the number of turns in a group is kept constant. The studied transformer has 10 layers with approximately 142 turns per layer. Each layer is divided in 10 groups with 14 turns per group. So, we assume that a layer consists of 10 groups. So the transformer  $\mathbf{L}$  matrix is of order 100x100. The capacitance matrix is built on a node-to-node basis and because the number of nodes  $N=B+1$  where  $B$  is the number of branches represented by inductances, the capacitance matrix is of order 101x101.

Finally, by making use of the inductance matrix  $\mathbf{L}$  and the capacitance matrix  $\mathbf{C}$ , impedance and admittance matrices  $\mathbf{Z}$  and  $\mathbf{Y}$  are determined [22]:

$$\begin{aligned} \mathbf{Z} &= \left( j\omega + \sqrt{\frac{2\omega}{\sigma\mu_0 d^2}} \right) \mathbf{L} \\ \mathbf{Y} &= (j\omega + \omega \tan \delta) \mathbf{C} \end{aligned} \quad (1)$$

where

- $d$  - is the distance between layers,
- $\sigma$  - is the conductor conductivity,
- $\tan \delta$  - is the loss tangent of the insulation.

### III. TRANSFORMER MODELING

According to [17], a general representation of N-winding transformer can be done by discretizing the transmission line equations. The general govern equations for the voltages and currents are:

$$\frac{dV_i(x)}{dx} = \sum_{j=1}^N - \int_0^{\lambda_j} Z_{ij}(x, \beta) I_j(\beta) \quad i=1, 2, \dots, N \quad (2)$$

$$\frac{dI_i(x)}{dx} = \sum_{j=1}^N - \int_0^{\lambda_j} Y_{ij}(x, \beta) V_j(\beta) \quad i=1, 2, \dots, N \quad (3)$$

Equations (2) and (3) are general equations that represent N-winding transformer model. In (2),  $I_j(\beta)$  is the inductive current at a distance  $\beta$  down the  $j$ th winding, and  $Z_{ij}(x, b)$  is a mutual impedance function. The self- and mutual impedance is frequency dependent, equation (2) is also in frequency domain, so the  $V_i(x)$  and  $I_j(\beta)$  are Fourier transformer of  $V_i(x, t)$  and  $I_j(\beta, t)$  respectively.  $\lambda_j$  represents the length of the  $j$ th winding. Because we are dealing with only one winding, the computation can be rather simplified, so the solution can be represented in a matrix form:

$$\begin{bmatrix} \mathbf{I}_B \\ \mathbf{V}' \end{bmatrix} = \begin{bmatrix} \mathbf{A} & \mathbf{B} \\ \mathbf{C} & \mathbf{D} \end{bmatrix} \begin{bmatrix} \mathbf{V}_B \\ \mathbf{V}' \end{bmatrix} \quad (4)$$

where  $\mathbf{V}_B$  represents the set of voltages at the winding terminals, and  $\mathbf{I}_B$  represents the set of currents entering them:

$$\mathbf{V}_B = \begin{bmatrix} \mathbf{V}_S \\ \mathbf{V}_R \end{bmatrix}, \quad \mathbf{I}_B = \begin{bmatrix} \mathbf{I}_S \\ -\mathbf{I}_R \end{bmatrix} \quad (5)$$

Applying equation (5), one can calculate the voltages in the internal nodes as:

$$\mathbf{V}' = (\mathbf{1} - \mathbf{D})^{-1} \mathbf{C} \mathbf{V}_B \quad (6)$$

More about derivation of (6) and corresponding submatrices  $\mathbf{A}$ ,  $\mathbf{B}$ ,  $\mathbf{C}$  and  $\mathbf{D}$  can be found in [17]. The time domain solutions are calculated by continuous inverse Fourier transform [18].

### IV. DESCRIPTION OF THE MEASURING SETUP

The measuring setup is done similar to the motor switching test circuit IEC 62271-110 [23]. The supply transformer is a special laboratory transformer with a voltage ratio 0.5/100 kV and nominal power of 50 kVA. Because the nominal current is 0.5 A, only switching-in tests at different voltage levels and at low current are performed. A 30 k $\Omega$  resistor on the high-voltage transformer side is installed to limit the load current and protect the transformer from high currents. So, the circuit is realized in a way to produce negligible current. On the high-voltage side of the supply transformer, a spark gap with a breakdown voltage of 20 kV is installed in order to protect the

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circuit from high overvoltages. Furthermore, only single-phase switch-in operations are performed, so the other two phases are grounded through a grounding switch AS. The test transformer is designed in a way that during measurements in one phase, the other two phases are disconnected and the end of the measured phase is grounded. The transformer switching test circuit is shown in Figure 6. A photo of the test setup is presented in Figure 7. During switching, a prestrike effect in the VCB takes place, so surges propagate along the cable and reach the transformer windings. The voltages are measured at the transformer terminal and at the measuring points installed along the winding.

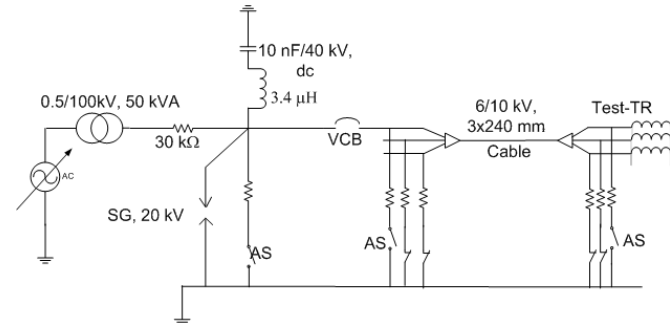


Figure 6. Transformer switching test circuit.



Figure 7. Transformer switching test circuit.

Voltages are measured by applying 20 kV PMK voltage probes between a specific measuring point and the ground, and currents are measured by a high frequency Pearson Electronic current probe. Both, currents and voltages are recorded by a 4-channel Nicolet Genesis transient recorder with a resolution of 14 bits and a sampling rate of 100 MS/s.

TABLE II  
CABLE DATA

Resistance (at 90 <sup>o</sup> C, 50 Hz)	0.161 Ω/km
Reactance (at 50 Hz)	0.088 Ω/km
Capacitance	0.41 μF/km
Length	100 m
wave travel time (measured)	5.7E-7 s

Cable data provided by the manufacturer are summarized in Table II. The travel time of the wave along the cable is measured by a applying a pulse with a short rise time at the

sending end of the cable, and recording the response at the receiving end.

## V. TEST RESULTS

### A. VCB switching-in test

Switching tests with the vacuum circuit breaker are done at different voltage levels. The voltage is changed between 4 kVrms and 12 kVrms with a step of 2 kVrms. Furthermore, measurements are done with and without cable. Table III summarizes the results of the measurements which are presented here.

TABLE III  
PERFORMED TYPES OF MEASUREMENTS

		4kV	6 kV	8kV	12kV
Phase B	with cable		x	x	
	no cable			x	x
Phase C	with cable			x	
	no cable	x			

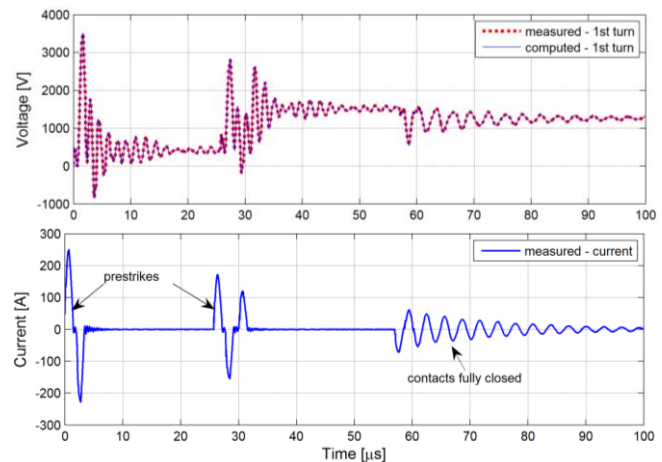


Figure 8. Measured and computed transformer terminal voltage in phase B during transformer energizing with applied voltage of 6 kV (upper figure); measured circuit breaker current (lower figure).

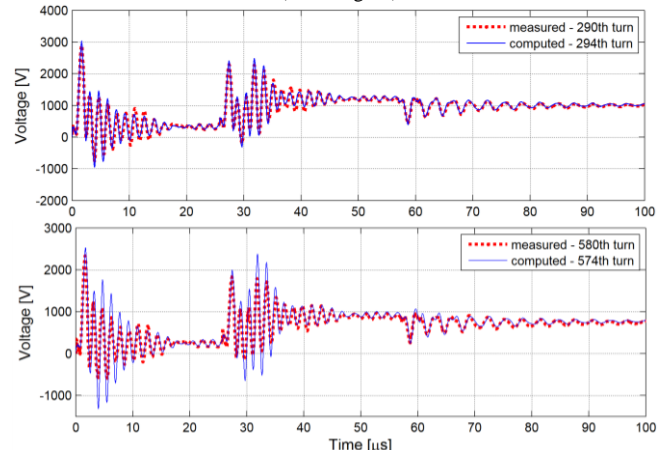


Figure 9. Measured and computed voltages at specific turns in phase B during transformer energizing with applied voltage of 6 kV.

Figure 8 through Figure 12 shows the results of the case when the transformer phase B is energized by supply voltage of 6 kV and 8 kV. During energizing the transformer, a prestrike occurs before the contacts physically touch each other. Figure 8 shows the first test done with a supply voltage of 6 kV. This test is followed by two prestrikes. After approximately 25 μs

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from the second prestrike, the contacts fully close and the load current is established. Figure 9 shows measured and computed voltages at specific points during 6 kV transformer energizing.

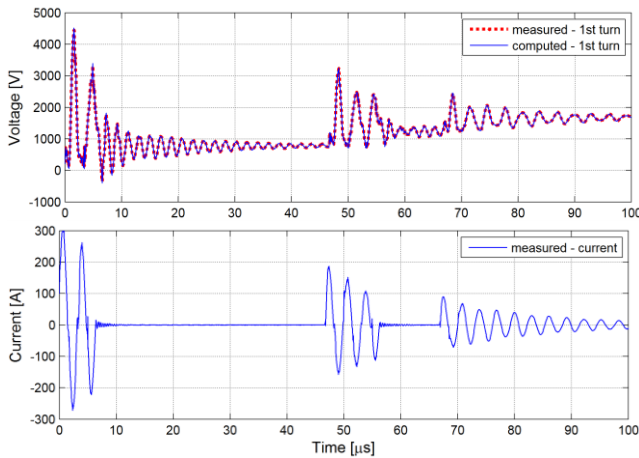


Figure 10. Measured and computed transformer terminal voltage in phase B during transformer energizing with applied voltage of 8 kV (upper figure); measured circuit breaker current (lower figure).

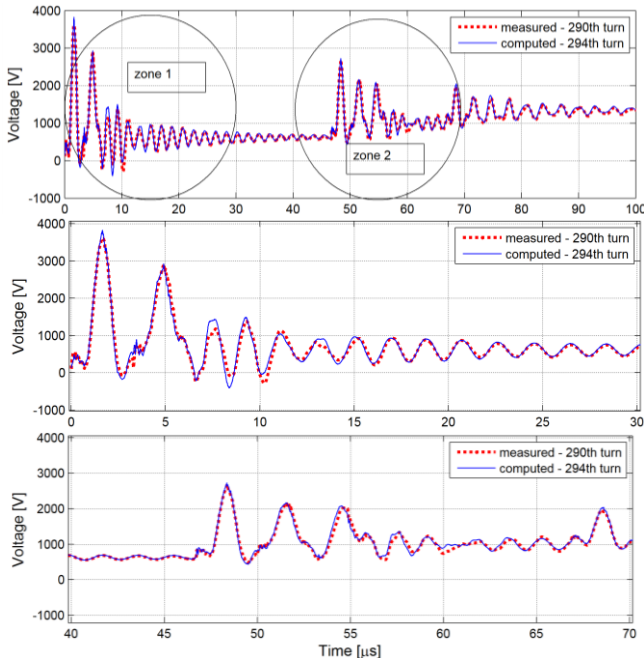


Figure 11. Measured and computed voltages in phase B during transformer energizing with applied voltage of 8 kV (upper figure); zone 1, first 30 μs (middle figure); zone 2, 40 - 70 μs (lower figure).

The next test is done with a supply voltage of 8 kV as shown in Figure 10. In this case, two prestrikes can be seen just as in the previous case, and the duration of the prestrike current is longer. This is according to the expectations; the higher the system voltage, the higher the duration of the prestrikes.

The oscillation frequency of the prestrike current is about 280 kHz. This frequency normally depends on the source side equivalent capacitance, load side equivalent capacitance and cable inductance [8]. However, this analysis shows that this is actually the lower resonance cable frequency  $f_0 = 1/(2\pi\tau) \approx 279.36$  kHz, where  $\tau = \sqrt{LC}$ ;  $L$  (H) and  $C$  (F) are cable inductance and capacitance respectively.

The oscillation frequency of the transformer voltages after the clearing of the prestrike current is approximately 500 kHz. This is the upper resonance frequency of the cable.

The amplitude of the current during second prestrike, as can be seen from Figure 8 and Figure 10 has lower value than that during the first prestrike. The reason for this is that the prestrike current depends on the withstand voltage between the circuit breaker contacts. Prestrike occurs when the transient recovery voltage is greater than the withstand voltage. As the contacts approach to each other, the withstand voltage is lower and the prestrike current decreases accordingly.

In all figures, measured and computed voltages are represented. For the turn 1 which is the terminal transformer voltage, there is a very good matching. From the measured voltage a numerical Fourier transform is done. The computed result is the inverse Fourier transform. This actually shows that the time domain solution is correctly obtained. This is important because the measured voltage at the transformer terminal is an input parameter for the determination of the voltage distribution in all windings. Furthermore, it can be seen that there is a good agreement between measured and computed voltages.

Figure 11 presents measured and computed voltages for the second test with supply voltage of 8 kV in phase B. Voltage transients in the 290<sup>th</sup> turn are measured and compared with the computed transients in the 294<sup>th</sup> turn. Figure 11 shows the enlarged time scale for the zone 1 and zone 2.

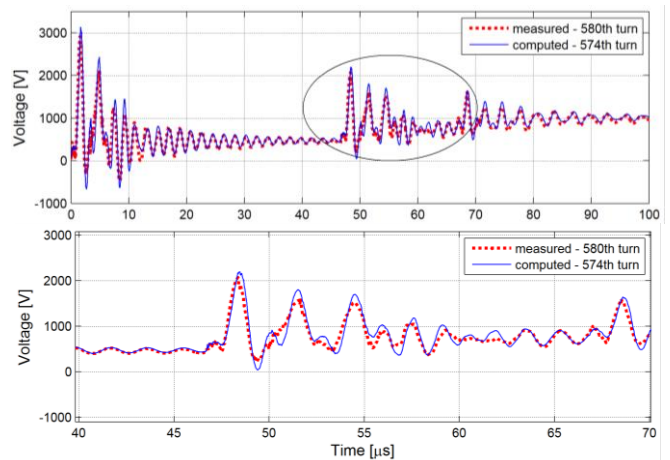


Figure 12. Measured and computed voltages in phase B for transformer energizing with applied voltage of 8 kV (upper figure); increased time scale between 40 - 70 μs (lower figure).

Also enlarged time scale between 40 μs and 70 μs in Figure 12 is shown for voltage transients recorded and computed in the 580<sup>th</sup> and 574<sup>th</sup> turn respectively.

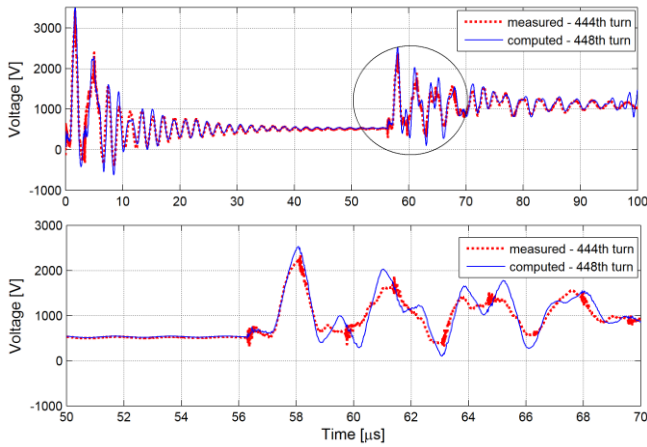


Figure 13. Measured and computed voltages in phase C for transformer energizing with applied voltage of 8 kV (upper figure); increased time scale between 50 - 70  $\mu$ s (lower figure).

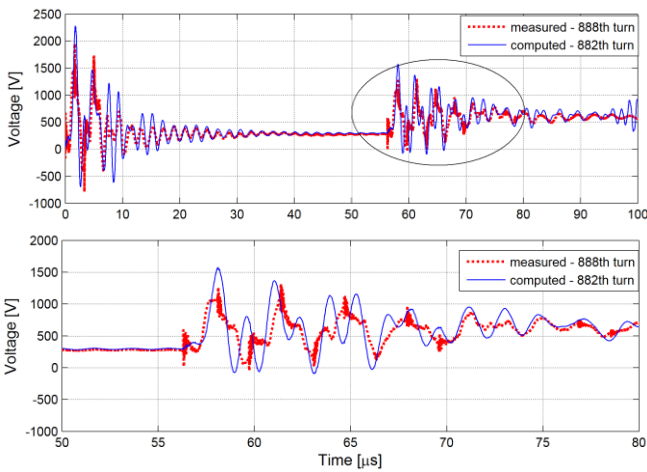


Figure 14. Measured and computed voltages in phase C for transformer energizing with applied 8 kV (upper figure); increased time scale between 50 - 80  $\mu$ s (lower figure).

Figure 13 and Figure 14 shows the results during transformer energizing of phase C with 8 kV supply voltage. In this phase, the 444<sup>th</sup> turn and 888<sup>th</sup> turn are supplied with measuring points. The comparison shows that the measured and computed results in the 888<sup>th</sup> turn differ more during the period of reignitions than those computed for the 294<sup>th</sup> and 574<sup>th</sup> turn in phase B. This means that the error rises as the turn number increases. This is most probably because of the frequency-dependent losses which provide higher damping than the damping that results from the losses as estimated by (1).

Figure 15 presents the results of the case when the transformer is energized without applying a cable between the circuit breaker and the transformer. The supply voltage is 4 kV. Recorded voltage in 444<sup>th</sup> turn is compared by the computed voltage in 434<sup>th</sup> turn. It can be seen that the prestrike current in this case is eliminated after half cycle.

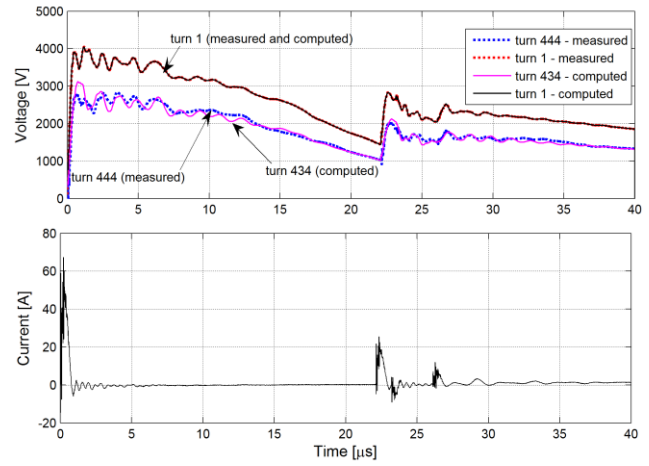


Figure 15. Measured and computed voltages in phase C (upper figure); measured circuit breaker current (lower figure).

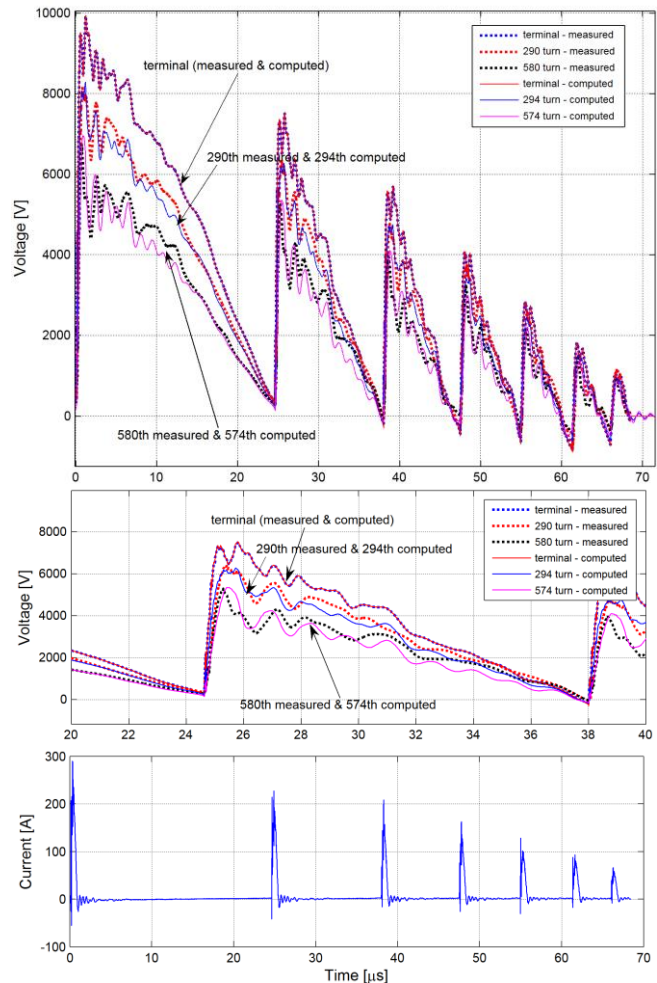


Figure 16. Measured and computed voltages in phase B (upper figure); increased time scale (middle figure); measured circuit breaker reignition current (lower figure); source voltage is 8 kV.

In Figure 16, the results of a switching test without a cable between the VCB and transformer are presented for a supply voltage of 8 kV. Solid lines in the upper and in the middle figure represent the computed results, whilst dotted lines show the measured results. The prestrike current (just as in the previous case – see Figure 15) is damped rapidly, and the

voltage decreases rapidly after arc extinction. The reason for this is that the load voltage side capacitance is very low and consists only of the transformer bushing capacitance and busbar capacitance that connects the circuit breaker and transformer. In this case, the voltage escalates more than in the case when a cable exists between the VCB and transformer.

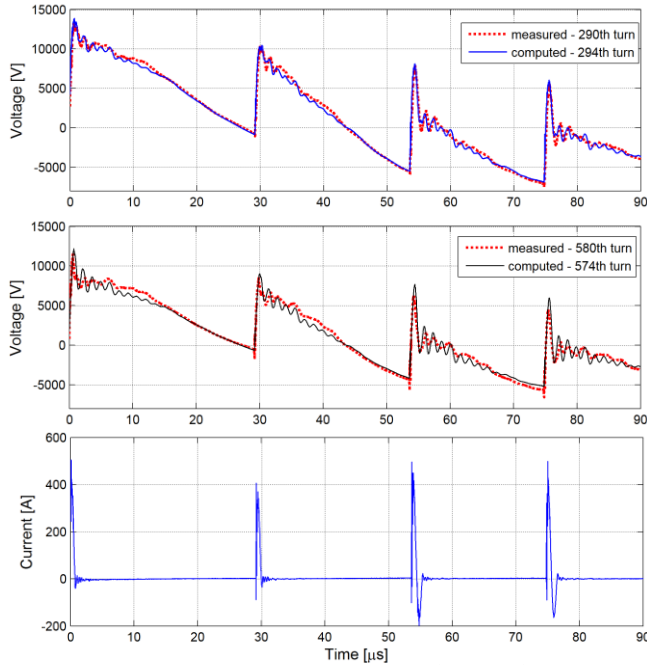


Figure 17. Measured and computed voltages of 290<sup>th</sup> and 294<sup>th</sup> turn in phase B (upper figure); measured and computed voltages of 580<sup>th</sup> and 574<sup>th</sup> turn in phase B (middle figure); measured circuit breaker reignition current (lower figure); source voltage is 12 kV.

Figure 17 is a similar example for a case when the supply voltage is 12 kV.

## VI. DISCUSSION

Transformer characteristic is measured for open and short-circuited LV winding. In each of them, two impedance amplitude and phase values are determined. These values correspond to the resonance frequencies of the cable.

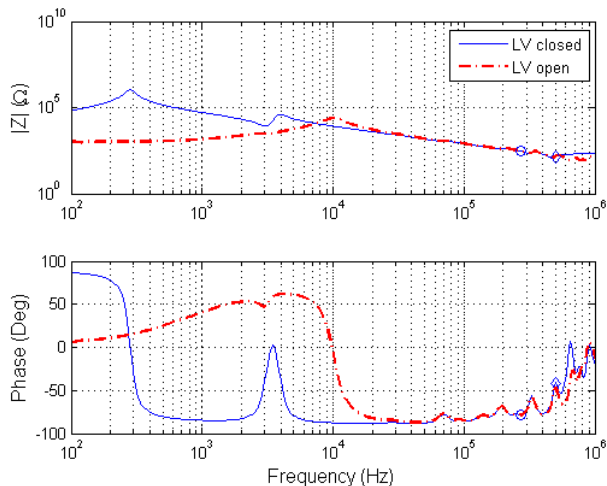


Figure 18. Transformer terminal impedance characteristic; amplitude characteristic (upper figure); phase characteristic (lower figure).

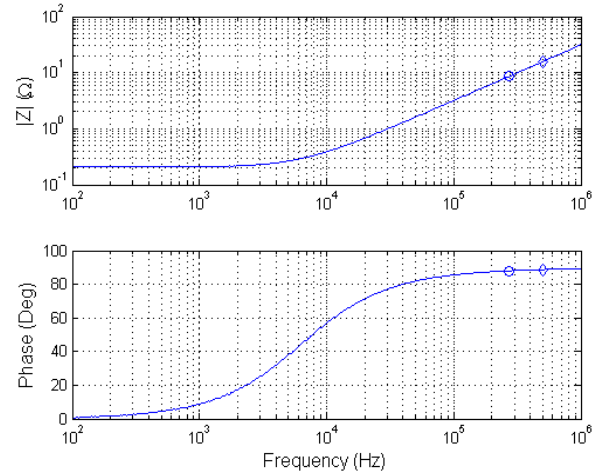


Figure 19. Bus-bar terminal impedance characteristic; amplitude characteristic (upper figure); phase characteristic (lower figure).

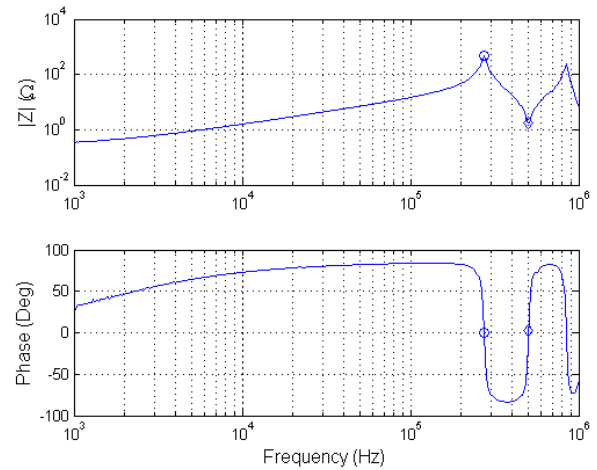


Figure 20. Terminal impedance characteristic of the cable (receiving end of the cable short circuited); amplitude characteristic (upper figure); phase characteristic (lower figure).

Figures 18, 19 and 20 show measured amplitude and phase terminal impedance characteristics of the transformer, the busbar and the cable used in the test circuit of Figure 7. The ratio between the terminal transformer voltage and the supply voltage can be approximately determined by:

$$k \approx \frac{Z_{tr}}{Z_{tr} + Z_{bus} + Z_{cab}}, \quad U_T = k \cdot U_S \sqrt{2} \quad (7)$$

where  $U_T$  is the maximum transformer terminal voltage, and  $U_S$  is the rms value of supply voltage. In (7), absolute values of the impedances are used.

TABLE IV  
MEASURED IMPEDANCES AT SPECIFIC RESONANCE FREQUENCIES

Frequency	~ 280 kHz	~500 kHz
$\underline{Z}_{tr}$	58.86-j280.9	103.11-j90.7
$\underline{Z}_{bus}$	0.29+j8.65	0.334+j15.89
$\underline{Z}_{cab}$	463-j0.085	1.73+j0.0925

Table IV shows the terminal impedances of the transformer, the busbar and the cable at cable's resonance frequency



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computed from the measured characteristics. The frequency of the prestrike current is approximately 280 kHz, so the voltage division factor is  $k = 0.378$ . For source voltages 6 kVrms and 8 kVrms, the calculated maximum transformer voltages are 3.2 kV and 4.26 kV respectively. This approach explains why the maximum terminal transformer voltage increases slightly with the increase of the supply voltage when a cable is applied between the transformer and the circuit breaker.

After the prestrike current is cleared, transformer terminal voltage oscillates with a frequency of 500 kHz. From Figure 20, it can be seen that this frequency is the second resonance frequency of the cable. So, the frequency of the transformer terminal voltage depends on the transformer equivalent inductance and capacitance, and the busbar inductance at this frequency. From Figure 19, the busbar inductance at 500 kHz is estimated as 5  $\mu\text{H}$ . Taking into account a transformer bushing capacitance of approximately 1 nF, and making use of measured transformer impedance from Table IV, one can easily derive a transformer inductance of 72.5  $\mu\text{H}$ . This implies a frequency of 591 kHz.

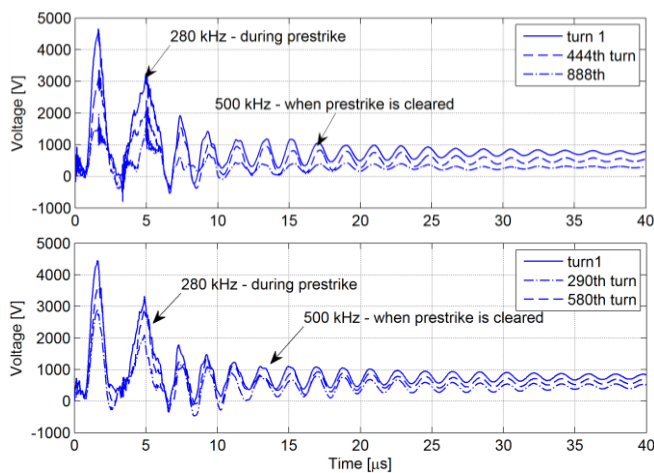


Figure 21. Voltage distribution along the transformer winding for applied voltage of 8 kV; upper figure – phase C, lower figure – phase B.

Figure 21 shows two different tests of measured voltages at different turns along transformer windings in phase B and phase C. It can be seen that the frequency of the voltage oscillations, after the prestrike current is cleared is the same, and it is also around 500 kHz. Therefore, using Figure 5 another simplified analysis of the oscillation frequency of the internal voltages is done. One  $L$  in parallel with  $C_1$  leads to a frequency of 650 kHz. However, in this approximation no influence from the mutual inductances that correspond to the inductance matrix  $\mathbf{L}$  is taken into account.

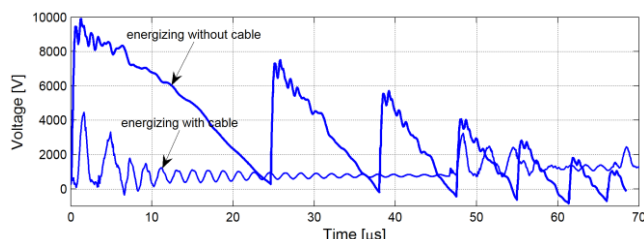


Figure 22. Comparison between measured transformer terminal voltages when the transformer is energized with and without a cable; Source voltage is 8 kV.

This implies that the actual frequency will be much lower than 650 kHz. Furthermore, a linear distribution of the voltage amplitudes can be seen. Figure 22 shows the measured transformer terminal voltage with and without a cable. The amplitude of the voltage during prestrike when a cable is applied is less than the half of the voltage when the transformer is energized without a cable.

## VII. CONCLUSION

Transformers can be exposed to very fast voltage transients which occur due to prestrike or restrike effect of the circuit breaker. Transformer insulation will deteriorate and finally fail when the transformer is frequently exposed to these transients. Surge voltages are dangerous not only with their amplitude but also with their rate of rise. Therefore, in order to design the transformer insulation, it is important to simulate the voltage wave forms more accurately. Especially, the voltage escalation during prestrikes or restrikes has very high rate of rise, and therefore an accurate transformer model is important. In this work, switching tests are done with and without cable connected between the circuit breaker and transformer.

From the results, it can be seen that the case when a cable exists is different from that when no cable exists. The cable contributes to longer frequency oscillations and lower voltage amplitudes, whilst switching the transformer without cable will contribute to steeper voltage rise and short duration of the restrike current.

This work shows that the lumped-parameter model based on discrete telegraphist's equations can be used with full success to study voltage transients along transformer windings. The modeling needs only information about the geometrical dimensions of the transformer which can be easily obtained by the manufacturer.

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## IX. REFERENCES

- [1] B.K.Gupta, E.P.Dick, A. Greenwood, M. Kurtz, T.S. Lauber, B.A. Lloyd, A. Narang, P.R. Pillai, G.C. Stone: "Turn Insulation Capability of Large AC motors: Vol. 2, Appendixes: Final Report", Technical Report, EPRI-EL-5862-Vol.2, 1988.
- [2] G. Stein: "A Study of the Initial Surge Distribution in Concentric Transformer Windings", *AIEE Transaction*, September 1964, pp. 877-892.
- [3] G.C. Damstra: Virtual Chopping Phenomena Switching Three-Phase Inductive Circuits, *Colloquium of CIGRE SC 13*, Helsinki, September 1981.
- [4] W.M.C. van den Heuvel, J.E. Daalder: "Interruption of a Dry Type Transformer in No-load by a Vacuum Circuit Breaker", EUT Report, Eindhoven, 1983, ISBN 90-6144-141-2.
- [5] A.O. Soysal: Protection of Arc Furnace Supply Systems From Switching Surges, *Proceedings of 1999 IEEE PES Winter Meeting*, 31

published in IEEE Transactions on Power Delivery in 2009; The paper has won IEEE PES Prize Award and IEEE Switchgear Committee Award in 2011.

- January-4 February 1999, New York, NY, Vol. 2, pp. 1092-1095, ISBN 0-7803-4893-1.
- [6] J. Kosmac, P. Zunko: A Statistical Vacuum Circuit Breaker Model for Simulation of Transient Overvoltages, *IEEE Transactions on Power Delivery*, Vol. 10, No. 1, January 1995, pp. 294-300.
  - [7] Cigre SC A3: "Electrical Environment of Transformers – Impact of Fast Transients", Summary Paper of the CIGRE JWG 12/32/23.21, A3-04 (SC) 26 IWD.
  - [8] M. Popov, L. van der Sluis, G. C. Paap: "Investigation of the Circuit Breaker Reignition Overvoltages Caused by No-load Transformer Switching Surges", *European Transactions on Electric Power (ETEP)*, Vol. 11, No. 6, November/December 2001, pp. 413-422.
  - [9] E. Colombo, G. Costa, L. Piccarreta: "Results of an Investigation on the Overvoltages due to a Vacuum Circuit Breaker When Switching an H.V. Motor", *IEEE Transactions on Power Delivery*, Vol. 3, No. 1, January 1988, pp. 205-213.
  - [10] J.L.Guardado, K.J. Cornick: "A Computer Model for Calculating Steep-Fronted Surge Distribution in Machine Windings", *IEEE Transaction on Energy Conversion*, Vol. 4, No.1, March 1989, pp. 95-101.
  - [11] J.L. Guardado, V. Venegaz, E. Melgoza, K.J. Cornick, J.L. Naredo: "Transient Overvoltages in Electrical Motors During Sequential Pole Closure", *IEEE Transaction on Energy Conversion*, Vol.14, No.4, December 1999, pp. 1057-1064.
  - [12] J.L. Guardado, V. Carrillo, K.J. Cornick: "Calculation of Interturn Voltages in Machine Windings During Switching Transients Measured on Terminals", *IEEE Transaction on Energy Conversion*, Vol.10, No.1, March 1995, pp. 87-94.
  - [13] Y. Shibuya, S. Fujita, N. Hosokawa: "Analysis of Very Fast Transient Overvoltages in Transformer Winding", *IEE Proceedings on Generation Transmission and Distribution*, Vol.144, No. 5, September 1997, pp.461-468.
  - [14] M. Popov, L. van der Sluis, G.C. Paap, H. de Herdt: "Computation of Very Fast Transient Overvoltages in Transformer Windings", *IEEE Transactions on Power Delivery*, Vol. 18, No. 4, October 2003, pp. 1268-1274.
  - [15] B. Gustavsen, A. Semlyen: Rational Approximation of Frequency Domain Responses by Vector Fitting, *IEEE Transactions on Power Delivery*, Vol. 14, No. 3, July 1999, pp. 1052-1061.
  - [16] B. Gustavsen: Computer Code for Rational Approximation of Frequency Dependent Admittance Matrices, *IEEE Transactions on Power Delivery*, Vol. 17, No. 4, October 2002, pp. 1093-1098.
  - [17] D.J. Wilcox: "Theory of Transformer Modelling Using Modal Analysis", *IEE Proceedings-C*, Vol. 138, No. 2, March 1991, pp.121-128.
  - [18] J.P. Bickford, N. Mullineux, J.R. Reed: "Computation of Power System Transients", IEE, Peter Peregrinus Ltd., 1976, ISBN 0901223859.
  - [19] R.C. Degeneff, W.J. McNutt, W. Neugebauer, J. Panek, M.E. McCallum, C.C. Honey: "Transformer Response to System Switching Voltage", *IEEE Transactions on Power Apparatus and Systems*, Volume PAS-101, No.6, June 1982, pp. 1457-1470.
  - [20] W.J. McNutt, T.J. Blalock, R.A. Hinton: "Response of Transformer Windings to System Transient Voltages": *IEEE Transactions on Power Apparatus and Systems*, Vol. PAS-93 (1974), pp. 457-467.
  - [21] R.C. Dugan, R. Gabrick, J.C. Wright, K.V. Pattern: "Validated Techniques for Modeling Shell-form EHV Transformers", *IEEE Transactions on Power Delivery*, Vol.4, No.2, April 1989, pp. 1070-1078.
  - [22] Y. Shibuya, S. Fujita: "High Frequency Model of Transformer Winding", *Electrical Engineering in Japan*, Vol. 146, no.3, 2004, pp. 8-15.
  - [23] IEC 62271-110 *High-voltage switchgear and control gear Part 110: Inductive load switching*.

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